

*Interaction of the Solar Wind with  
Weak Obstacles:  
Simulation Method and a Tour of Applications*

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World Space Environment Forum, Schloss Seggau, May 2005

## *Outline*

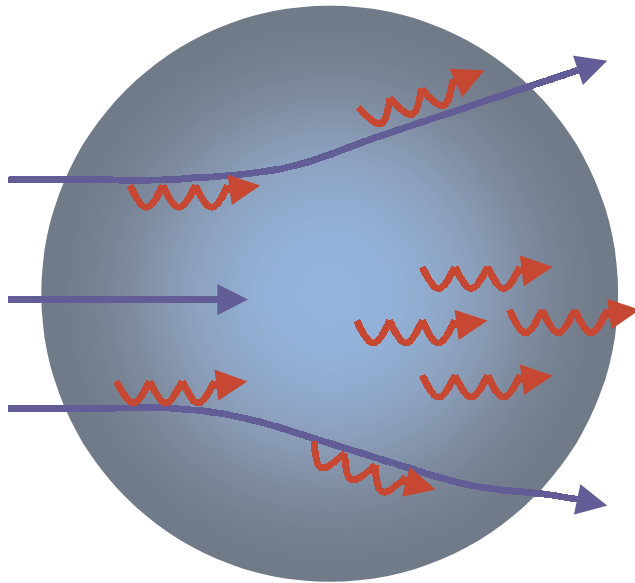
Background and scales

Simulation technique

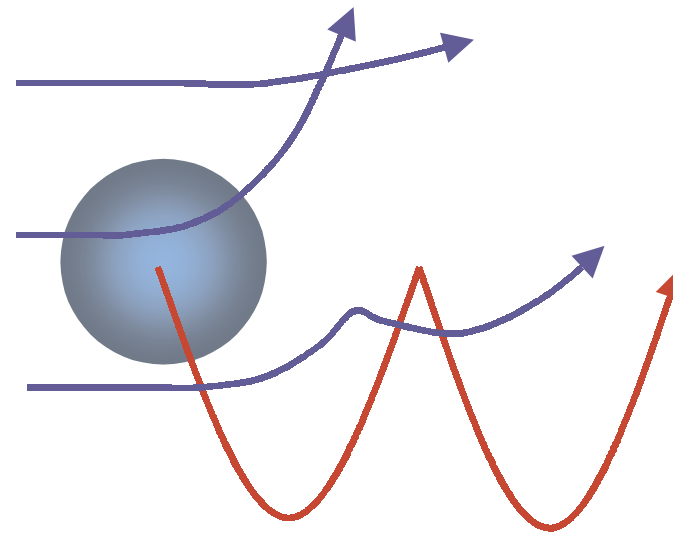
3D simulation results for

- Mars
- Weak Comets
- Titan
- Asteroids
- Extrasolar Planets

## *Strong vs. Weak Obstacles*

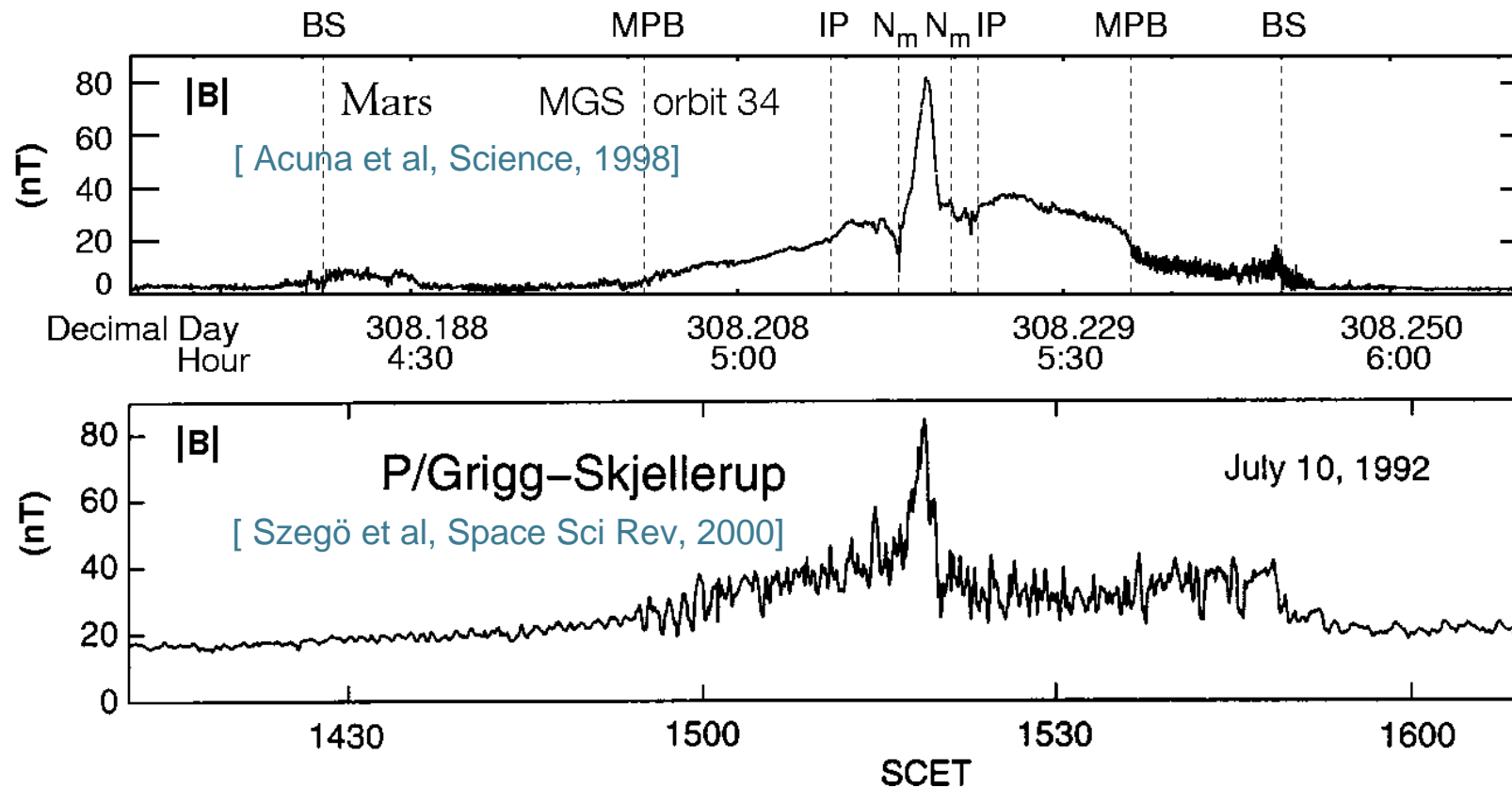


Strong: Jupiter, Earth,  
Halley



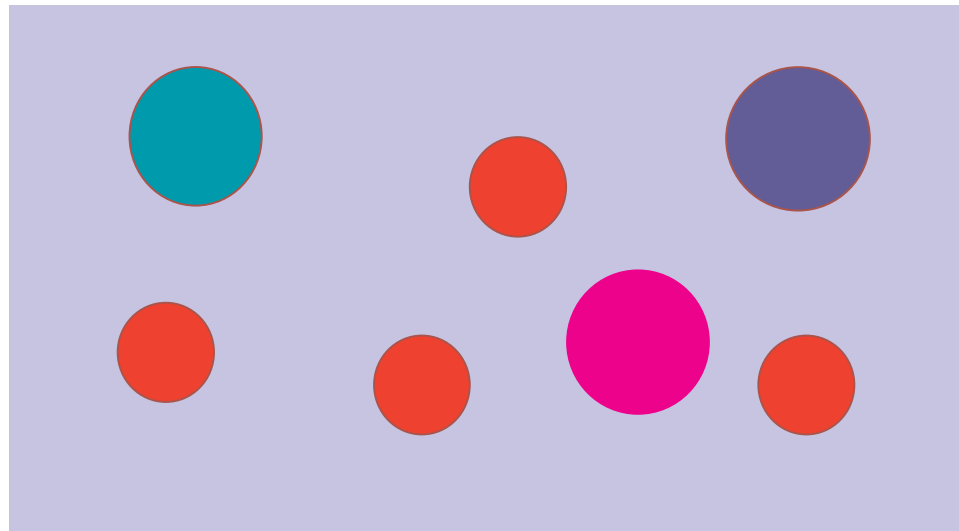
Weak: Mars, Titan,  
Asteroids,  
Churyumov-Gerasimenko

## Mars vs. Weak Comets



# *Simulation Technique*

(Hybrid model)



Electrons as fluid

Ions as particles:

Protons, Oxygen,

Water, Nitrogen,

...

