

# Spatially resolved vorticity in supergranulation with helioseismology (and LCT)

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Laurent Gizon (main adviser)

Aaron Birch

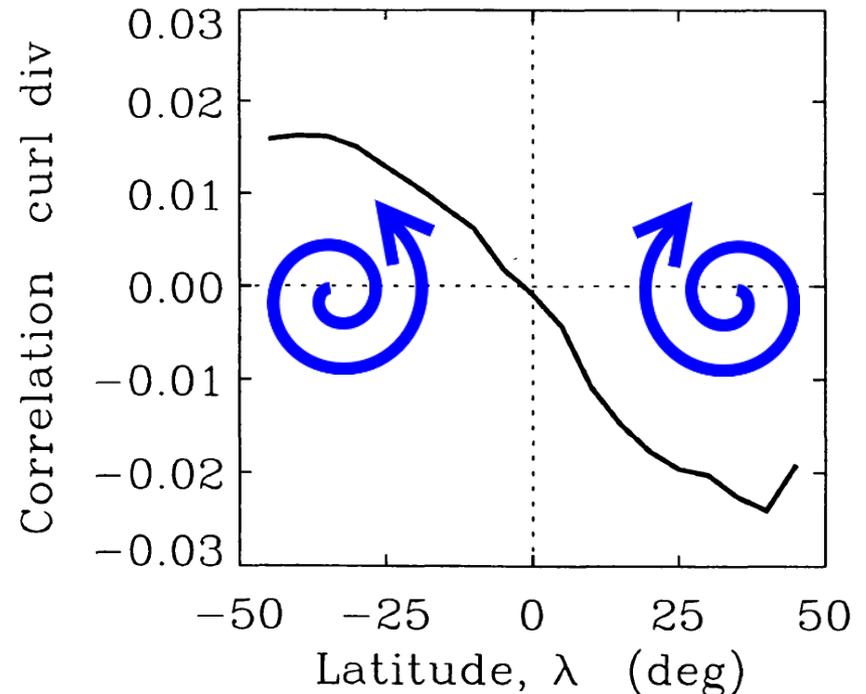


GEORG-AUGUST-UNIVERSITÄT  
GÖTTINGEN



# Motivation

- Known non-zero correlation  $\langle \text{div}_h \text{curl}_z \rangle$  in supergranular flows
- Probably due to Coriolis force acting on convective flows
- How does the circular flow component look in detail?  
→ Resolve spatially



Gizon & Duvall 2003

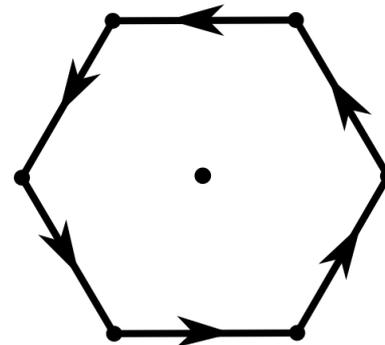
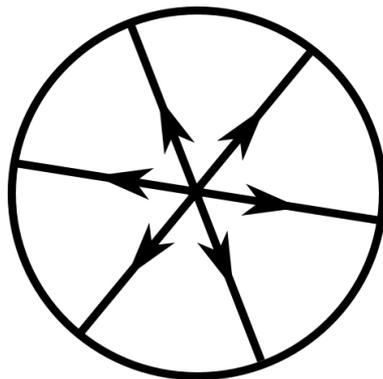
(using f modes in MDI Dopplergrams)

# Data and measurement geometries

- HMI Dopplergrams  $\sim 180 \times 180 \text{ Mm}^2$
- Tracked for 24h each (around central meridian)
- Remapped using Postel's projection
- Latitudes  $-60^\circ, -40^\circ, -20^\circ, 0^\circ, 20^\circ, 40^\circ, 60^\circ$
- 1 May – 28 August 2010
- Select modes: f and  $p_1$

Divergence  
-sensitive  
travel times

$\tau^{oi}$



Vorticity  
-sensitive  
travel times

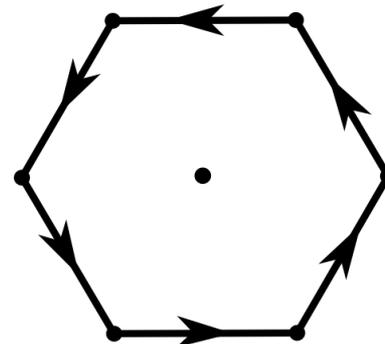
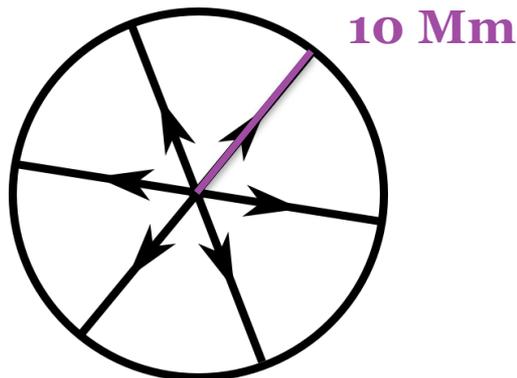
$\delta\tau^{\omega}$

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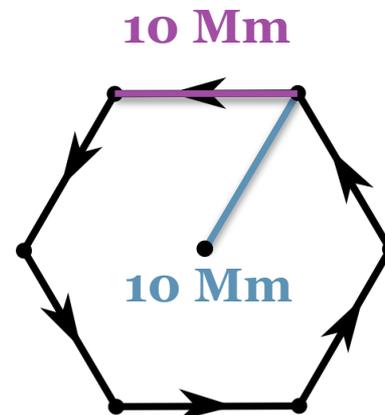
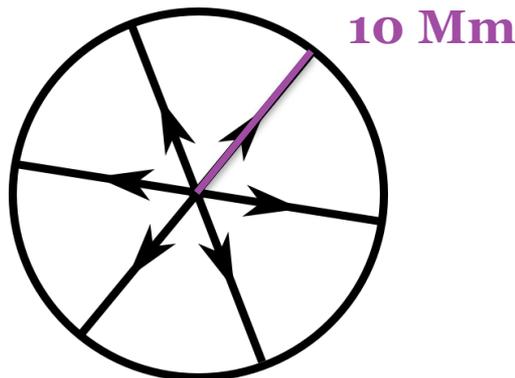
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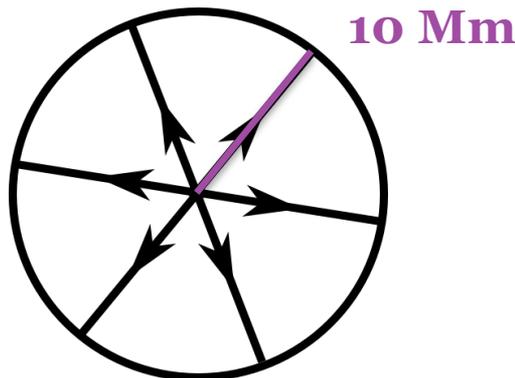
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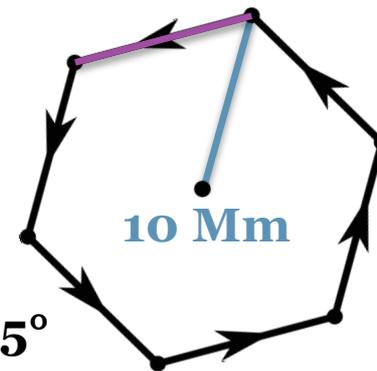
Divergence  
-sensitive  
travel times

$\tau^{oi}$



$\beta = 15^\circ$

10 Mm



Vorticity  
-sensitive  
travel times

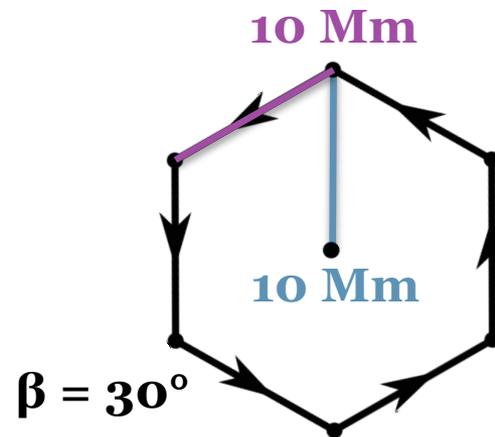
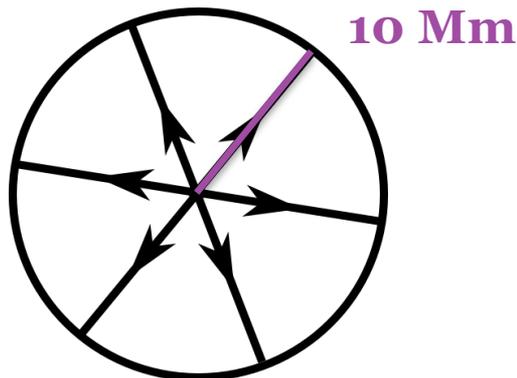
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Divergence  
-sensitive  
travel times

$$\tau^{oi}$$



Vorticity  
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travel times

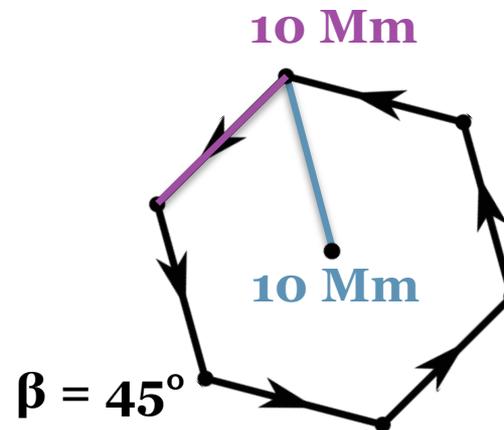
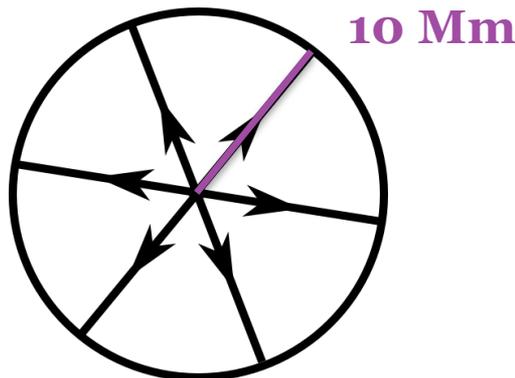
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Divergence  
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$$\tau^{oi}$$

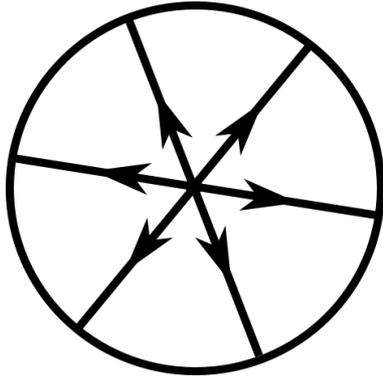


Vorticity  
-sensitive  
travel times

$$\delta\tau^{\cup}$$

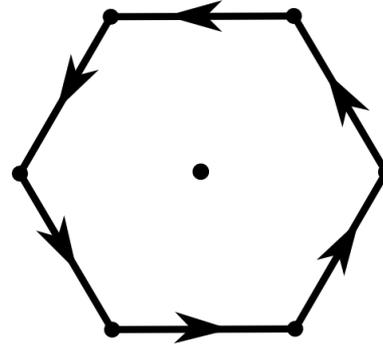
# Example travel-time maps

Divergence  
-sensitive  
travel times



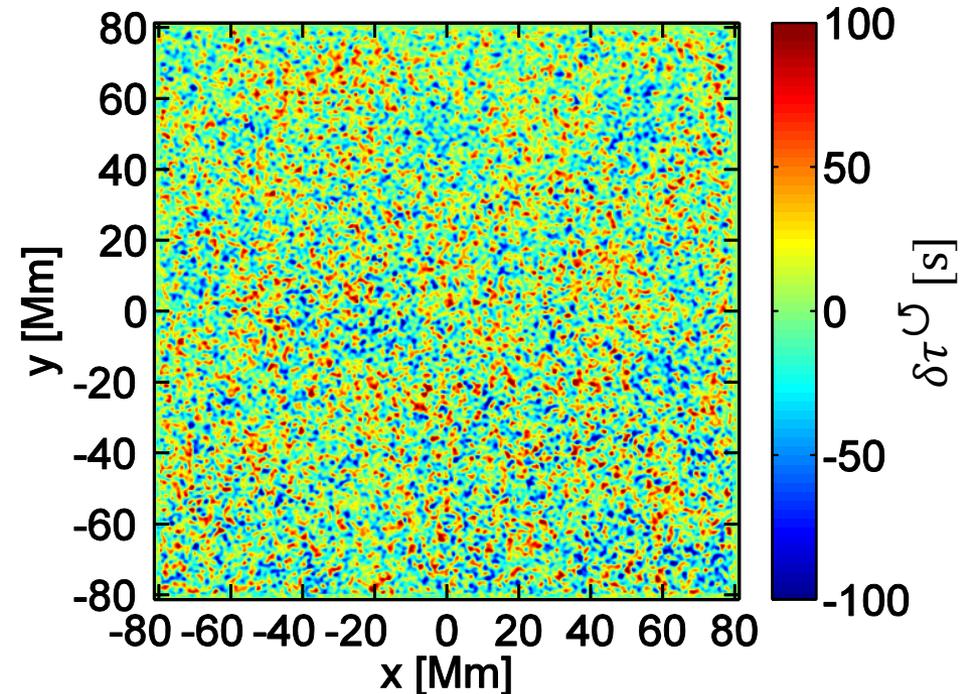
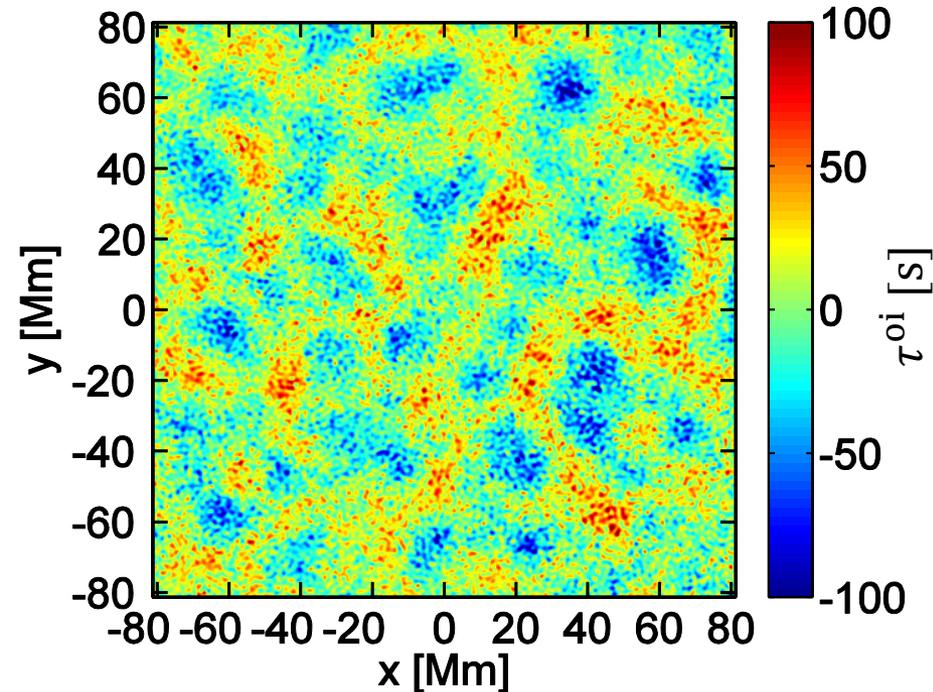
$$\tau^{oi}$$