## Basic Equations

Eq. of motion for ions:

$$\frac{d\underline{x}_s}{dt} = \underline{v}_s \quad \frac{d\underline{v}_s}{dt} = \frac{q_s}{m_s} (\underline{E} + \underline{v}_s \times \underline{B}) - \nu_{ns} n_n (\underline{v}_s - \underline{u}_n)$$

Electron fluid:

$$n_e m_e \frac{d\underline{u}_e}{dt} = -n_e e \underline{E} + \underline{J}_e \times \underline{B} - \nabla p_{e,sw} - \nabla p_{e,hi}$$

Ohm's law:

$$\underline{E} = -\frac{\underline{J}_i \times \underline{B}}{\rho_c} + \frac{\text{curl } \underline{B} \times \underline{B}}{\mu_0 \rho_c} - \frac{\nabla p_{e,sw} + \nabla p_{e,hi}}{\rho_c}$$

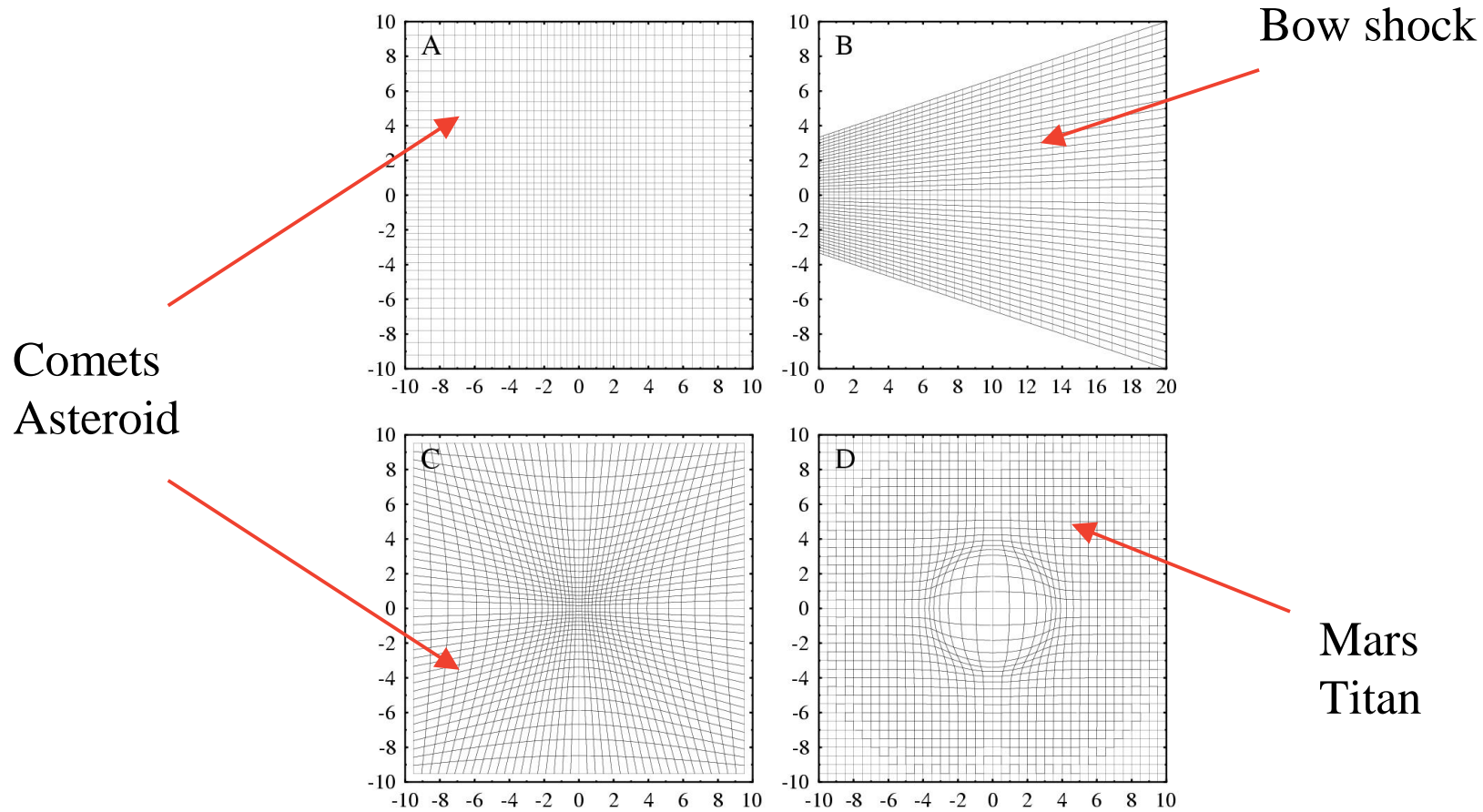
Adiabatic equation:

$$p_{e,sw} = \beta_{e,sw} \left( \frac{n_{sw}}{n_0} \right)^\kappa \quad p_{e,hi} = \beta_{e,hi} \left( \frac{n_{hi}}{n_0} \right)^\kappa$$

Faraday's law:

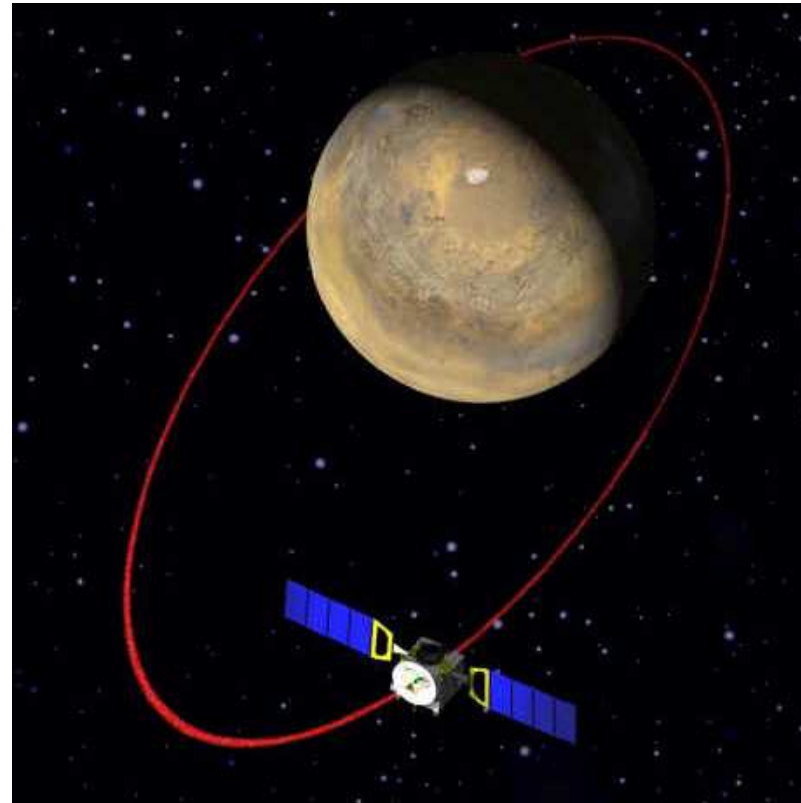
$$\frac{\partial \underline{B}}{\partial t} = \text{curl} \frac{\underline{J}_i \times \underline{B}}{\rho_c} - \text{curl} \frac{\text{curl } \underline{B} \times \underline{B}}{\mu_0 \rho_c}$$

## *Curvilinear Grids (3D)*



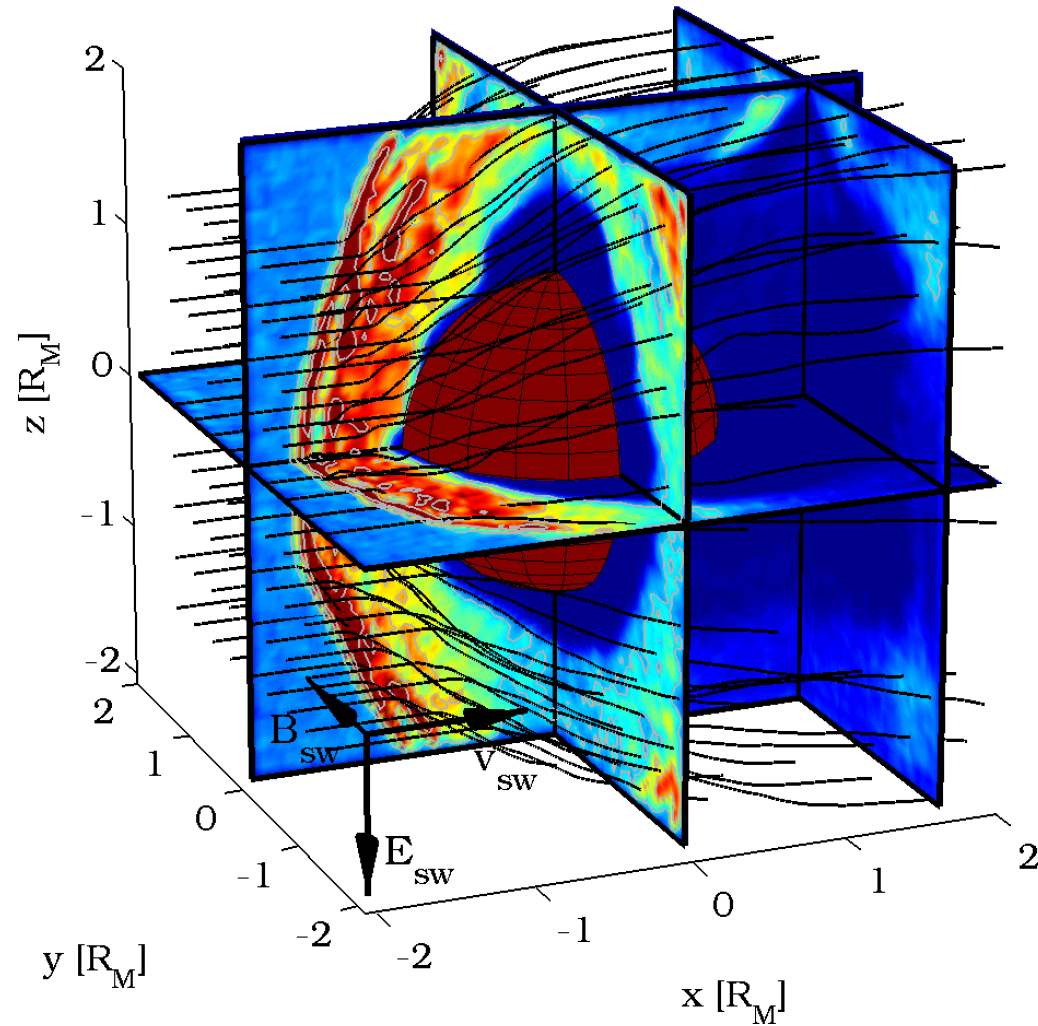
## *Simulation of Mars*

1989 Phobos  
1997 - Mars Global Surveyor  
2003 - Mars-Express



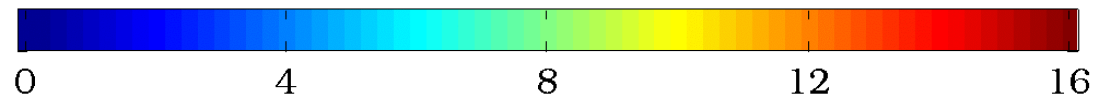


# Mars



[ Boesswetter et al,  
Ann. Geophys., 2004 ]

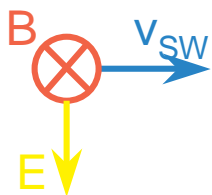
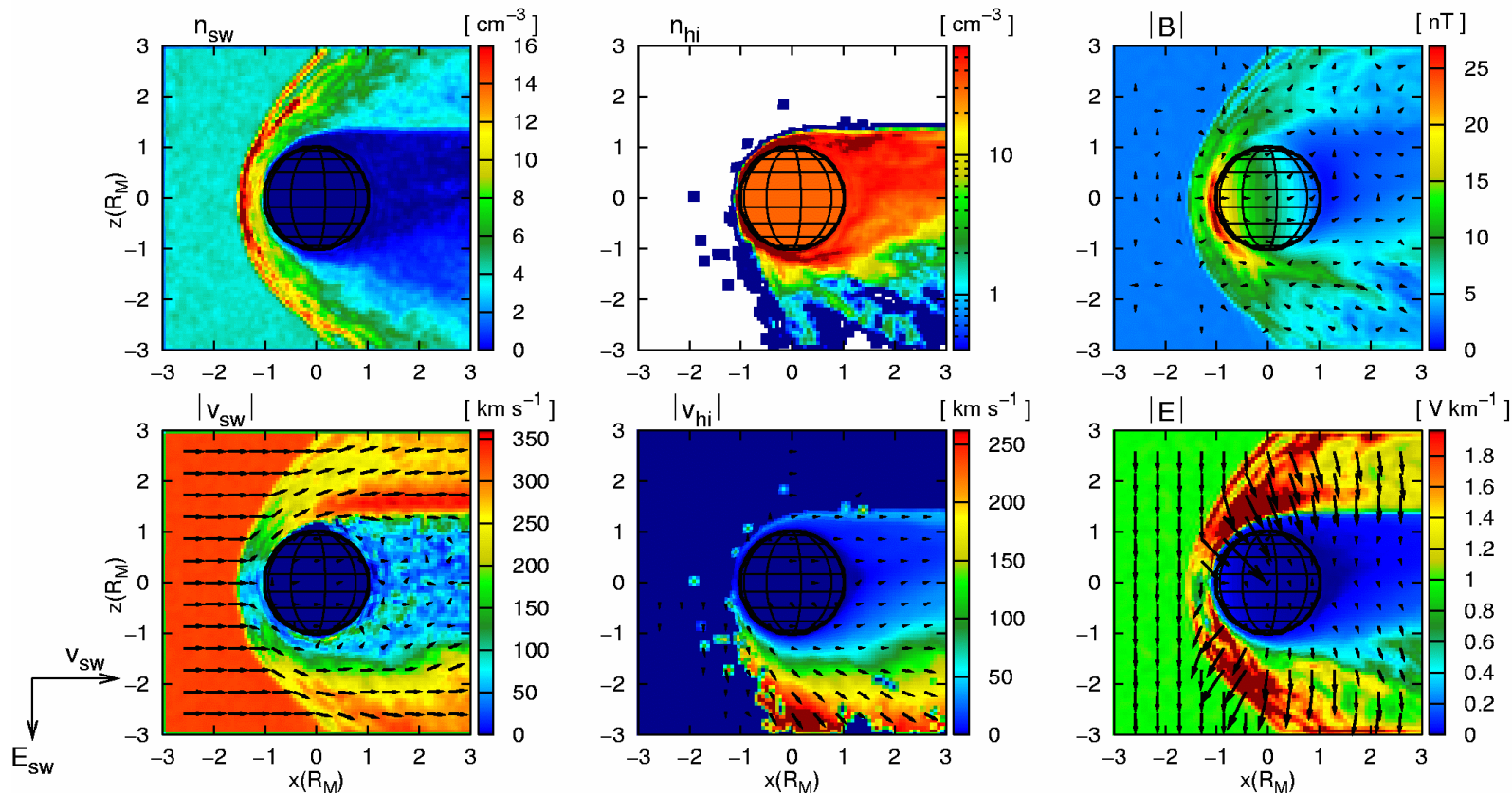
Solar wind density  $n_{sw}$  [ $cm^{-3}$ ]