40°  
f mode  
8h

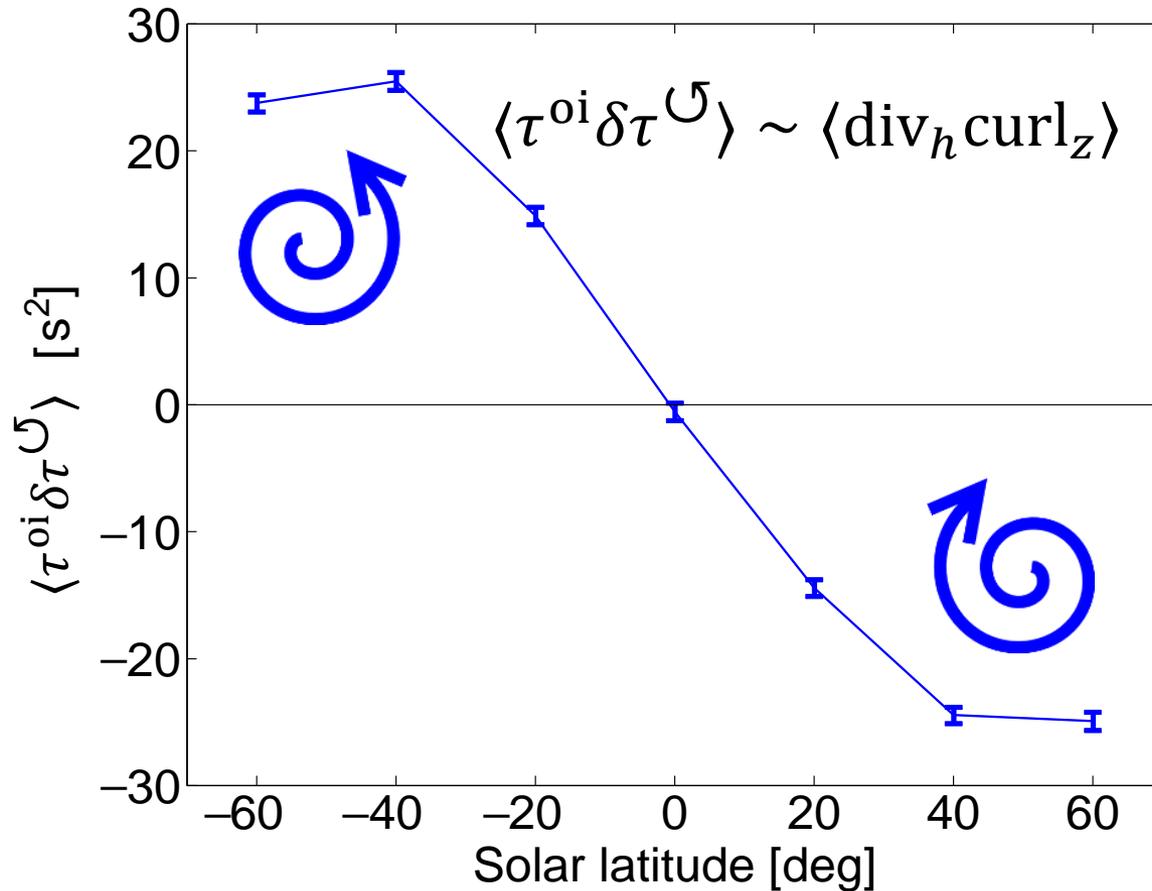


Vorticity  
-sensitive  
travel times

$$\delta\tau^{\zeta}$$

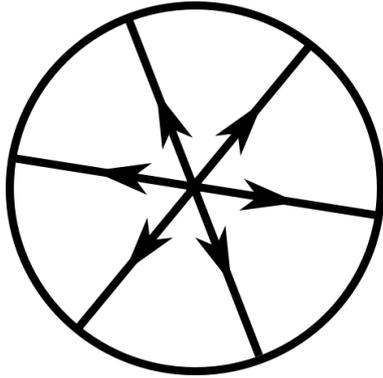


# $\langle \text{div}_h \text{curl}_z \rangle$ vs. latitude



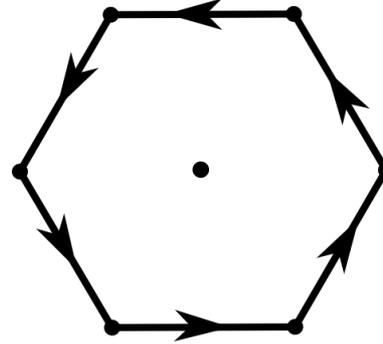
# Example travel-time maps

Divergence  
-sensitive  
travel times

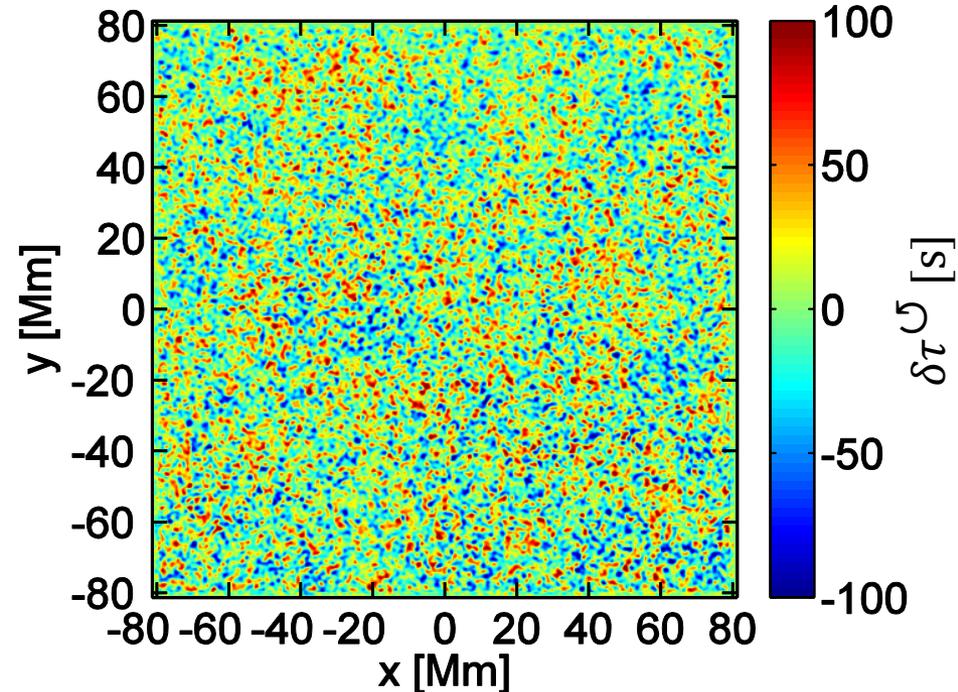
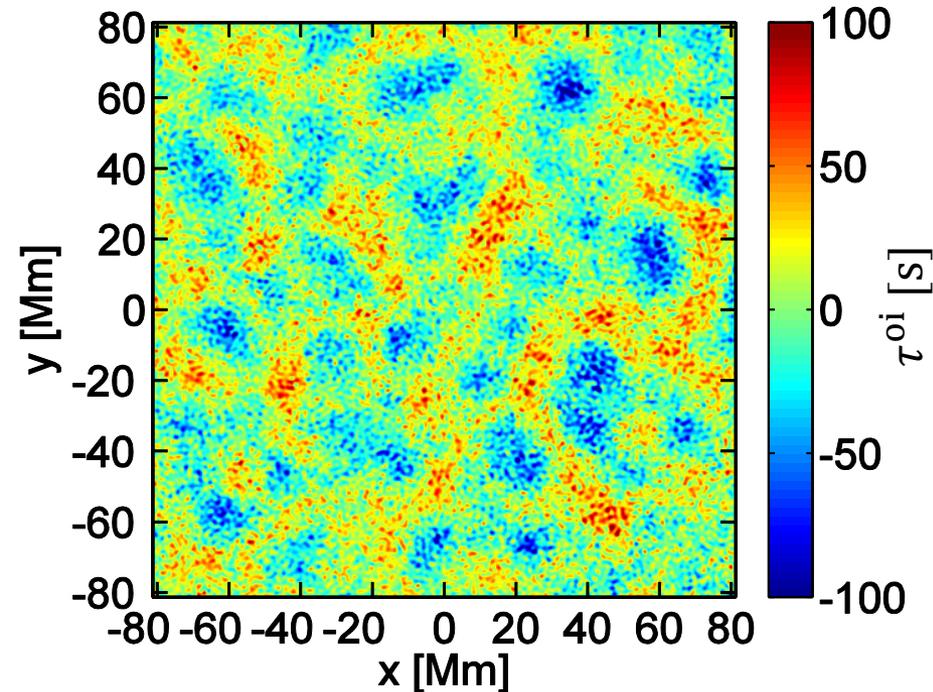


$$\tau^{oi}$$

Vorticity  
-sensitive  
travel times



$$\delta\tau^{\zeta}$$



# Example travel-time maps

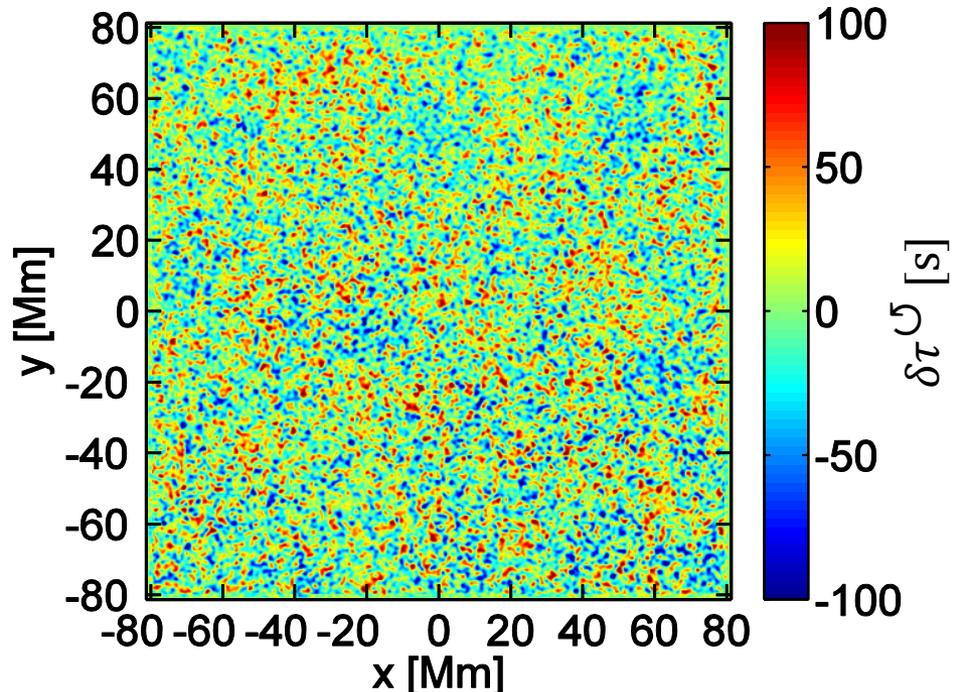
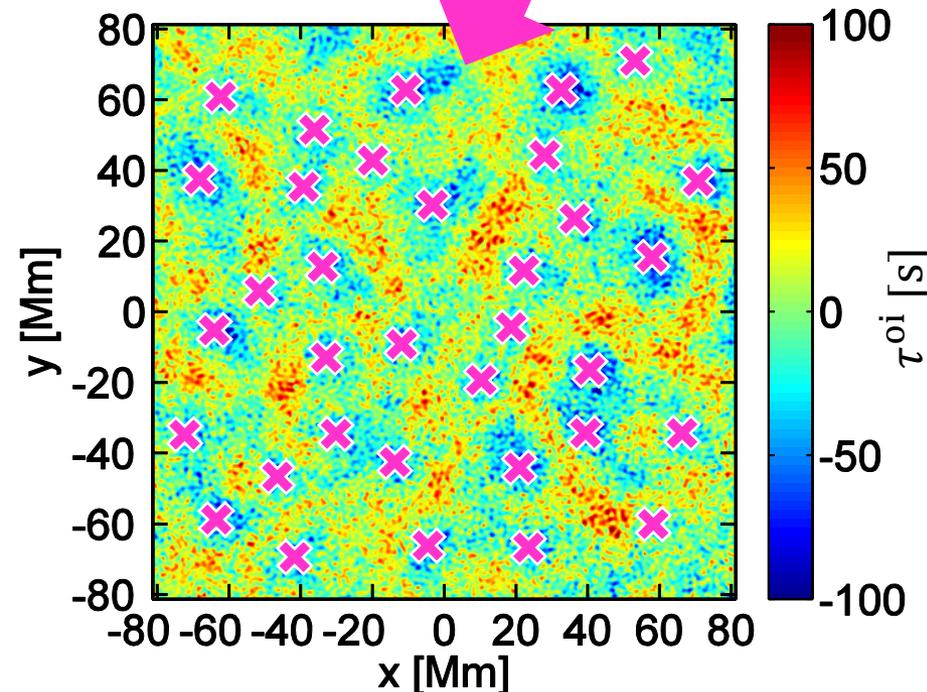
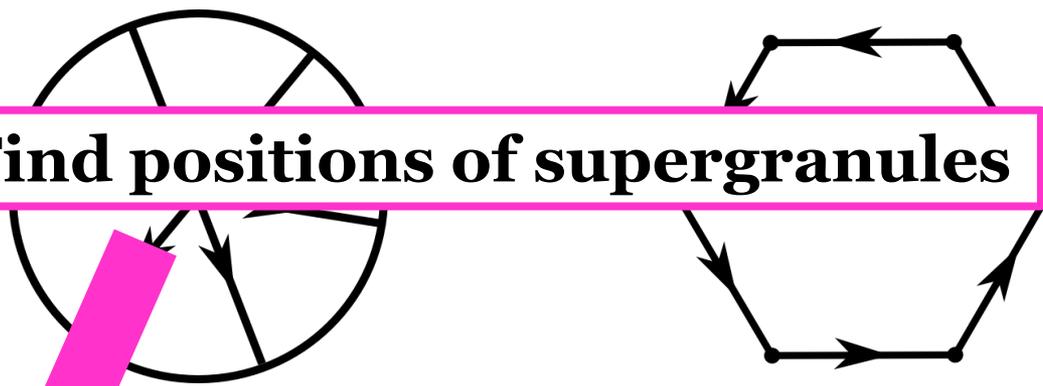
Divergence  
-sensitive  
travel times

$$\tau^{oi}$$

**Find positions of supergranules**

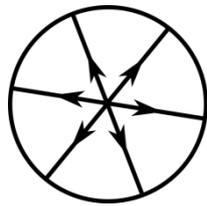
Vorticity  
-sensitive  
travel times

$$\delta\tau^{\zeta}$$

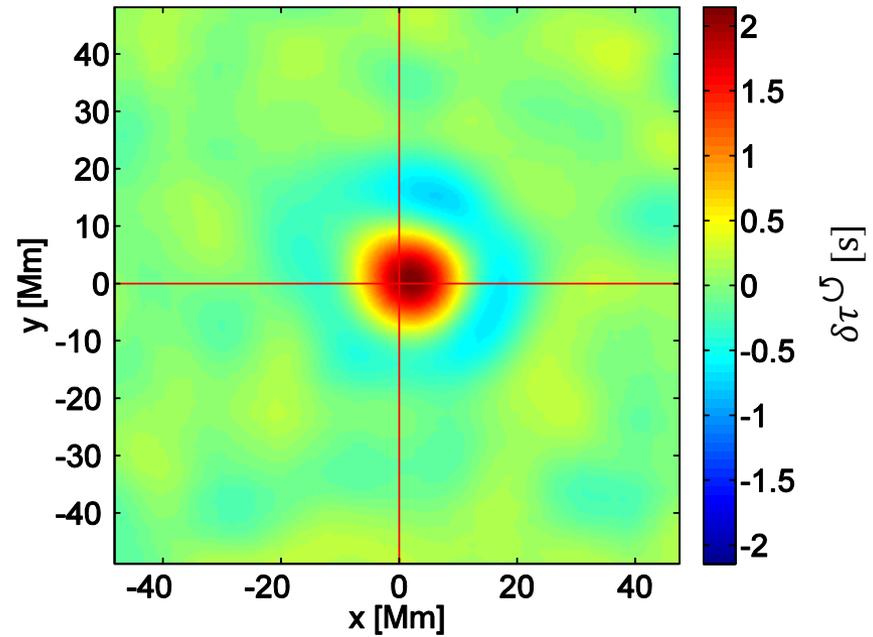
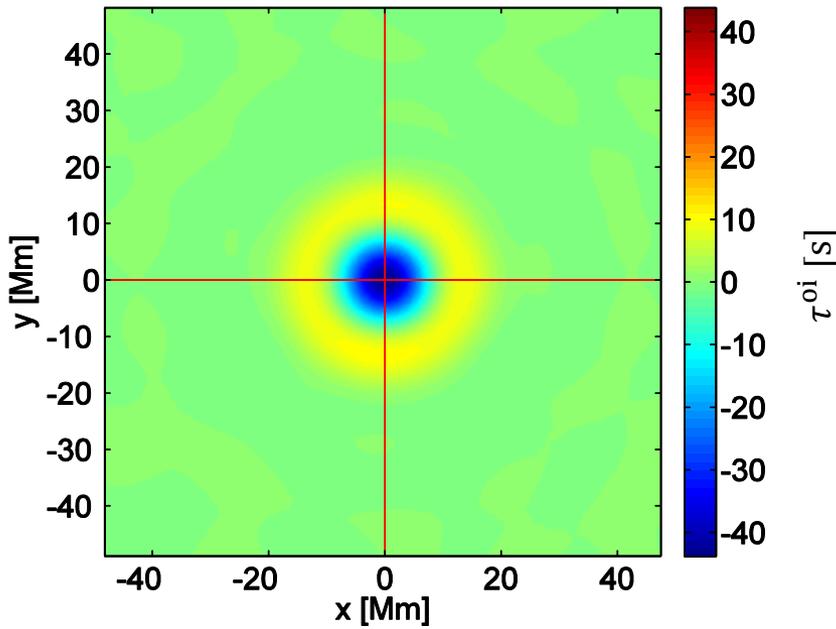
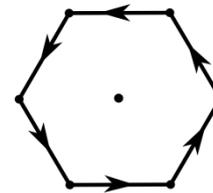


# The average supergranule

- Shift maps so supergranules are on top of each other
- Average over  $\sim 3,000$  supergranules (many maps)

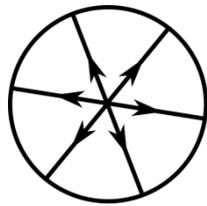


At  $40^\circ$  solar latitude

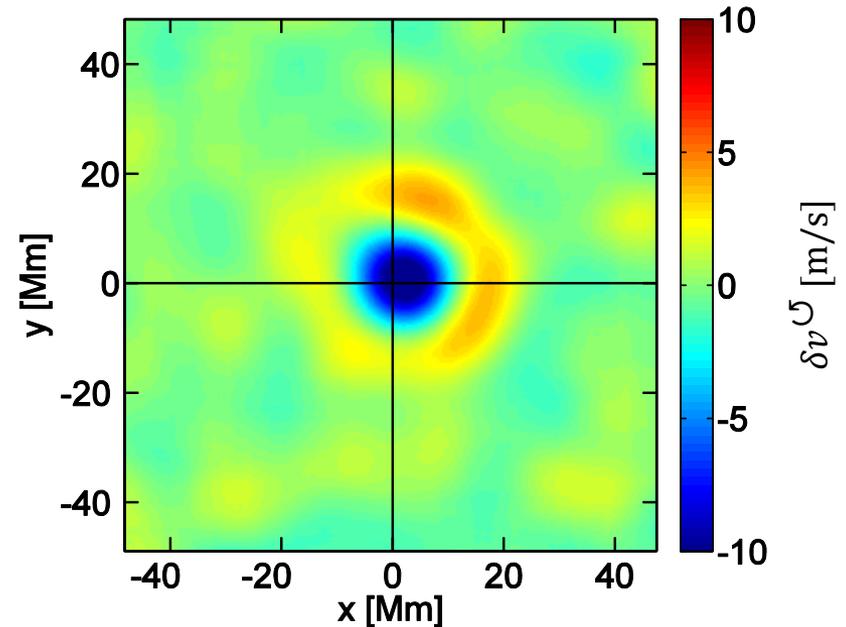
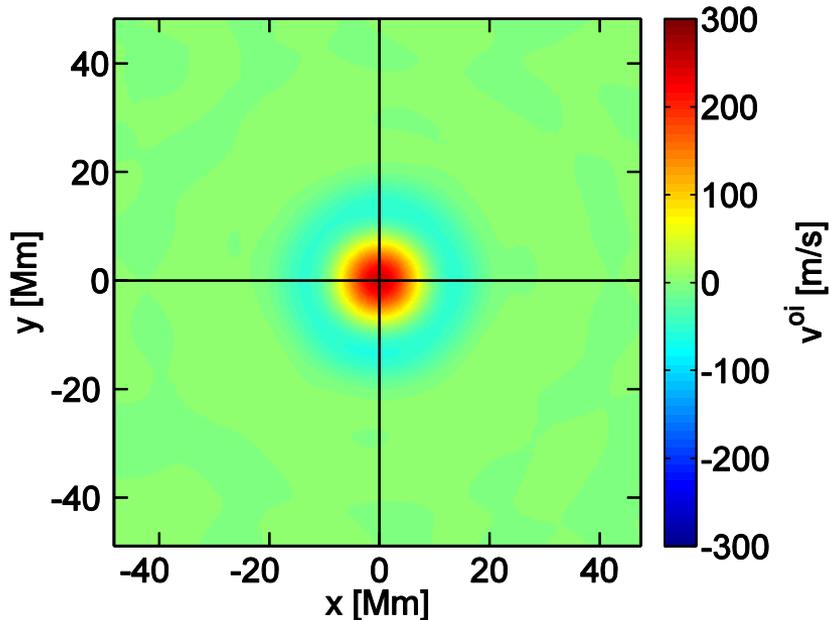
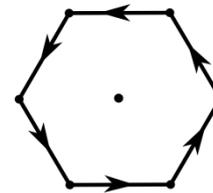


# The average supergranule

- Convert travel times into velocities (using a constant factor)

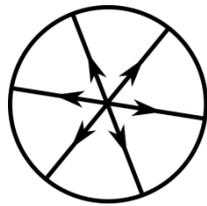


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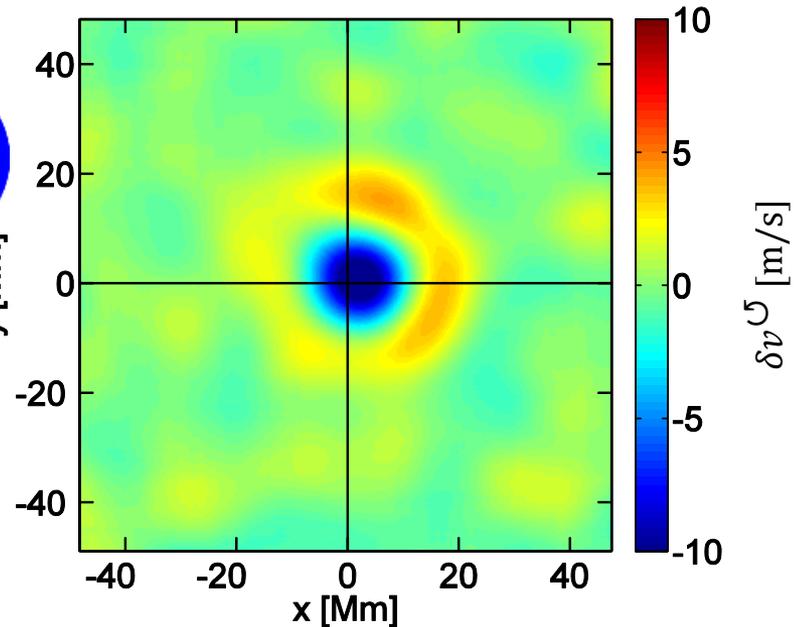
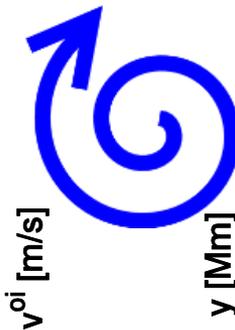
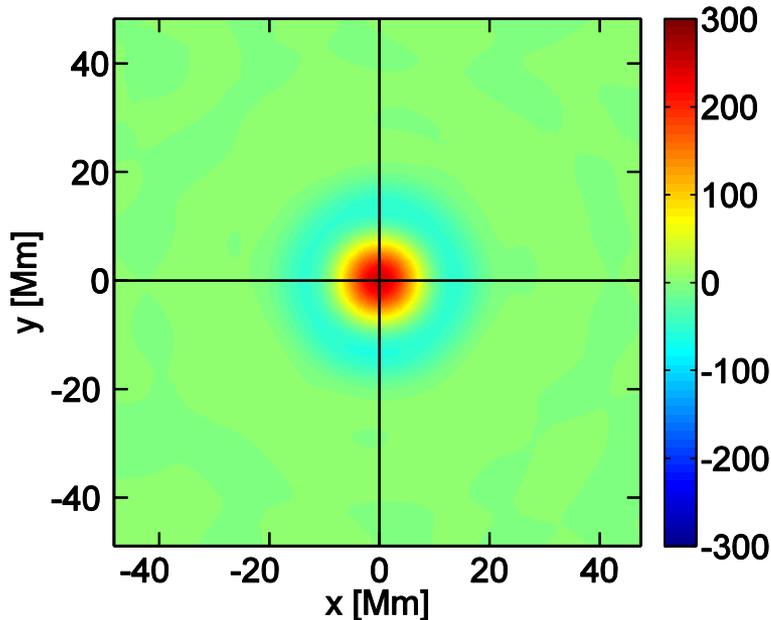
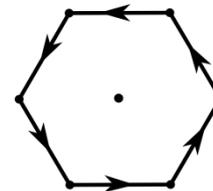


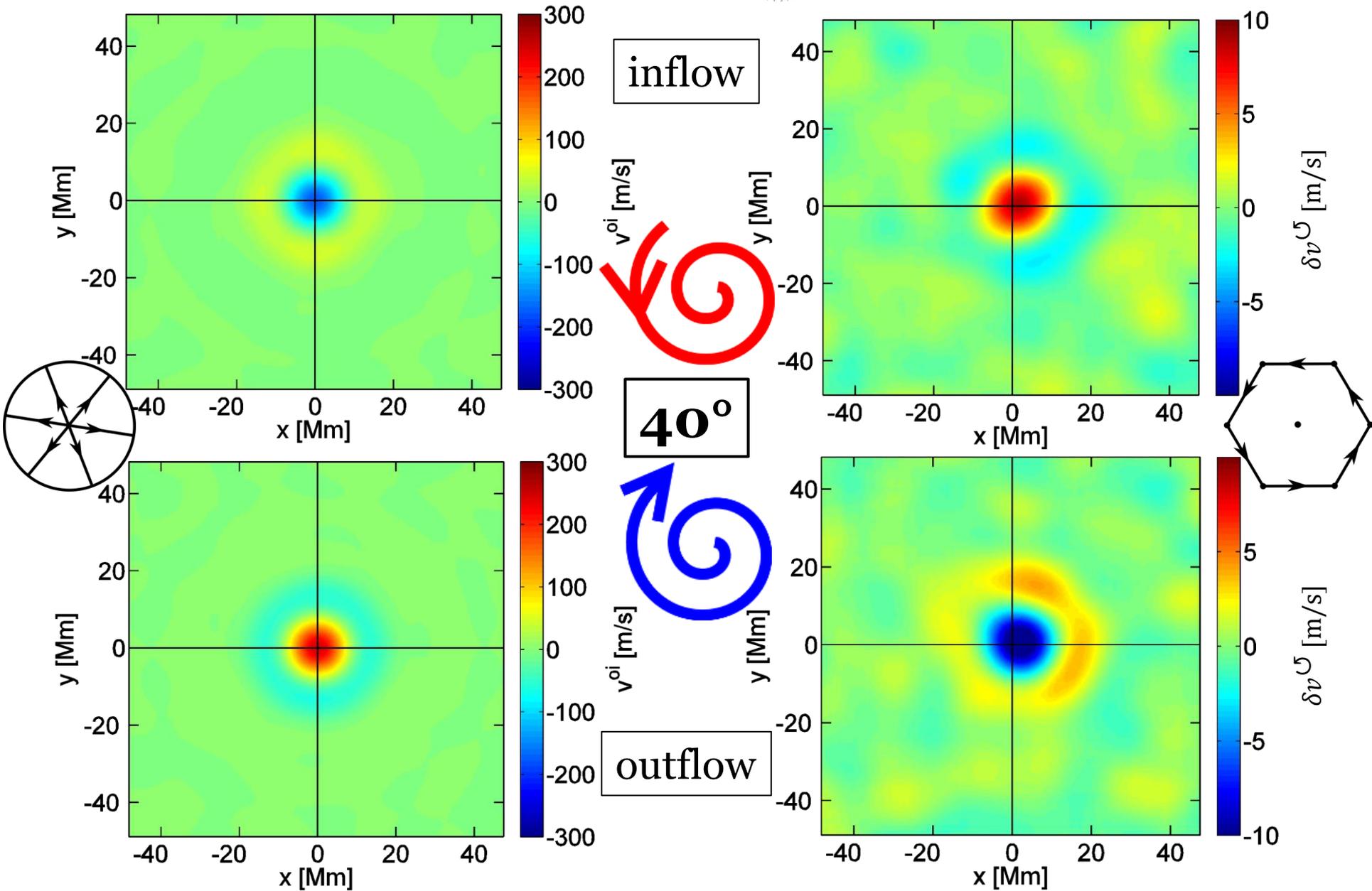
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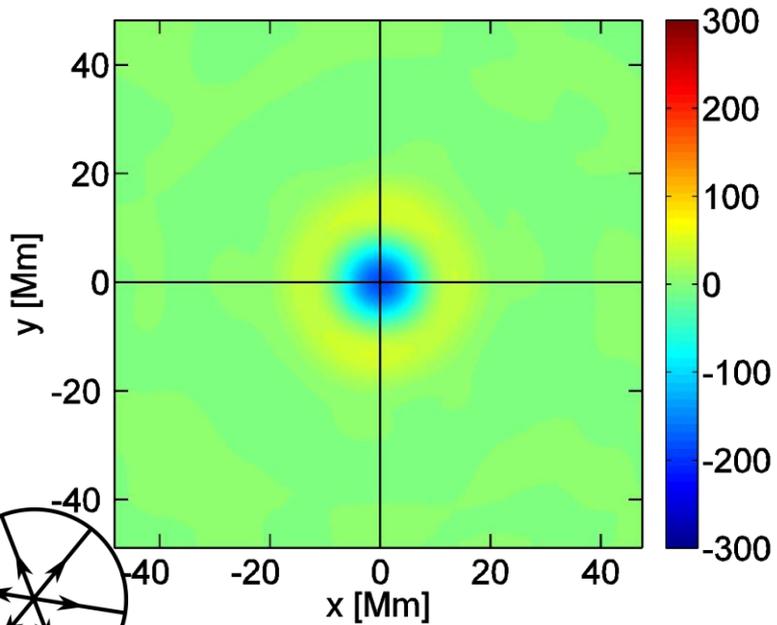
- Convert travel times into velocities (using a constant factor)