# Polar Plane, $T_e = 0.3 \text{ eV}$

$t = 1392.1 \text{ s}$

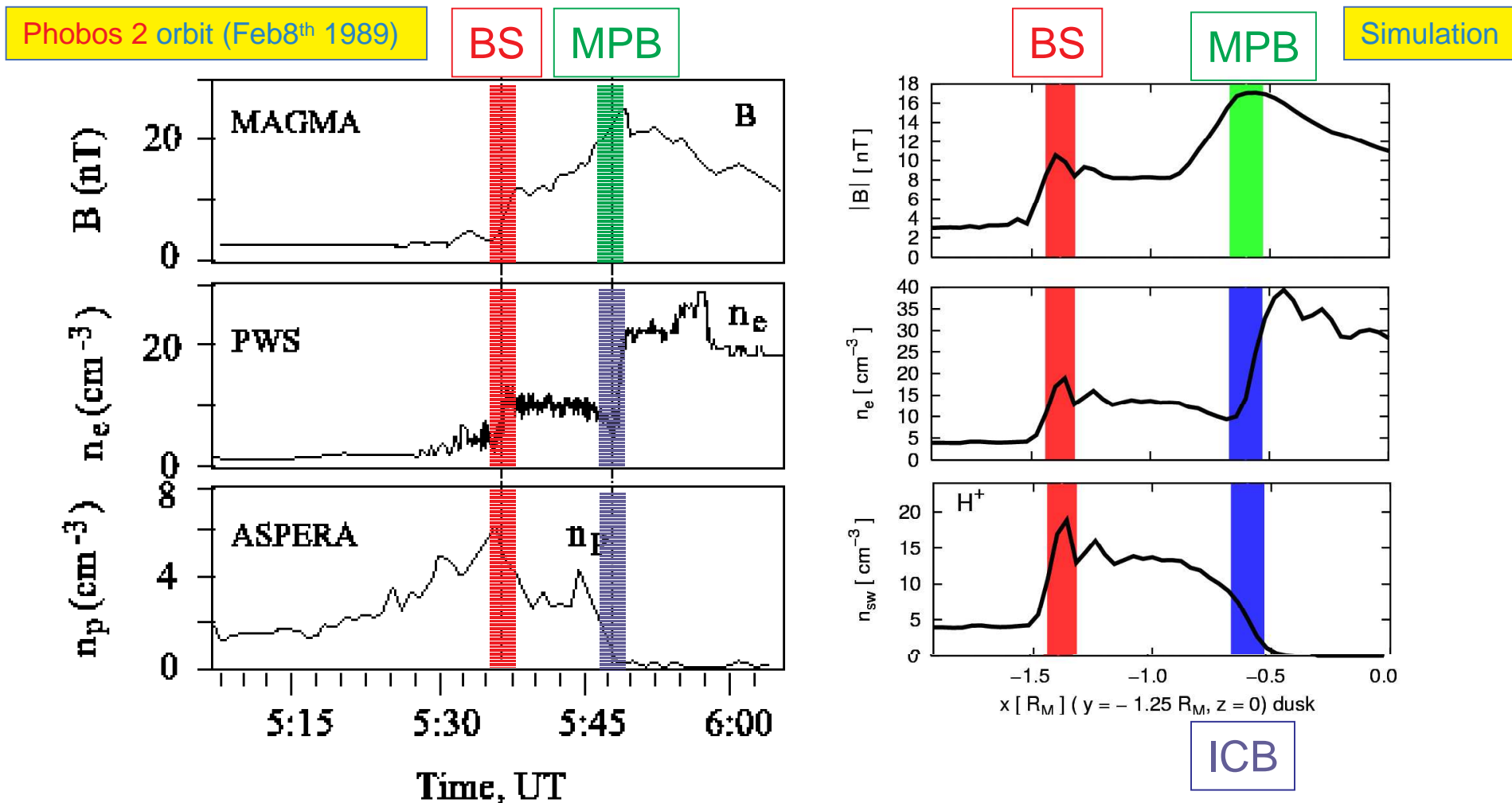
[ Bößwetter, Bagdonat, Motschmann; 2004 ]



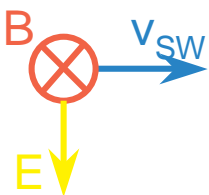
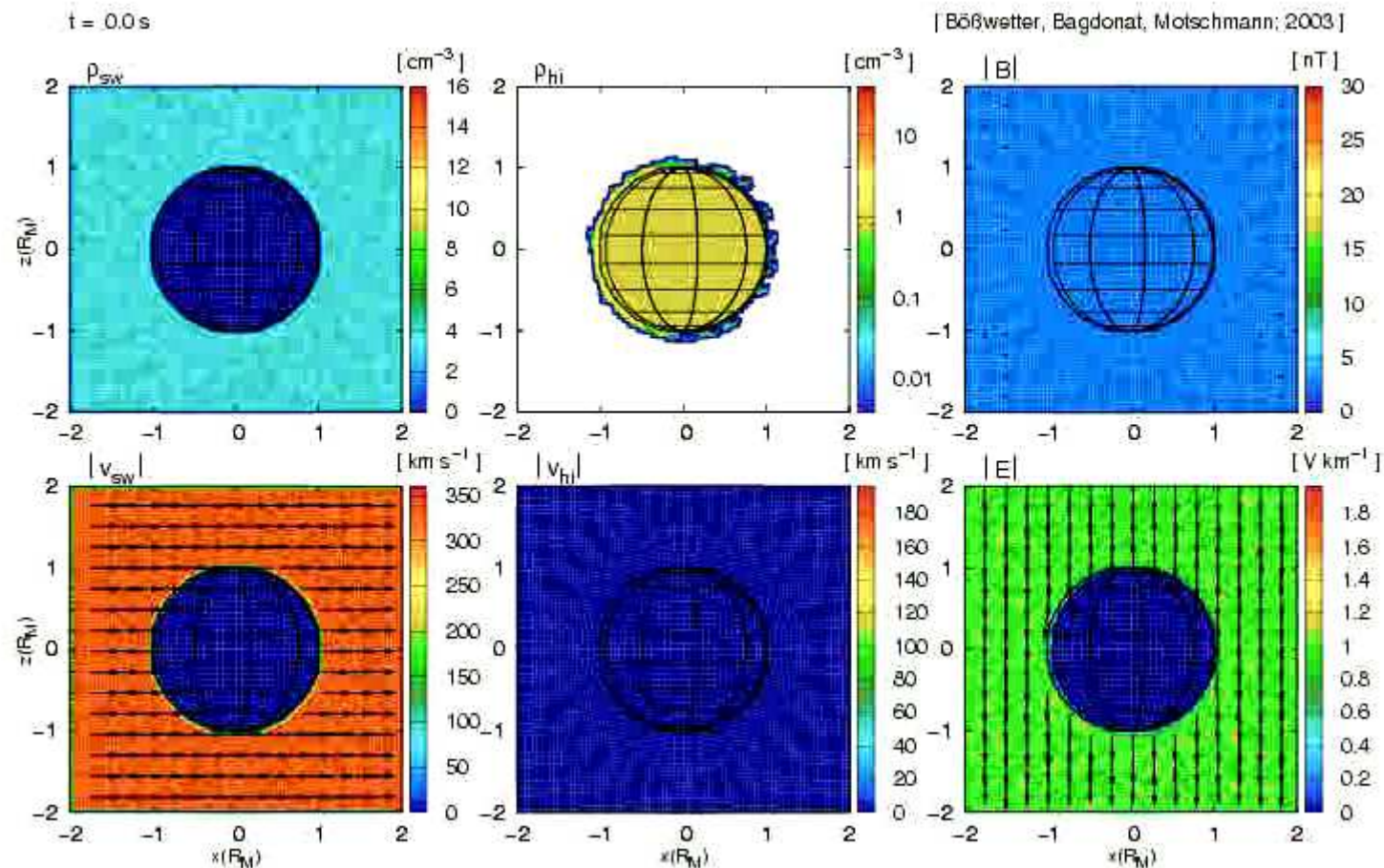
Total ion production rate:  $5.37 \cdot 10^{25} \text{ s}^{-1}$   
 Ionization frequency:  $2 \cdot 10^{-7} \text{ s}^{-1}$   
 Background magnetic field: 3 nT

Solar wind density:  $4 \text{ cm}^{-3}$   
 Alfvén Mach number: 10  
 Ion inertial length:  $c/\omega_{pi} = 114 \text{ km}$