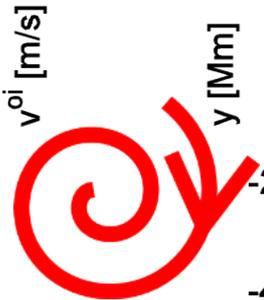
At  $40^\circ$  solar latitude



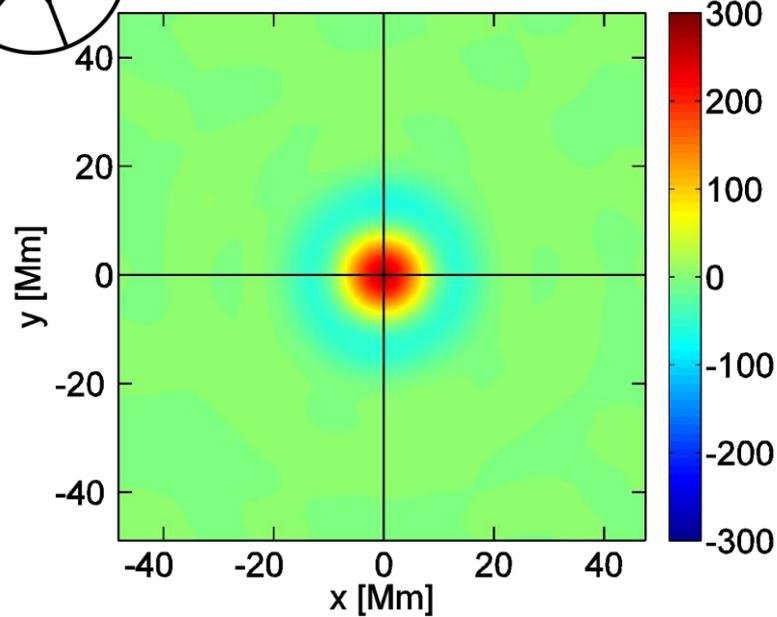
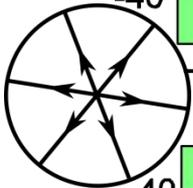
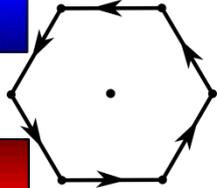
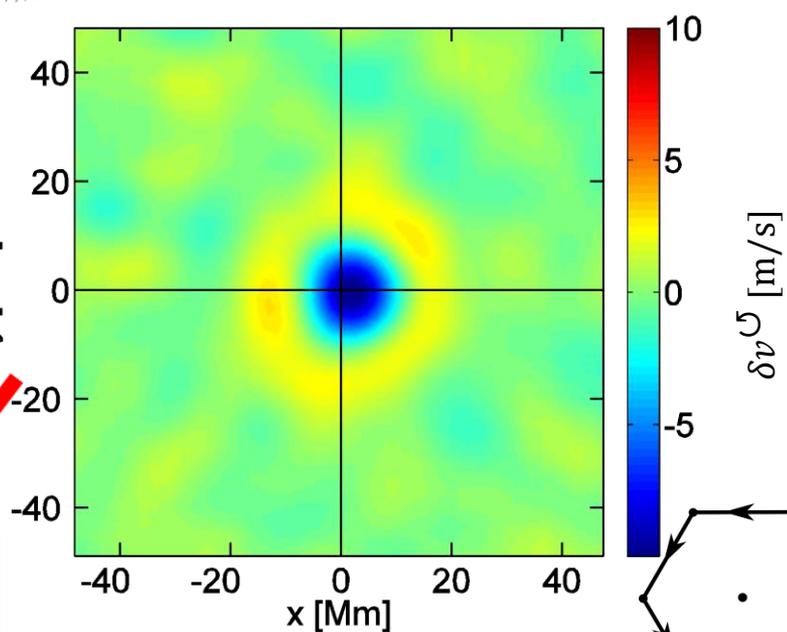




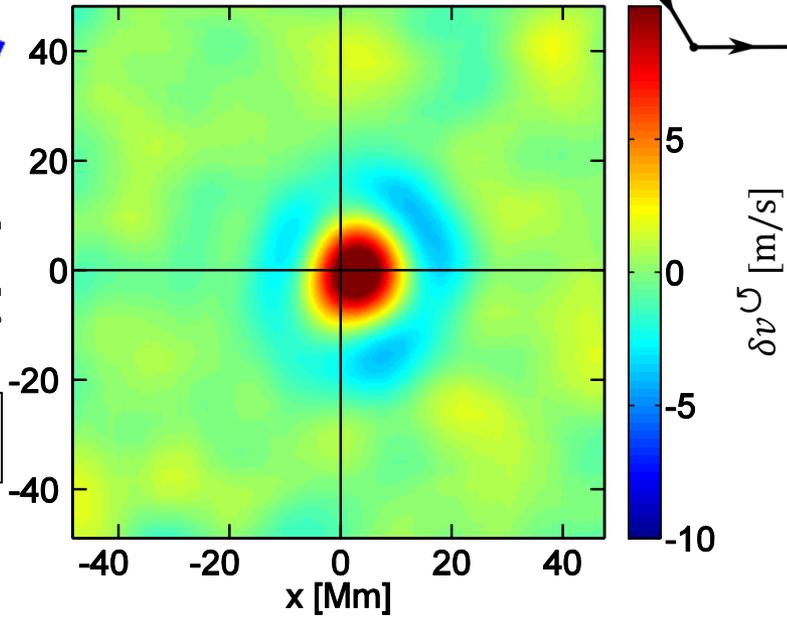
inflow

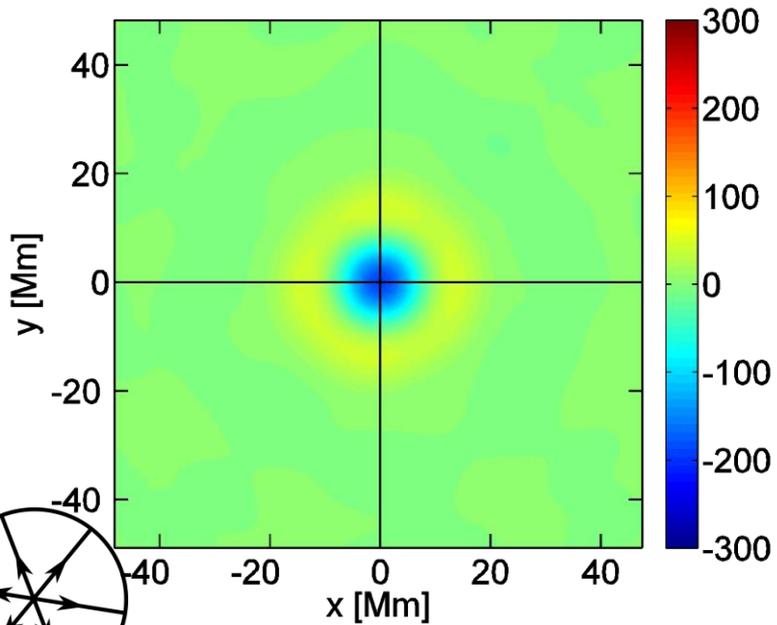


$-40^\circ$

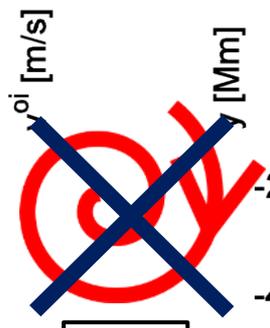


outflow

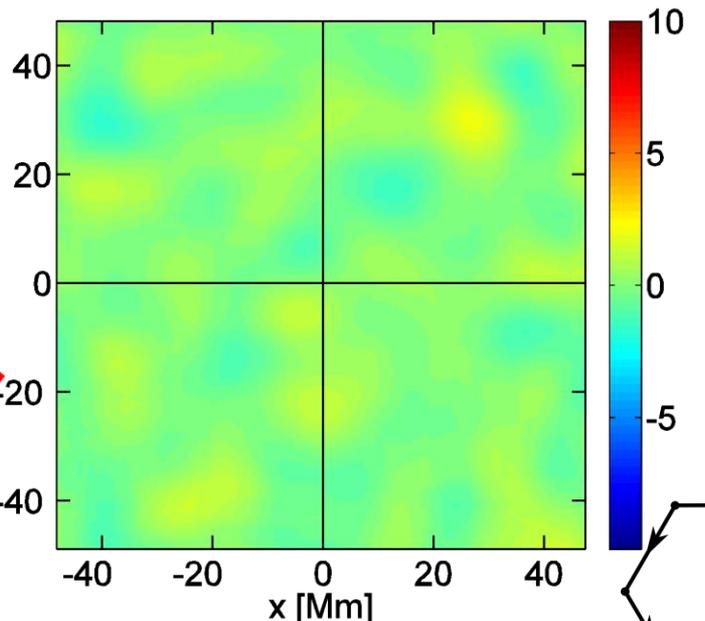




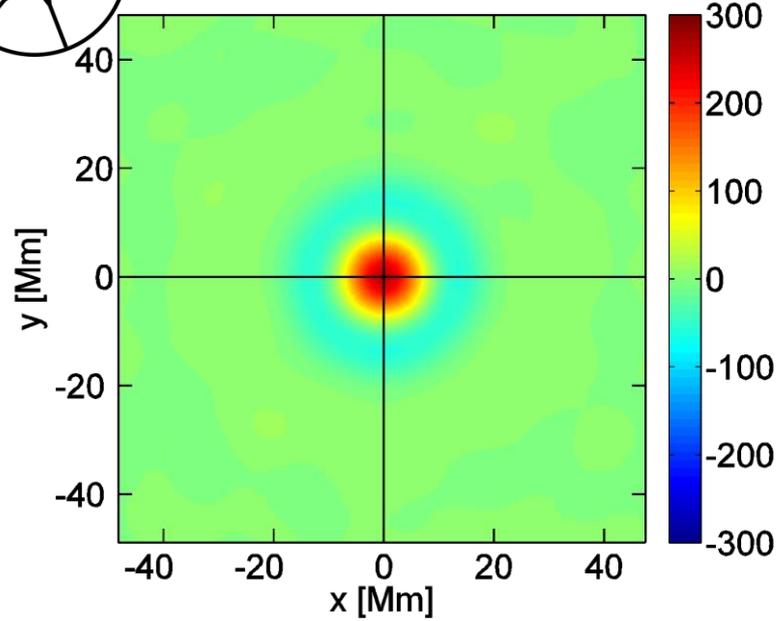
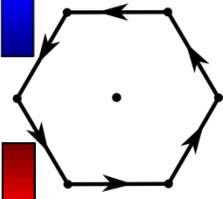
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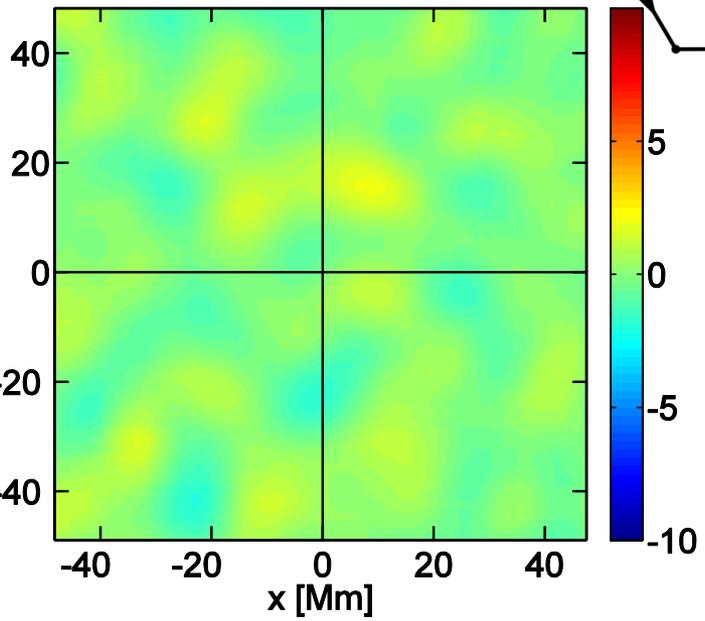
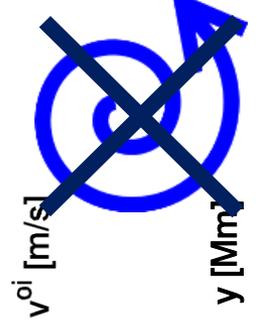
$0^\circ$



$\delta v^{oi}$  [m/s]



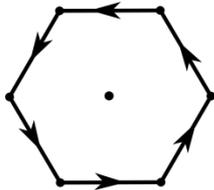
outflow



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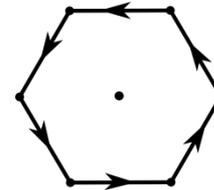


# Comparison: f mode / p<sub>1</sub> mode

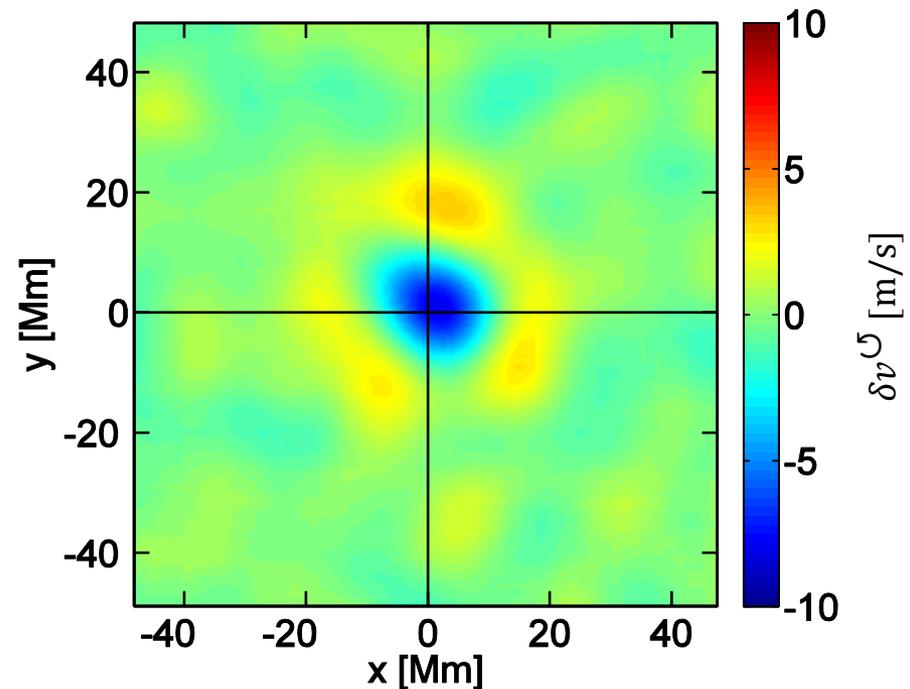
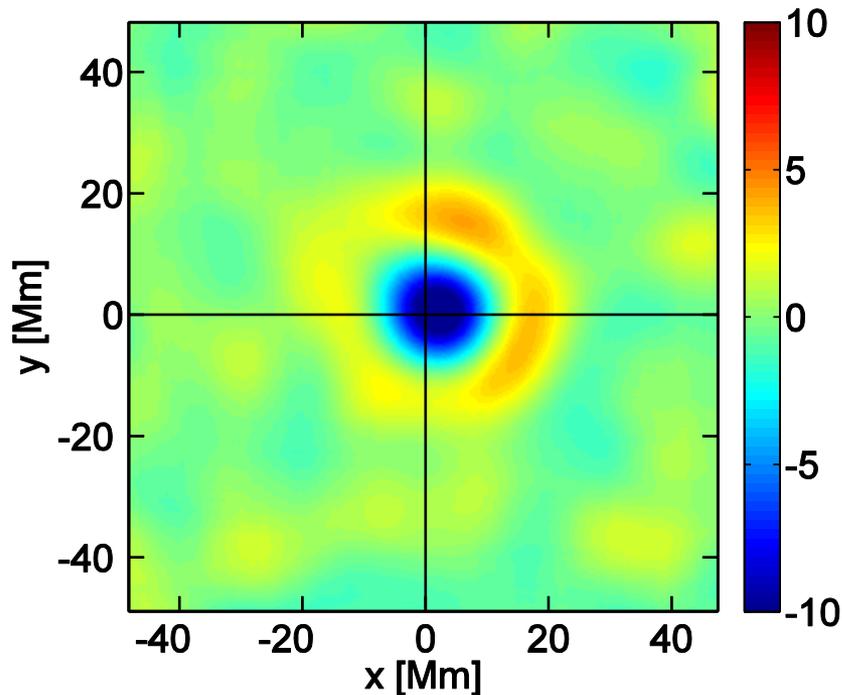


f mode

40°  
outflow

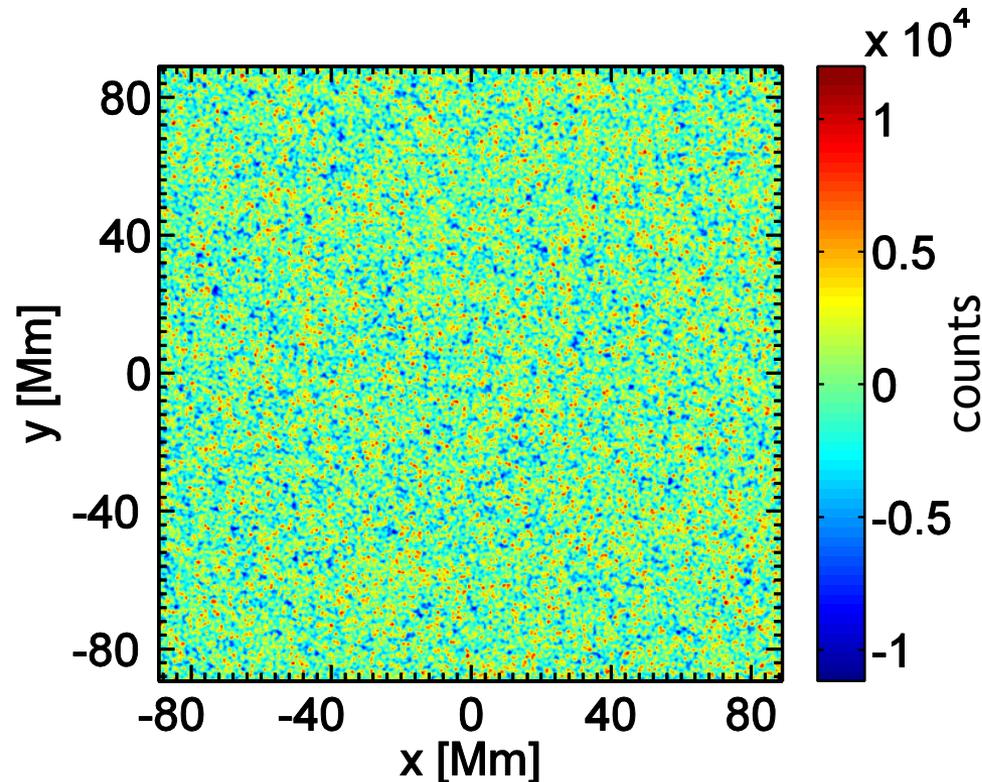


p<sub>1</sub> mode



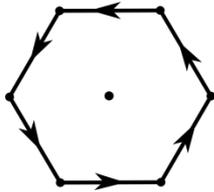
# Local correlation tracking (LCT)

HMI intensity image (mean subtracted)



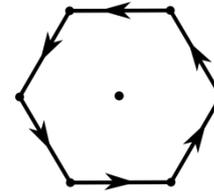
- Granules get advected by larger-scale flows
  - Use granules as tracers of supergranule motions
- Cross-correlate image parts at times  $t$  and  $t + \Delta t$ 
  - get shift  $\Delta x$
  - get velocity  $v = \frac{\Delta x}{\Delta t}$

# Comparison: Time-distance vs. LCT

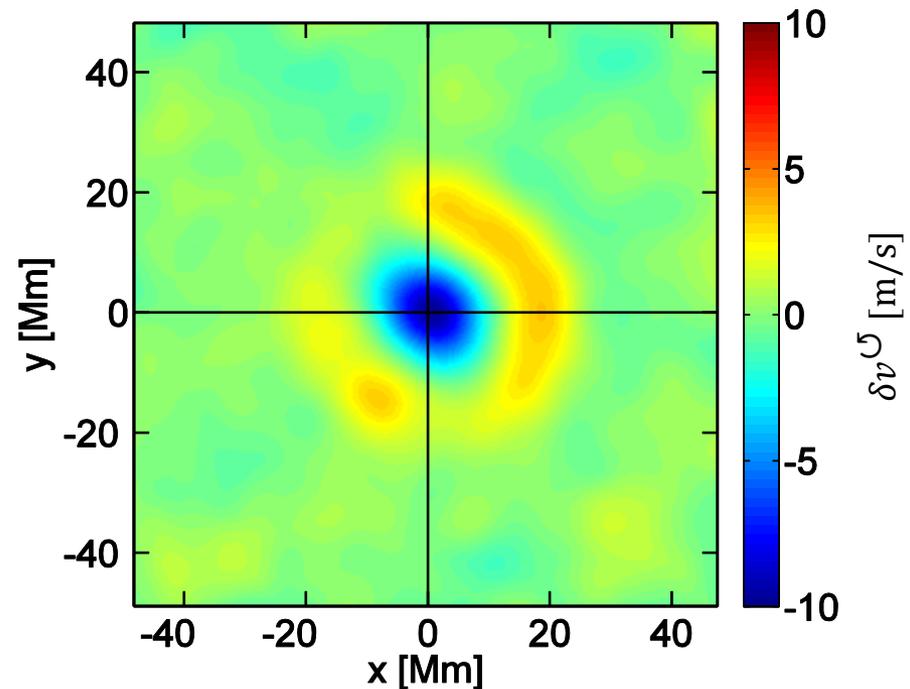
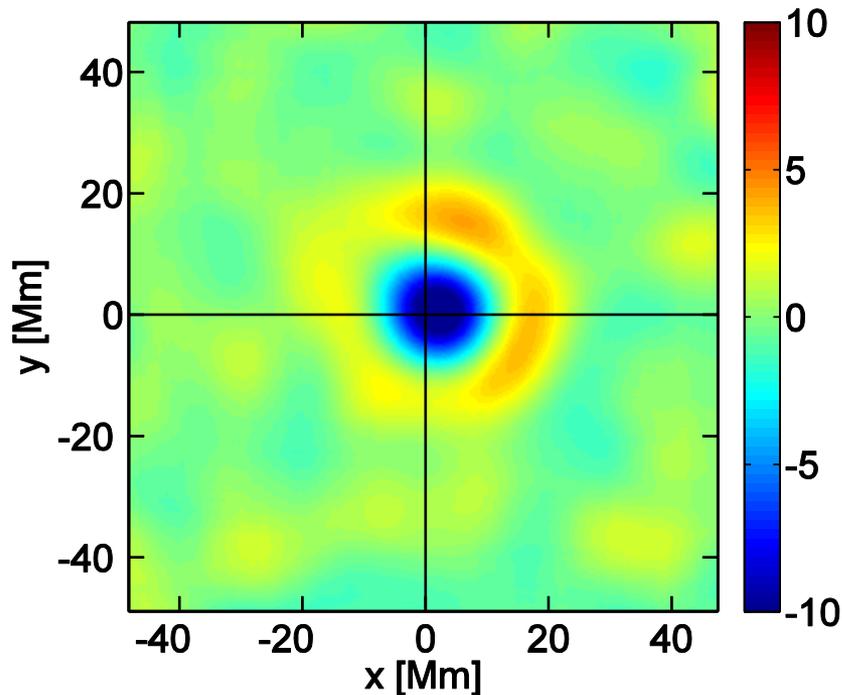


Time-distance (f mode)

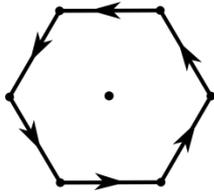
$40^\circ$   
outflow



LCT

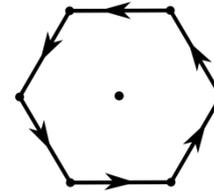


# Comparison: Time-distance vs. LCT

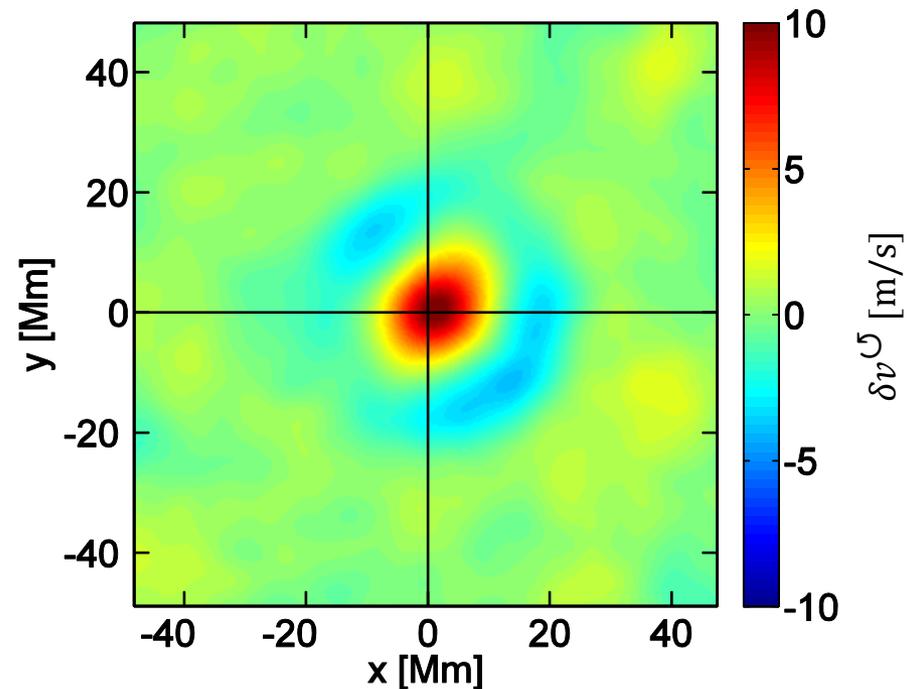
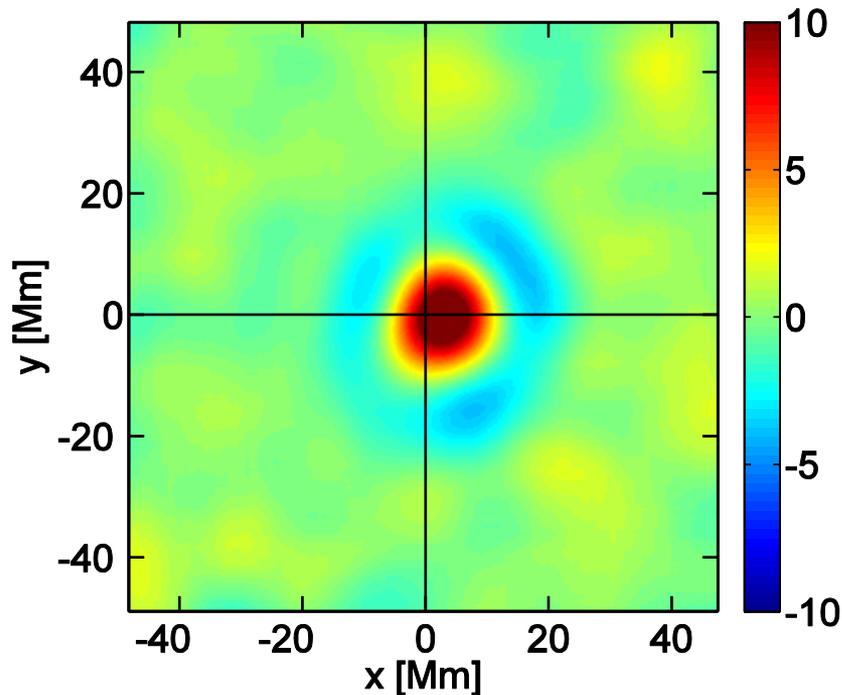