# Comparison of observation and simulation



# Polar Plane, $T_e = 2 \text{ eV}$



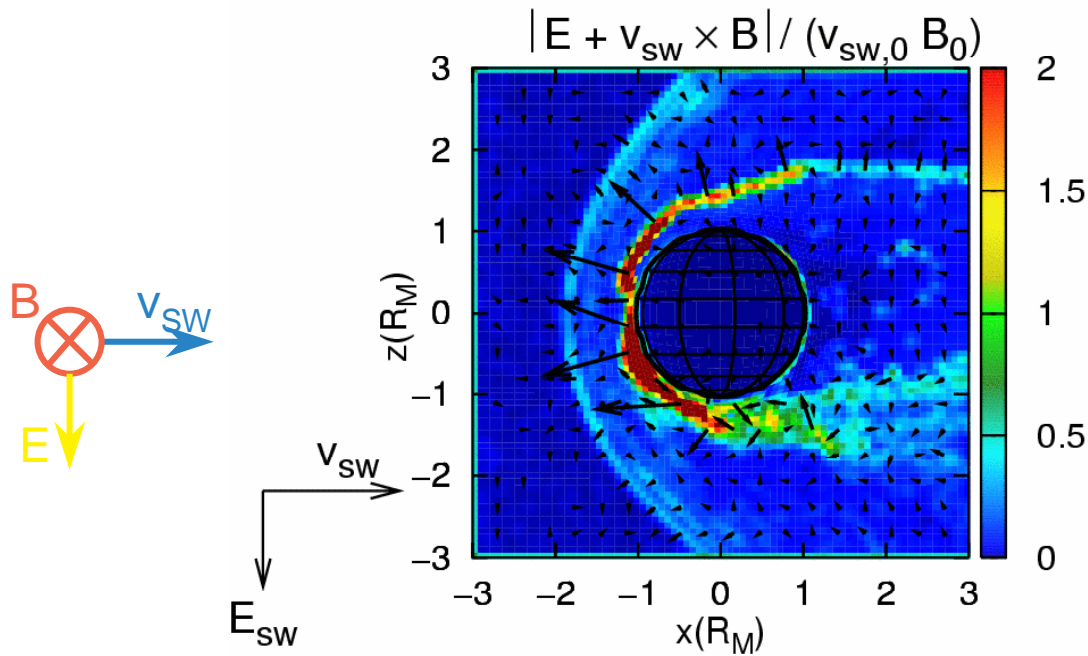
Total ion production rate:  $5.37 \cdot 10^{25} \text{ s}^{-1}$   
 Ionization frequency:  $2 \cdot 10^{-7} \text{ s}^{-1}$   
 Background magnetic field: 3 nT

Solar wind density:  $4 \text{ cm}^{-3}$   
 Alfvén Mach number: 10  
 Ion inertial length:  $c/\omega_{pi} = 114 \text{ km}$



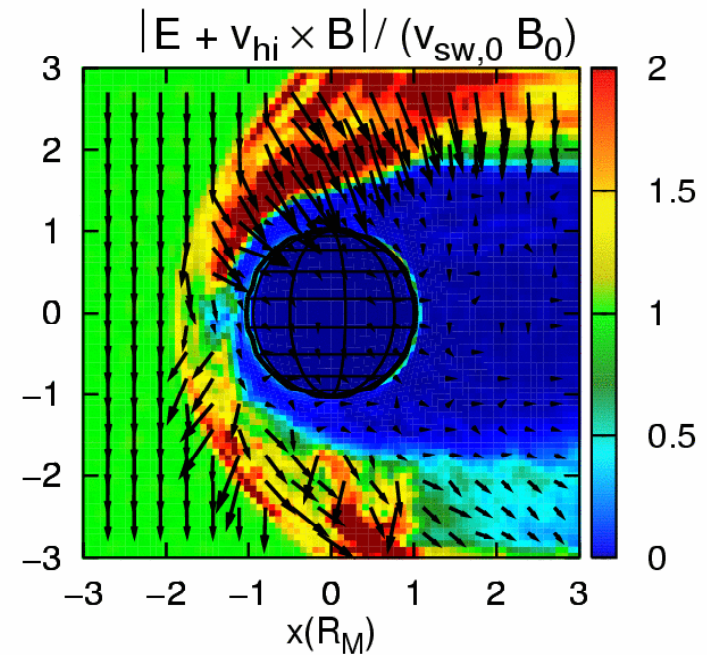
## Formation of the ICB/MPB

Force on solar wind protons



Gradient of the electron  
 pressure points **outward**  
 $\Rightarrow$  Reflection of SW protons

Force on  $O^+$  ions



Northern hemisphere:  
 Electric field of the SW  
 points **toward the planet**

# *Simulation of Comet Churyumov-Gerasimenko*

3.25 AU .....2.5 AU



# Simulation of CG at 3.25AU

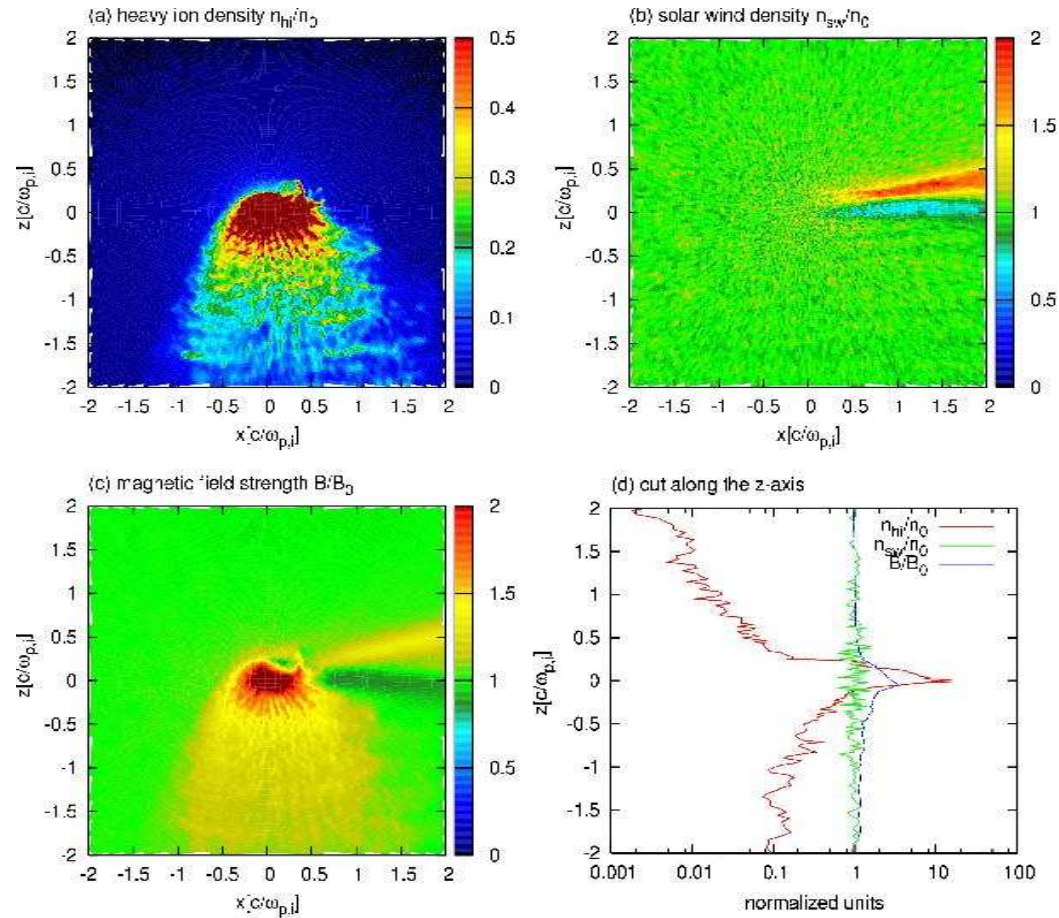
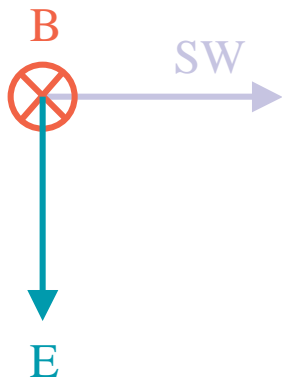
$$Q_n = 10^{24} \text{s}^{-1}$$

$$B_0 = 1.13 \text{nT}$$

$$n_0 = 0,66 \text{cm}^{-3}$$

$$M_{A0} = 10$$

$$x_0 = 280 \text{km}$$



[ Bagdonat et al, The new Rosetta Target, 2004 ]

# Simulation of CG at 2.5AU

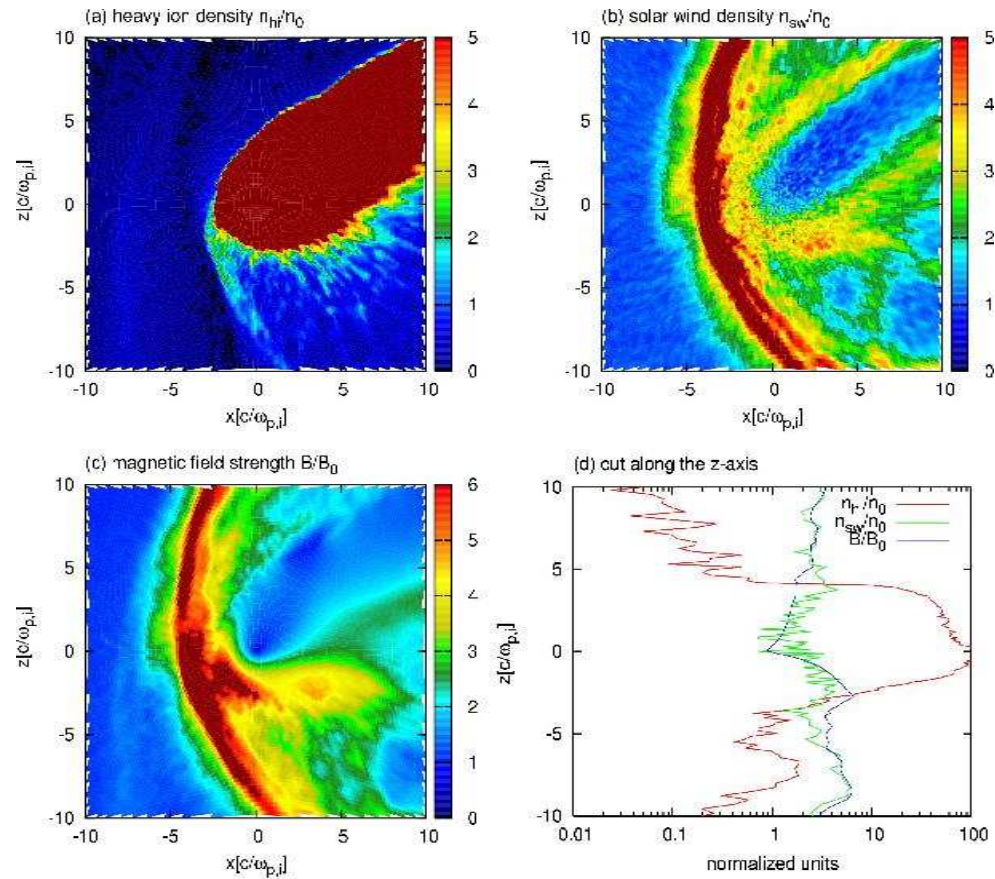
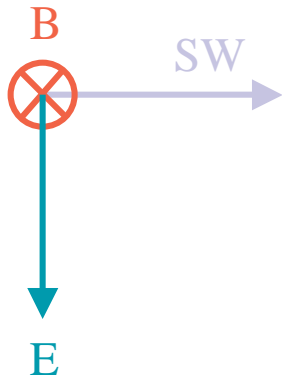
$$Q_n = 1.9 \cdot 10^{26} \text{s}^{-1}$$

$$B_0 = 1.5 \text{nT}$$

$$n_0 = 1,1 \text{cm}^{-3}$$

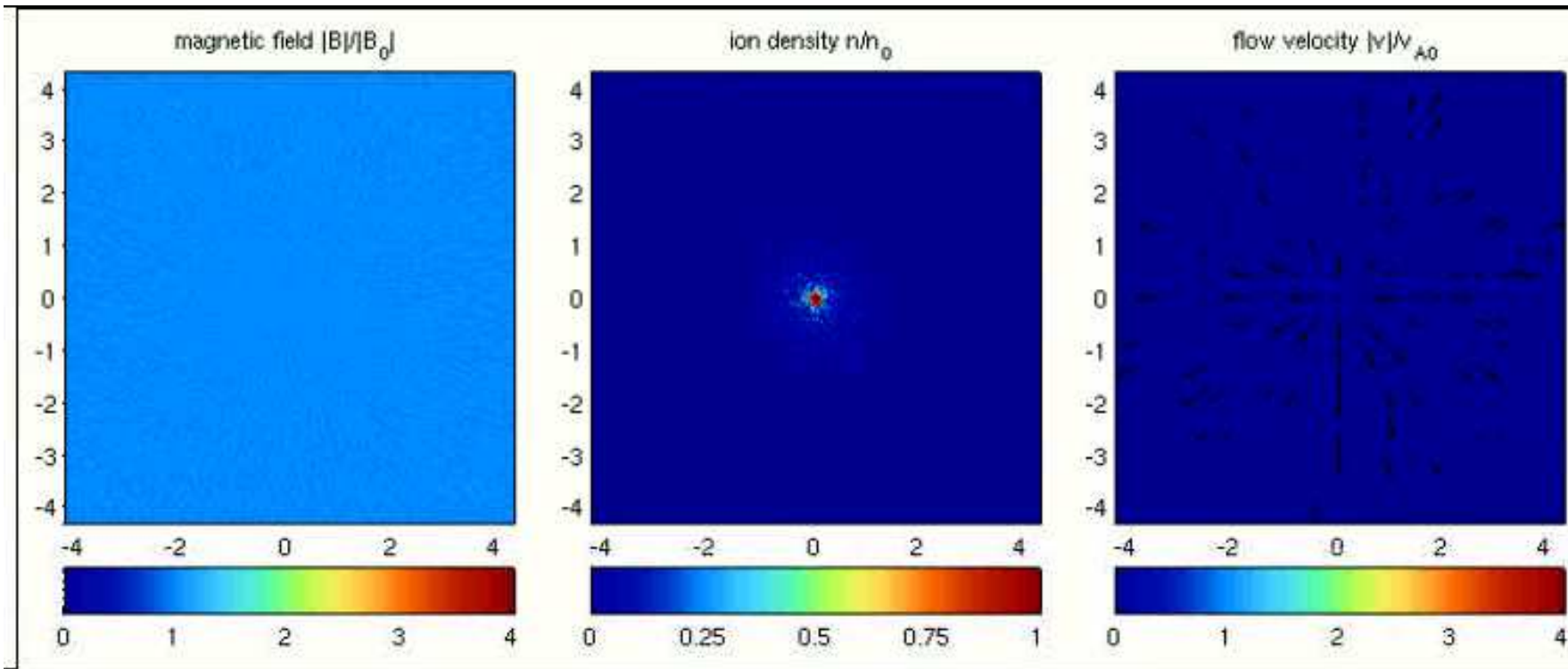
$$M_{A0} = 10$$

$$x_0 = 220 \text{km}$$



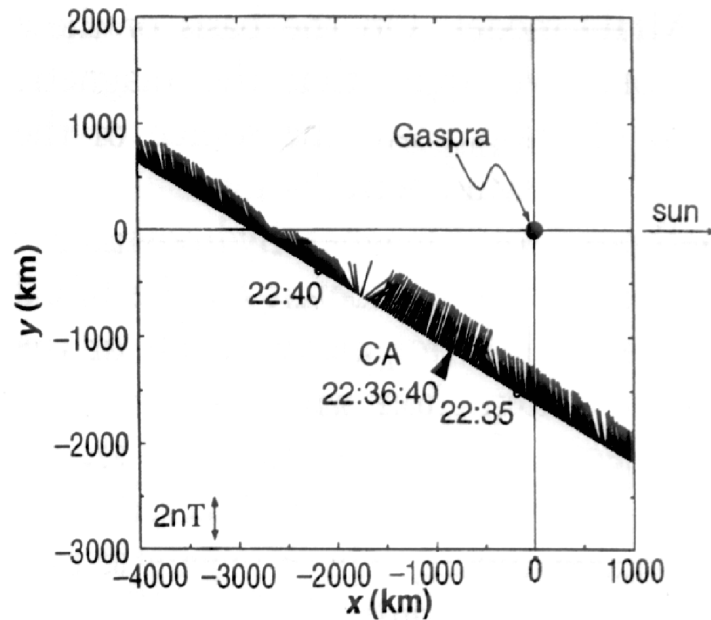


## *Evolution of CG at 2.5AU*



## *Simulation of a Magnetized Asteroid*

1991: *Galileo* flyby of asteroid *Gaspra*

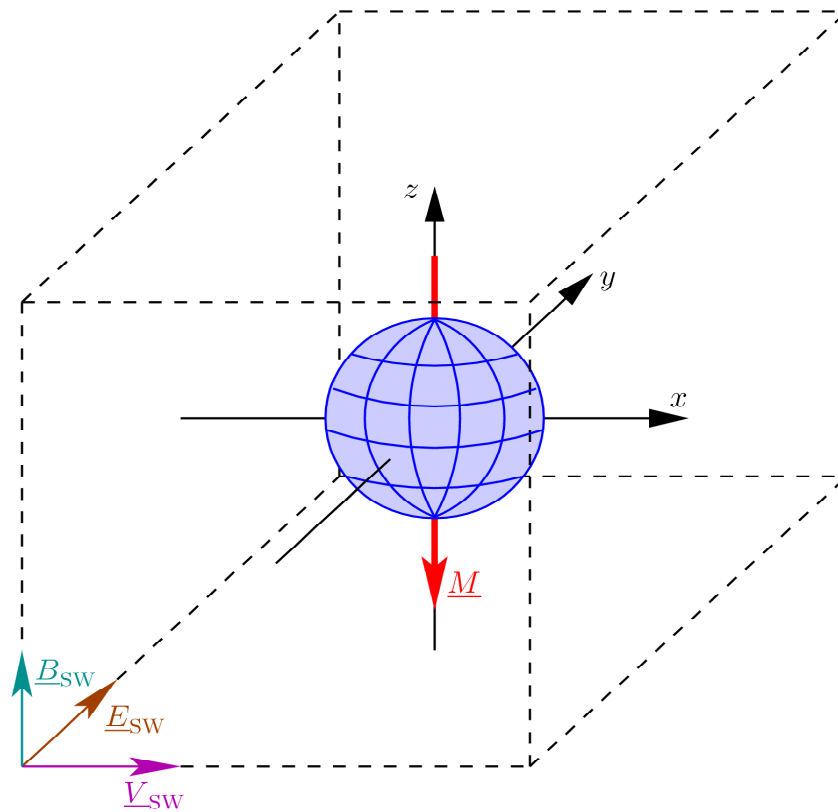


[ Kivelson et al, Science, 1993 ]