Time-distance (f mode)

$-40^\circ$   
outflow



LCT

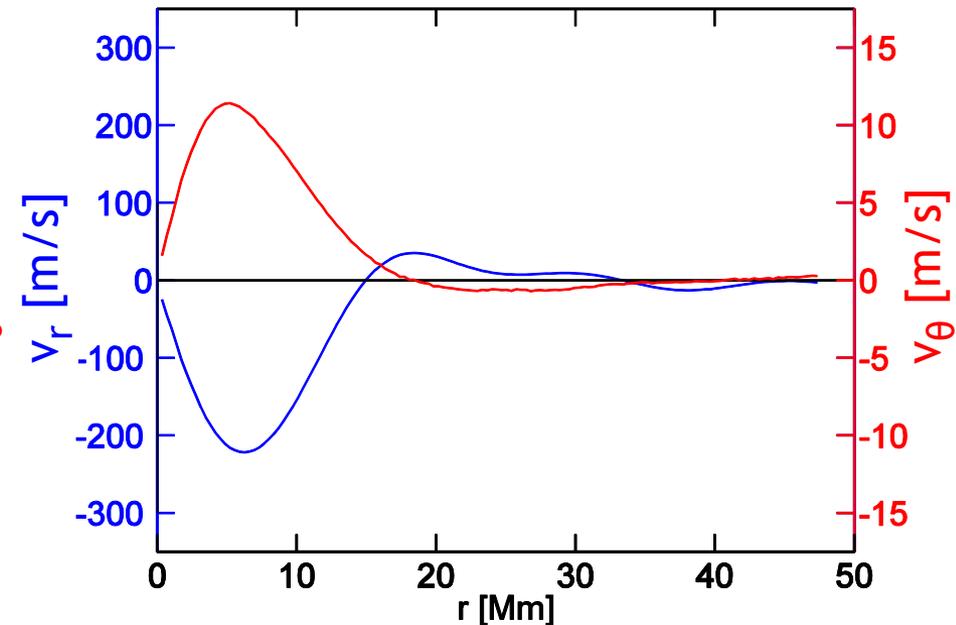
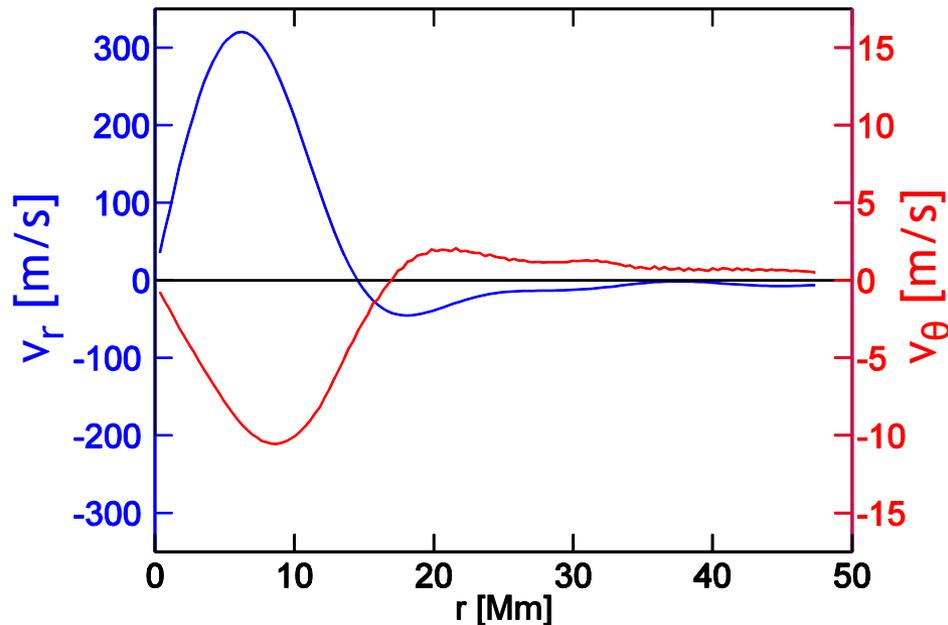


# LCT: avg. supergranule flow profiles

outflow

$40^\circ$

inflow

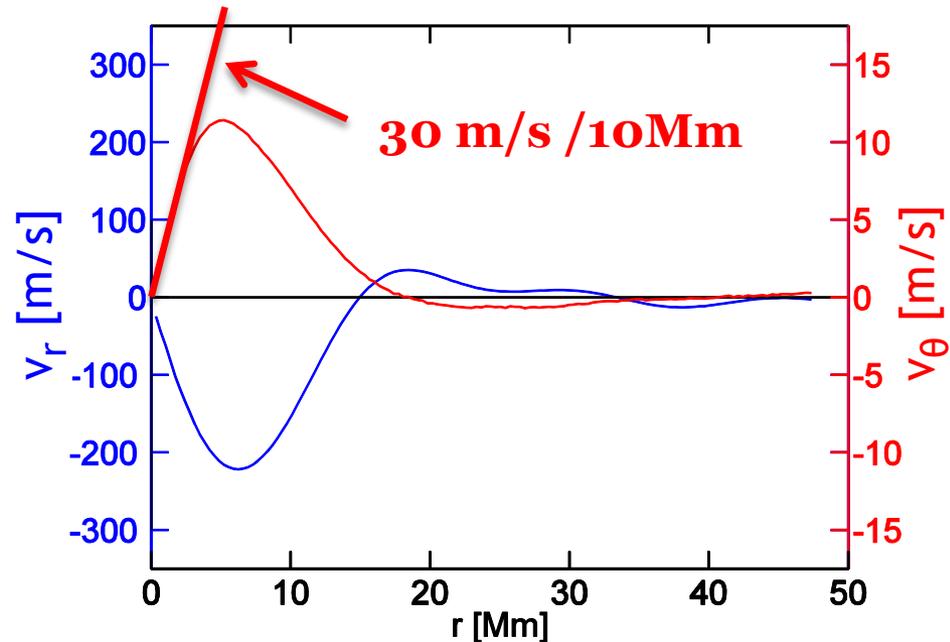
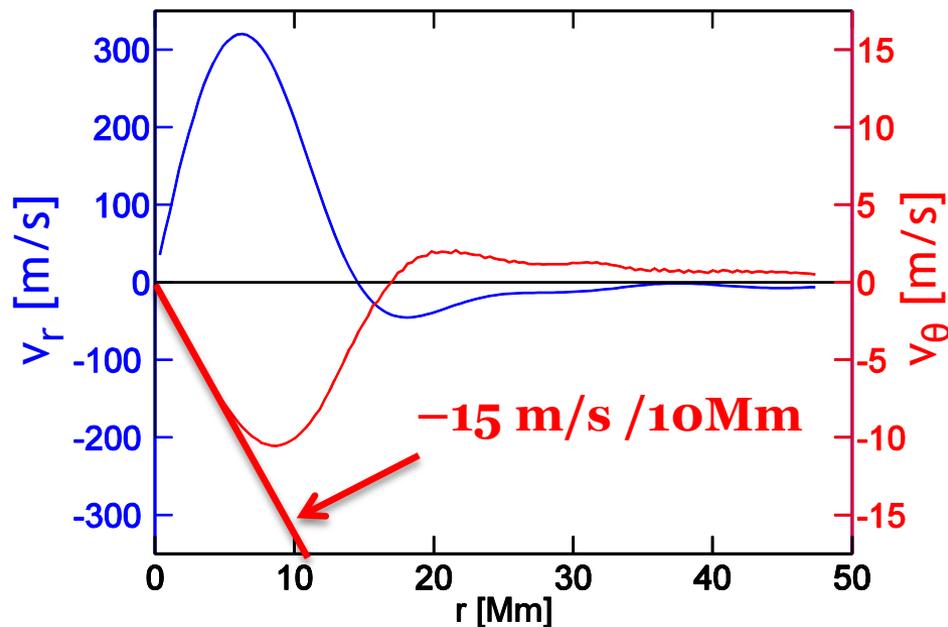


# LCT: avg. supergranule flow profiles

outflow

$40^\circ$

inflow

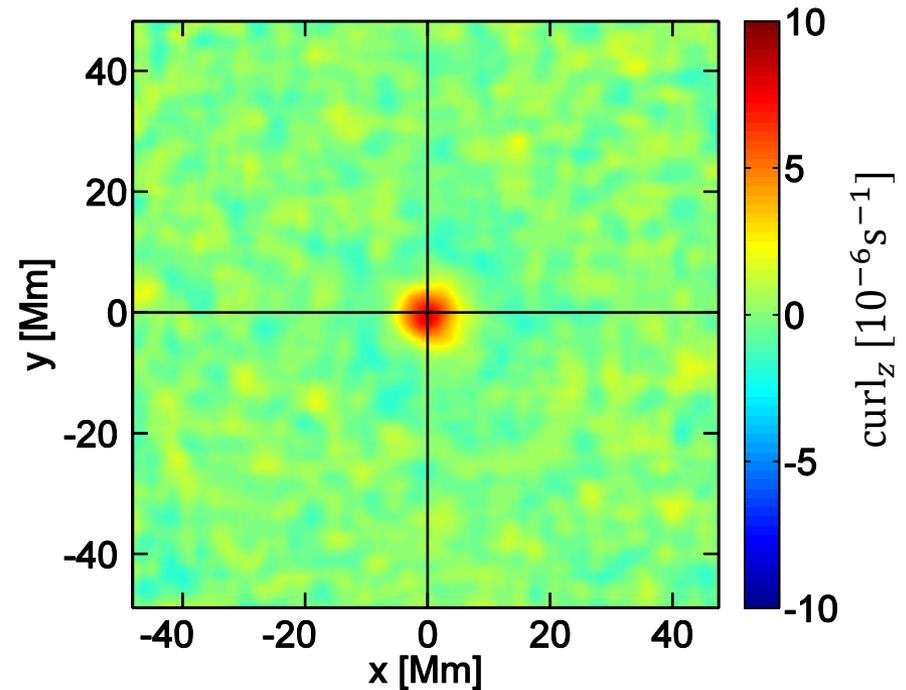
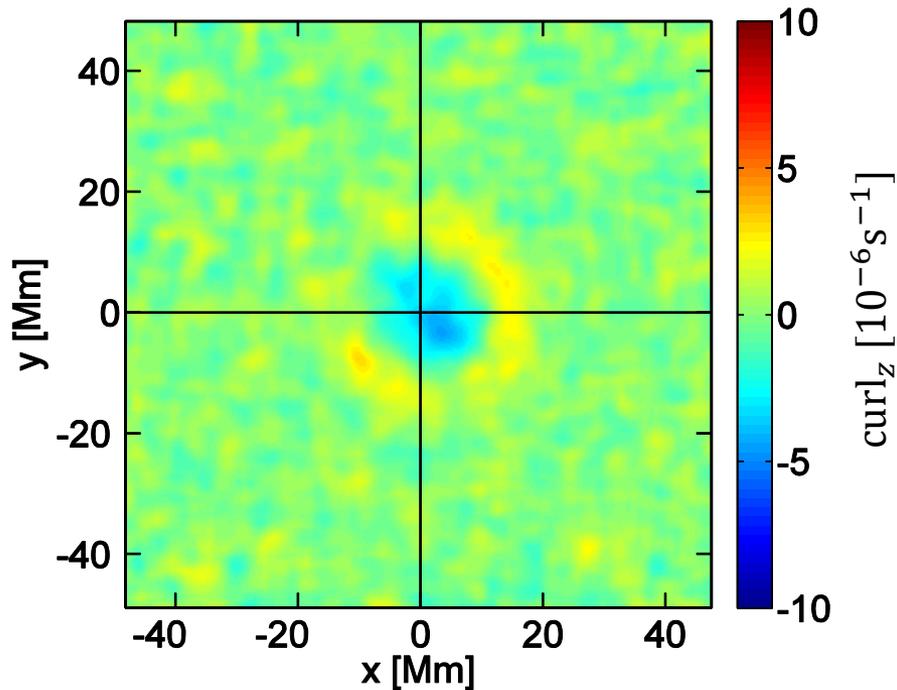


# LCT: Spatially resolved $\text{curl}_z$

outflow

$40^\circ$

inflow

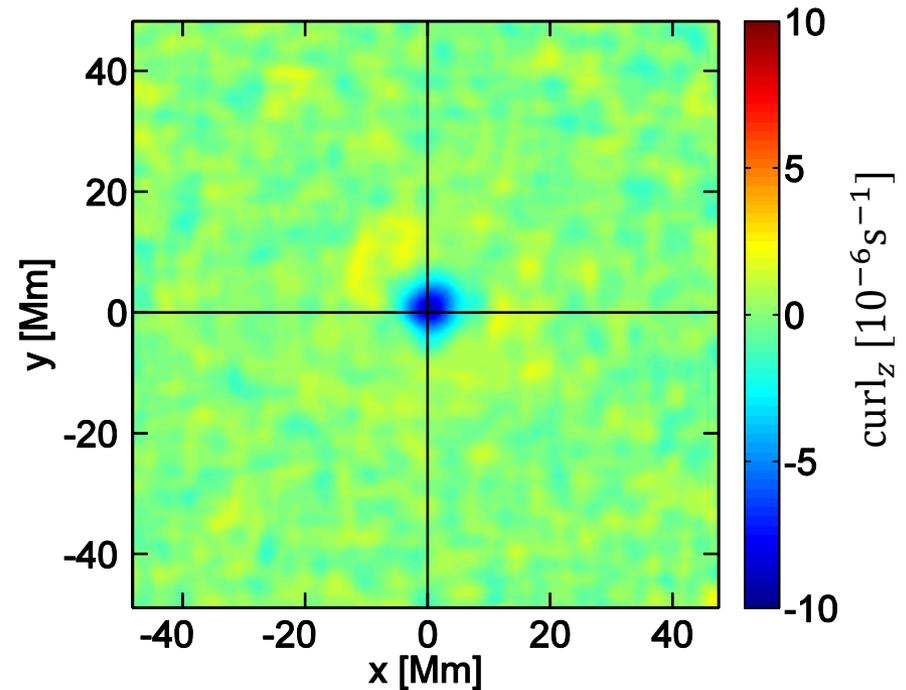
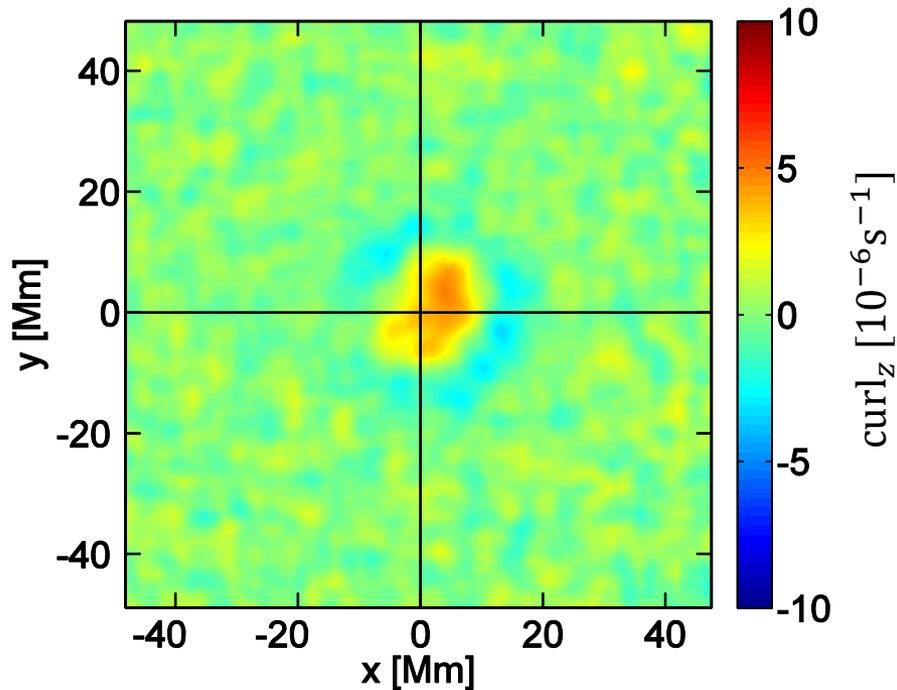


# LCT: Spatially resolved $\text{curl}_z$

outflow

$-40^\circ$

inflow



# Conclusions

- Circular velocity of the average supergranule measured with time-distance
- Result confirmed by LCT
- Horizontal flow profile measured with LCT
- $\text{curl}_z$  spatially resolved with LCT
- Time-distance can provide depth dependence (inversion)



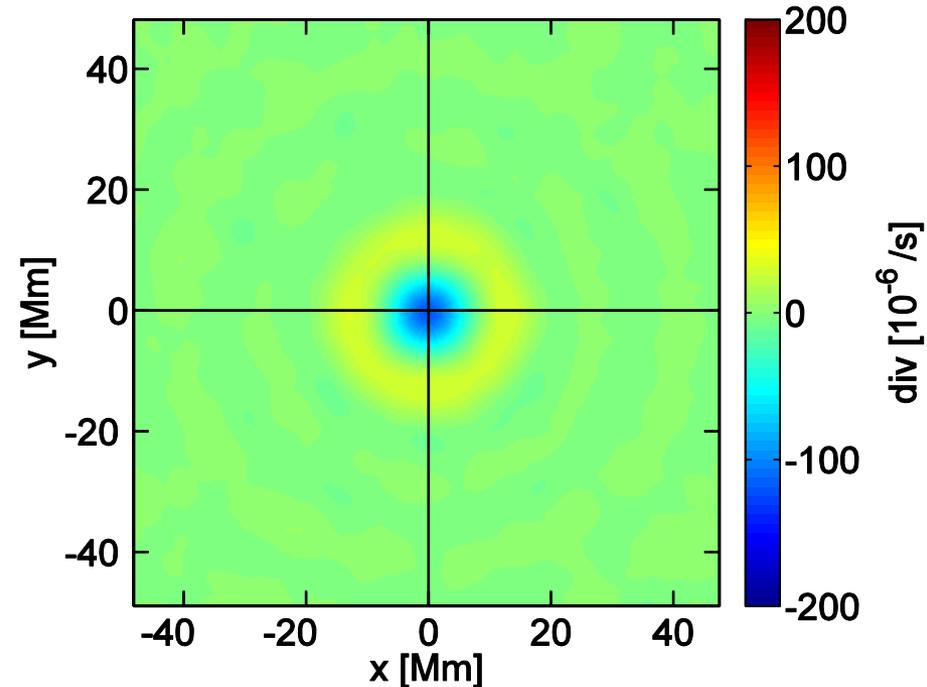
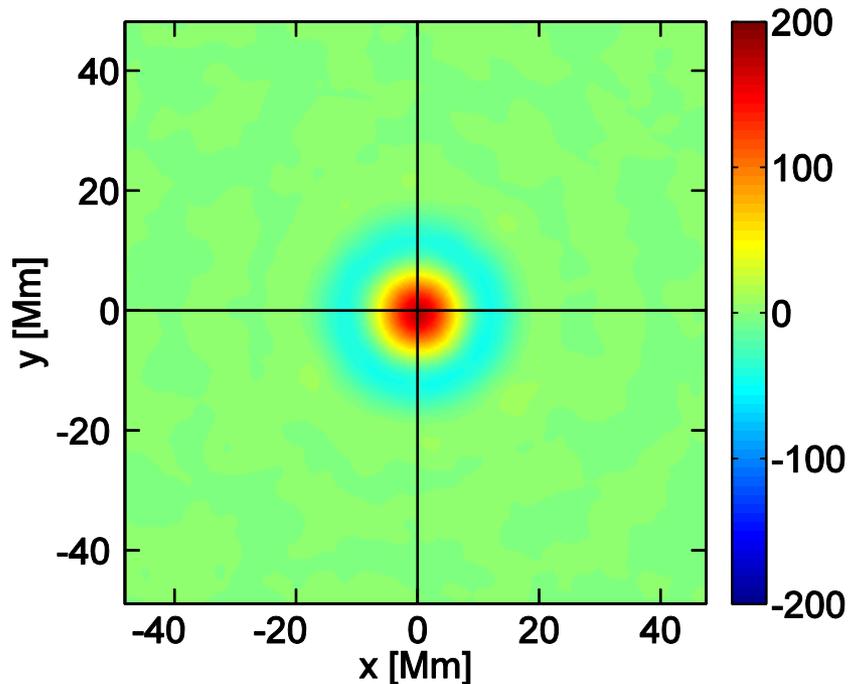
**Thank you  
for your attention!**

# LCT: Spatially resolved $\text{div}_h$

outflow

$40^\circ$

inflow

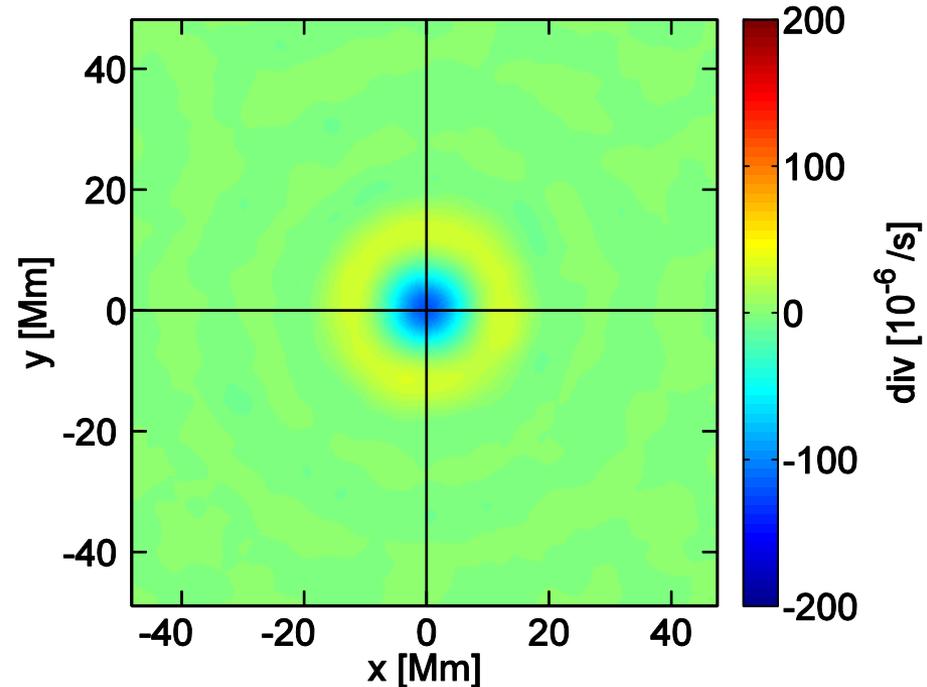
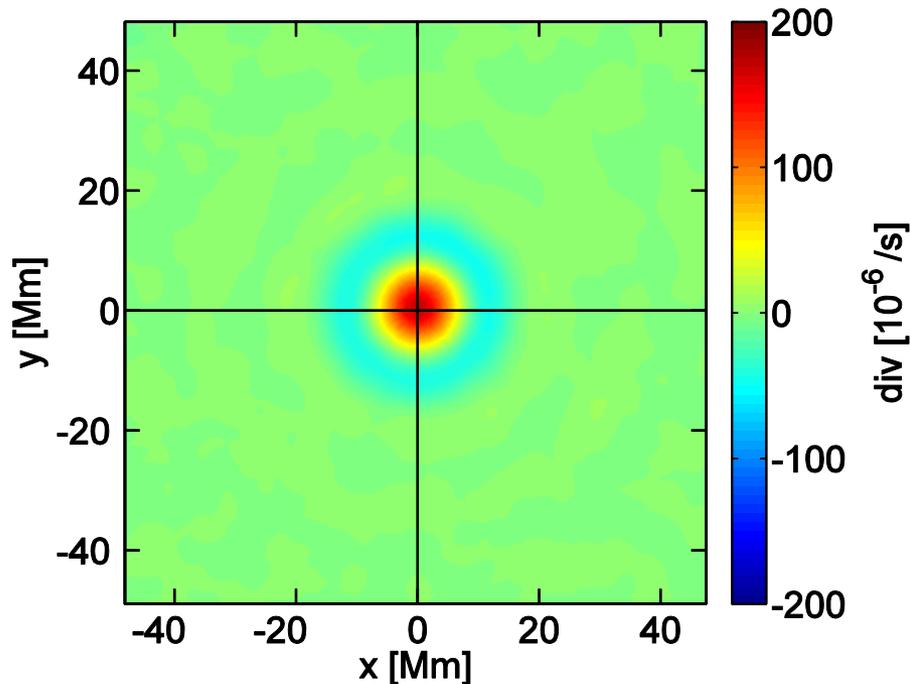