2008: *Rosetta* flyby of asteroid 2867 *Steins* (scheduled)

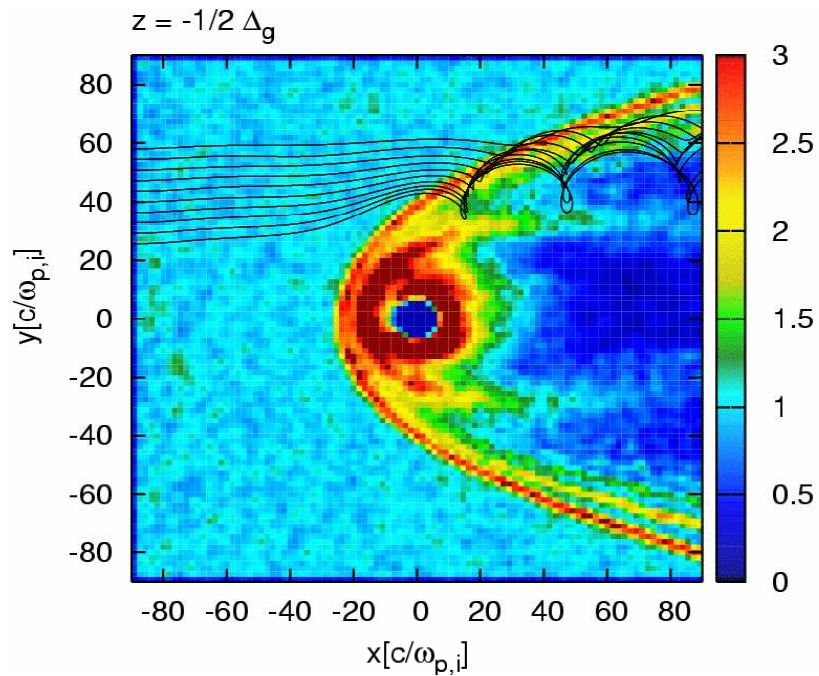
2010: *Rosetta* flyby of asteroid 21 *Lutetia* (scheduled)

## *Simulation Frame*

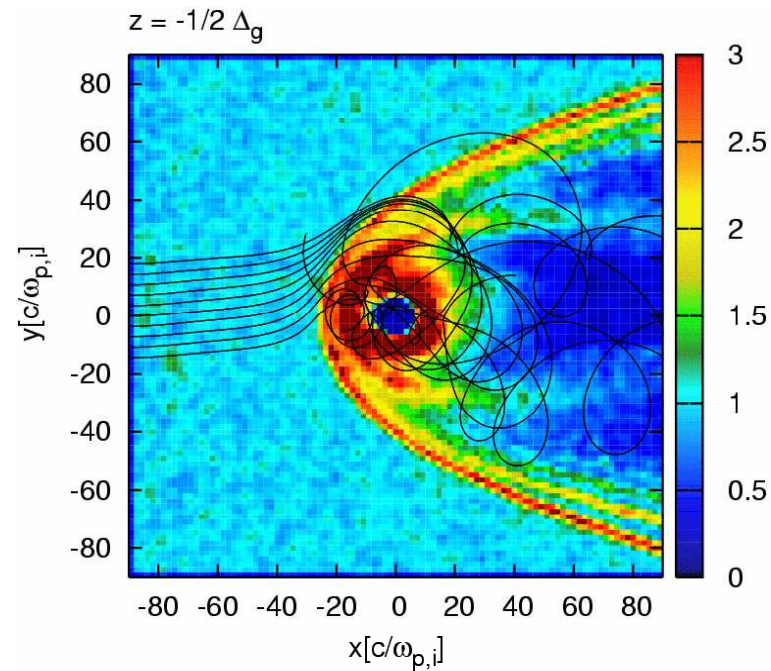


# Magnetized Asteroid

Substructure of the boundary layer



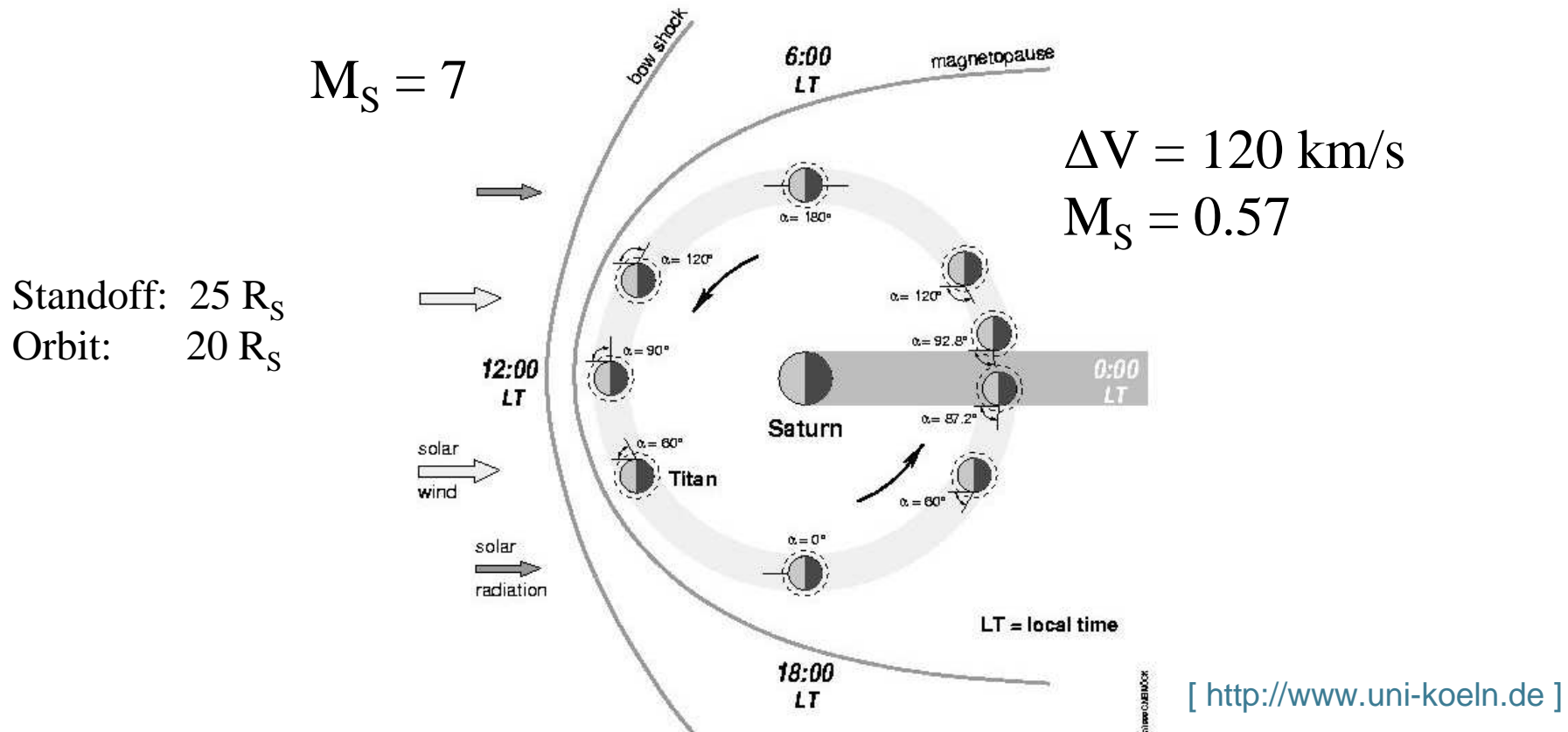
Ring of trapped particles around the obstacle



$$\underline{M} \parallel -\underline{e}_z, \quad \& \quad \underline{B}_{SW} \parallel \underline{e}_z$$

[Simon et al, DPG, 2005]

# Titan at Saturn

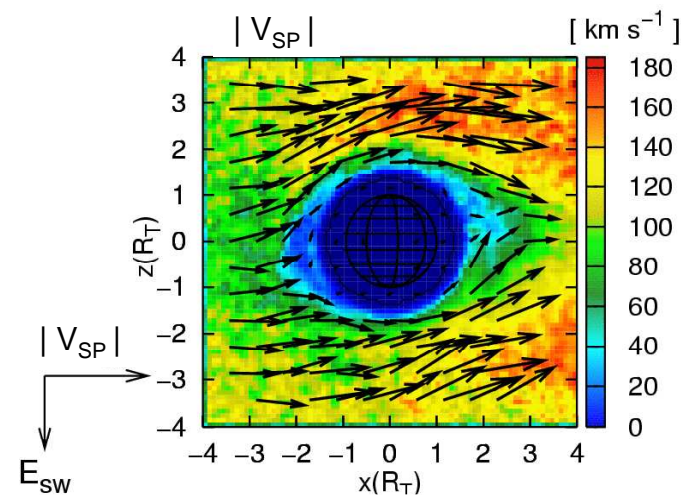
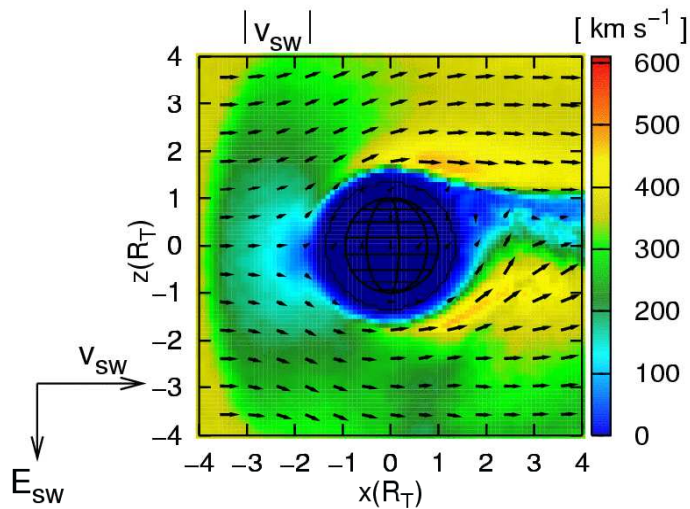
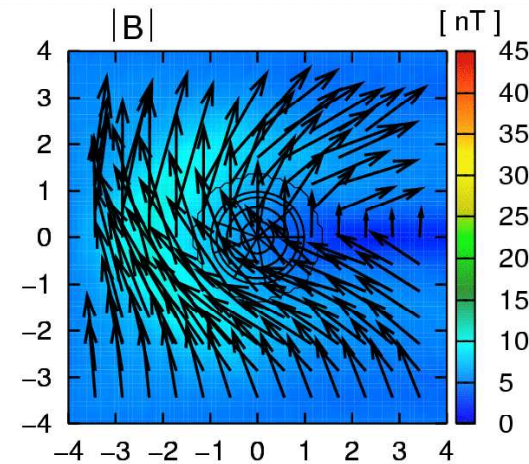
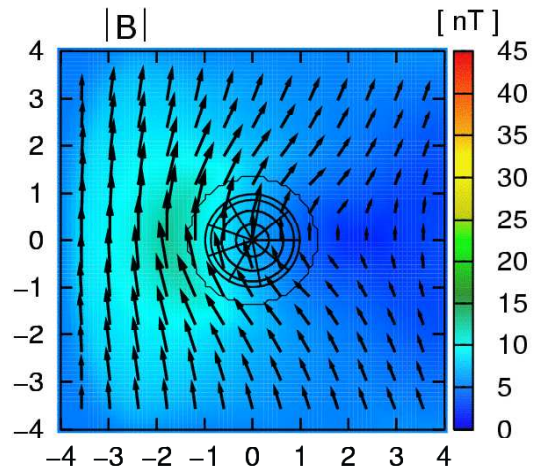




*Titan in SW ( $M_S = 7$ )*

*Titan in MS ( $M_S = 0.57$ )*

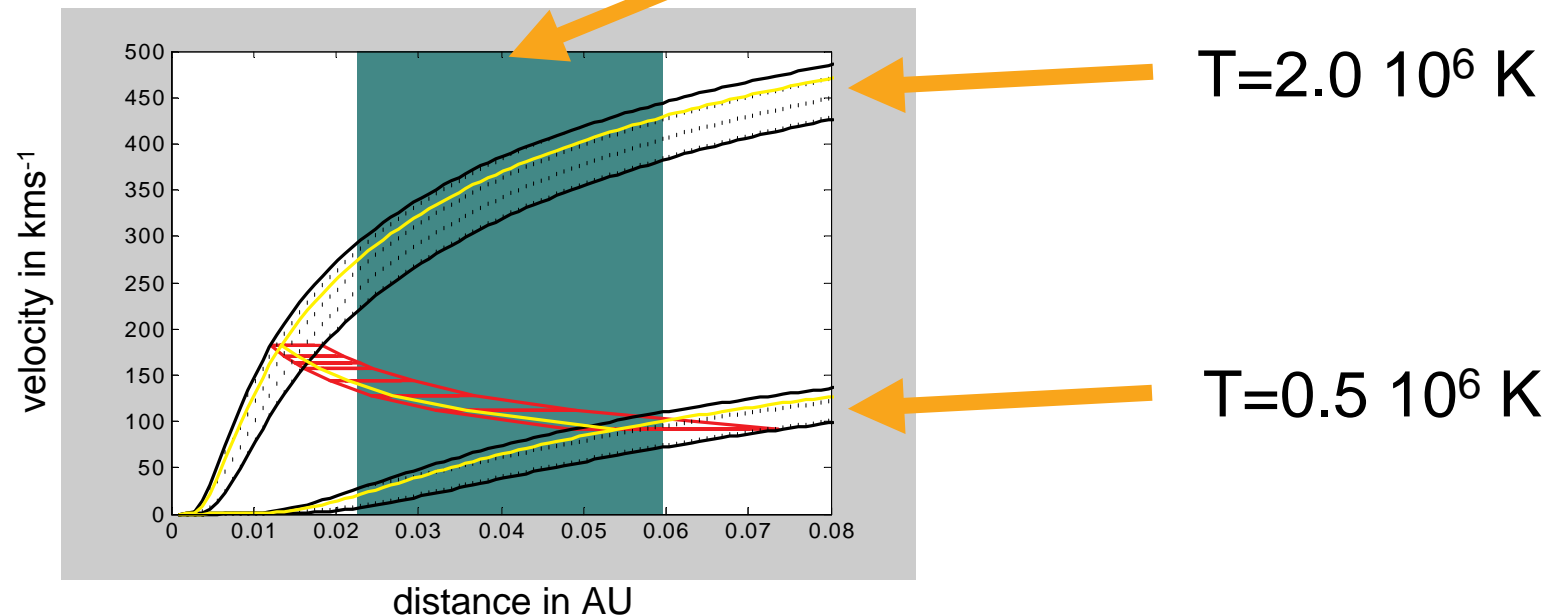
$$M_A = 1.9$$



## *Extrasolar Planet in Stellar Wind*

Stellar Wind Model:  
[Weber&Davis, ApJ, 1967]

Planetary orbits



Velocities much lower with respect to 1 AU  
Planets may be located within Alfvén radius

[Preusse et al, A&A, 2005]  
[Lipatov et al, PSS, 2005]

## *Summary*

- Weak obstacles:  $d \lesssim r_g$
- Hybrid code is appropriate technique
- Successful application to Mars, CG, Titan, asteroids
- Mars: BS, ICB/MPB reproduced and interpreted
- CG: „classical“ boundaries emerge and separate at about 2.8AU, pronounced ion kinetic behaviour, distribution functions strongly non-thermal
- Titan: subsonic flow in MS, Mars-like in SW
- Asteroid: „quasi-magnetospheric“ structures
- Exoplanets: located in Alfvén radius