# LCT: Spatially resolved $\text{div}_h$

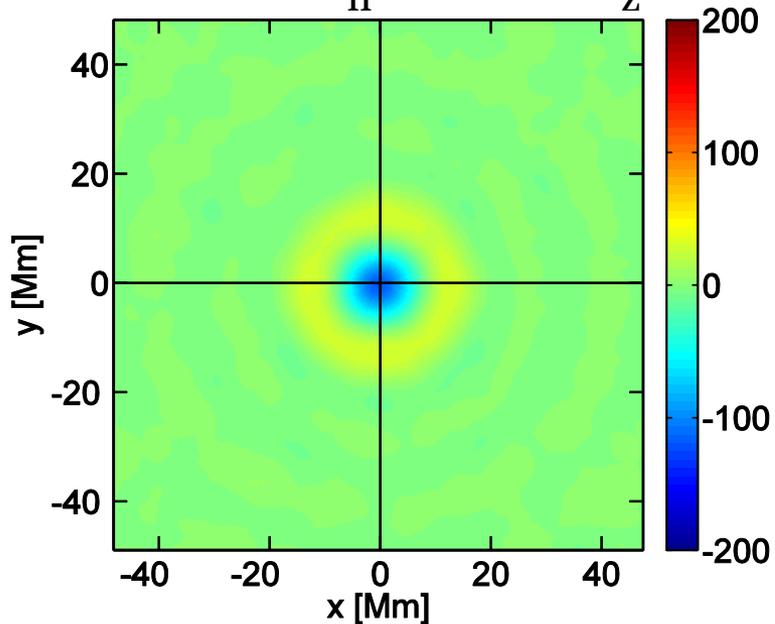
outflow

$-40^\circ$

inflow



# LCT $\text{div}_h$ and $\text{curl}_z$

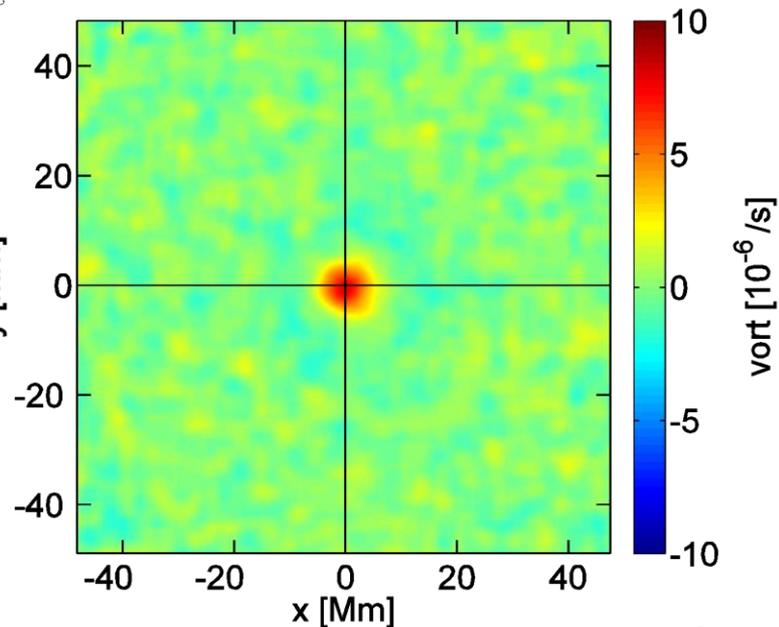


inflow

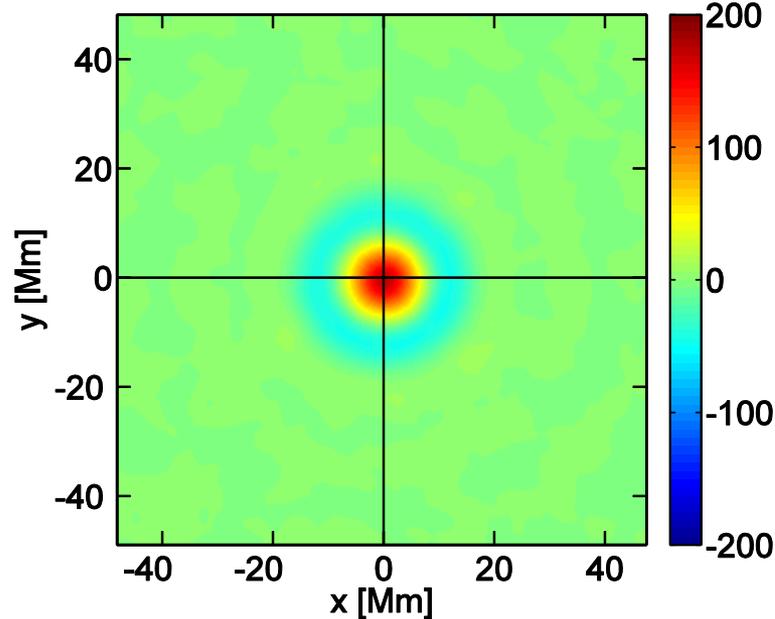
$\text{div} [10^{-6}/\text{s}]$



$40^\circ$



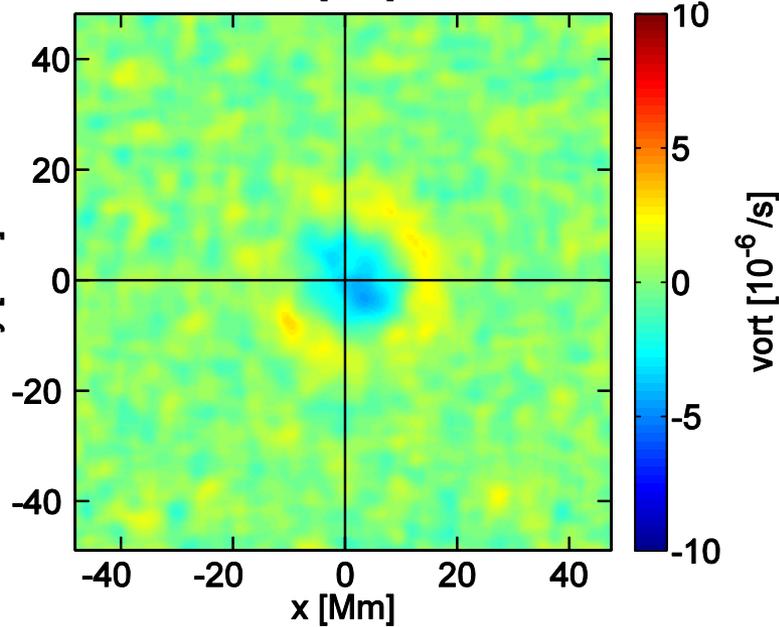
$\text{vort} [10^{-6}/\text{s}]$



$\text{div} [10^{-6}/\text{s}]$

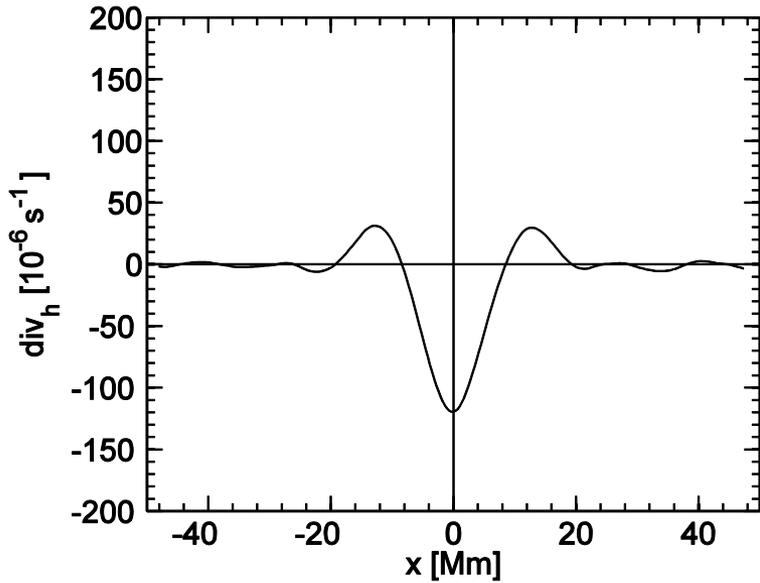


outflow



$\text{vort} [10^{-6}/\text{s}]$

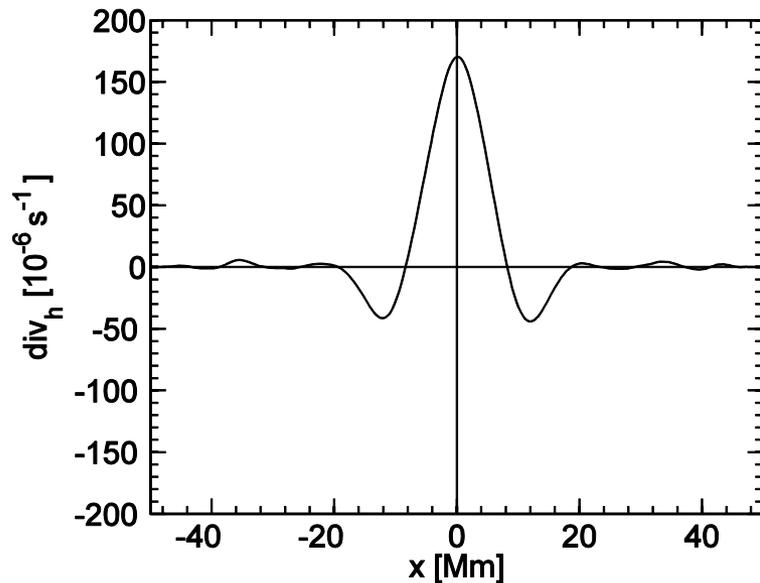
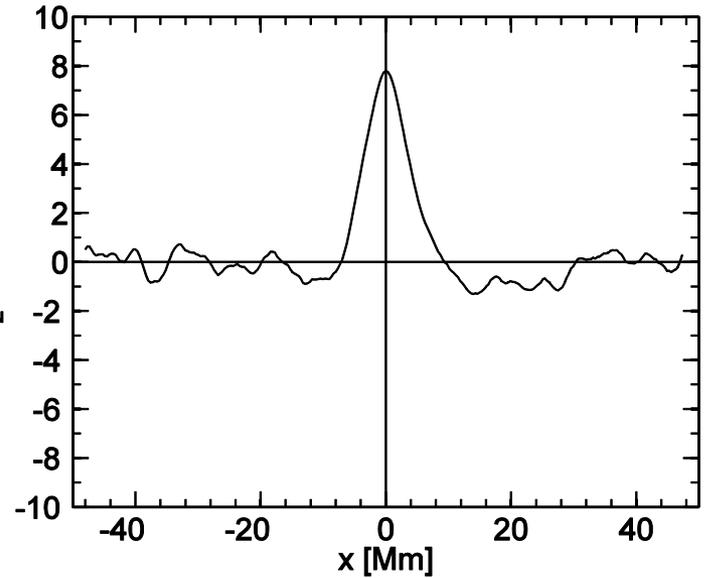
# LCT $\text{div}_h$ and $\text{curl}_z$ cuts $y=0$



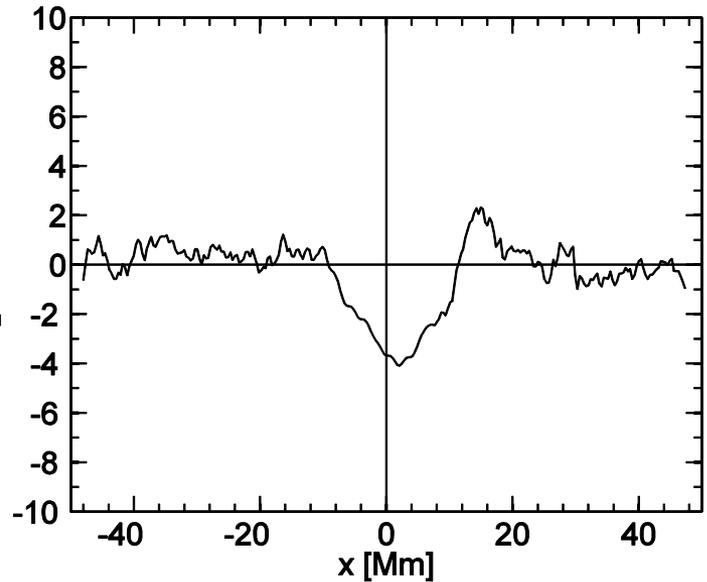
inflow



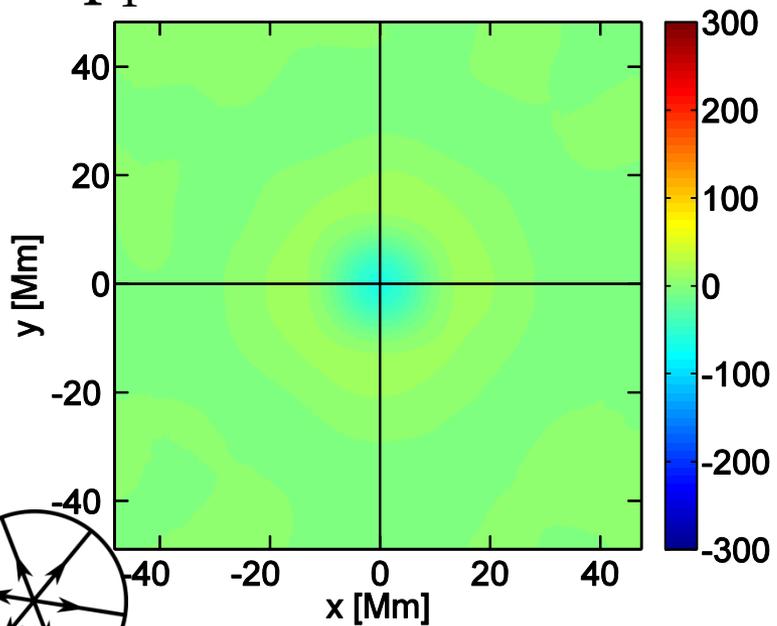
40°



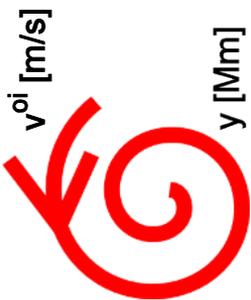
outflow



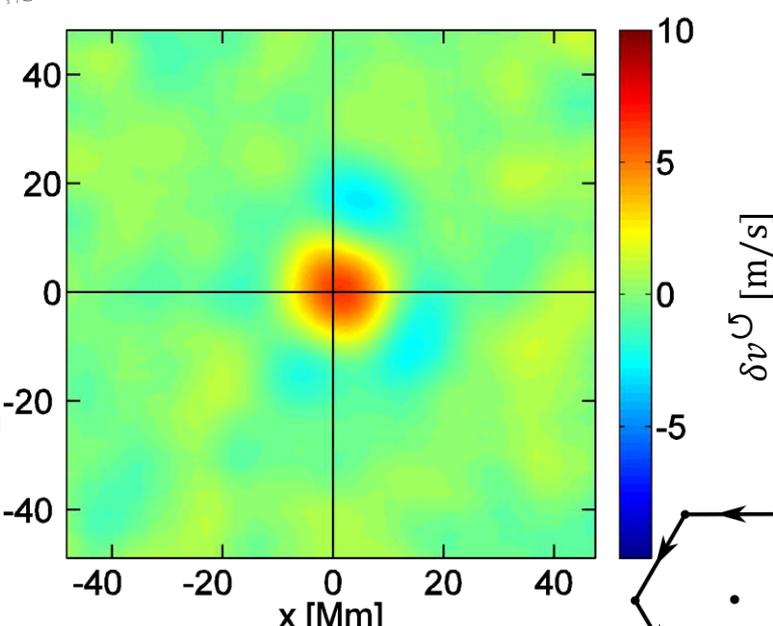
# $p_1$ mode



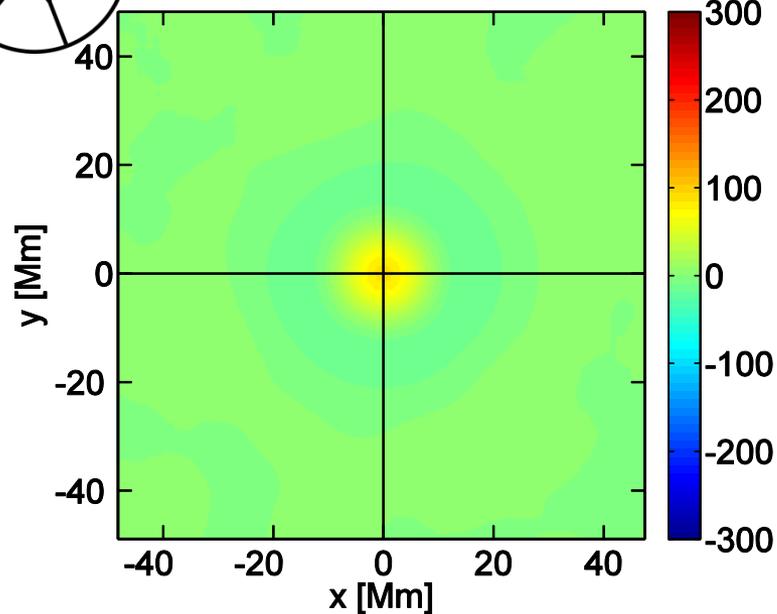
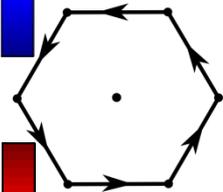
inflow



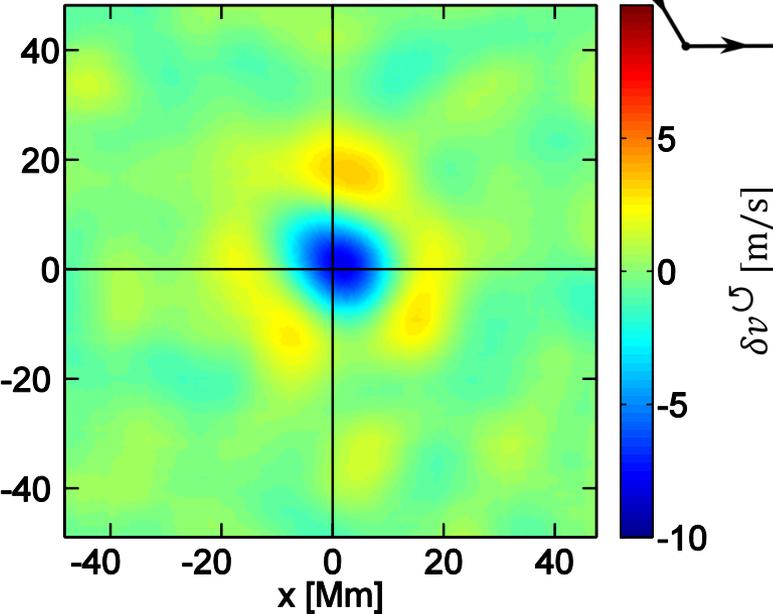
$40^\circ$



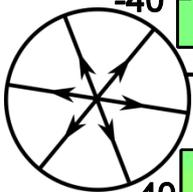
$\delta v^o$  [m/s]



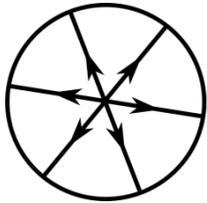
outflow



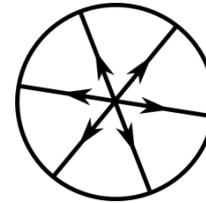
$\delta v^o$  [m/s]



# Comparison: Time-distance vs. LCT

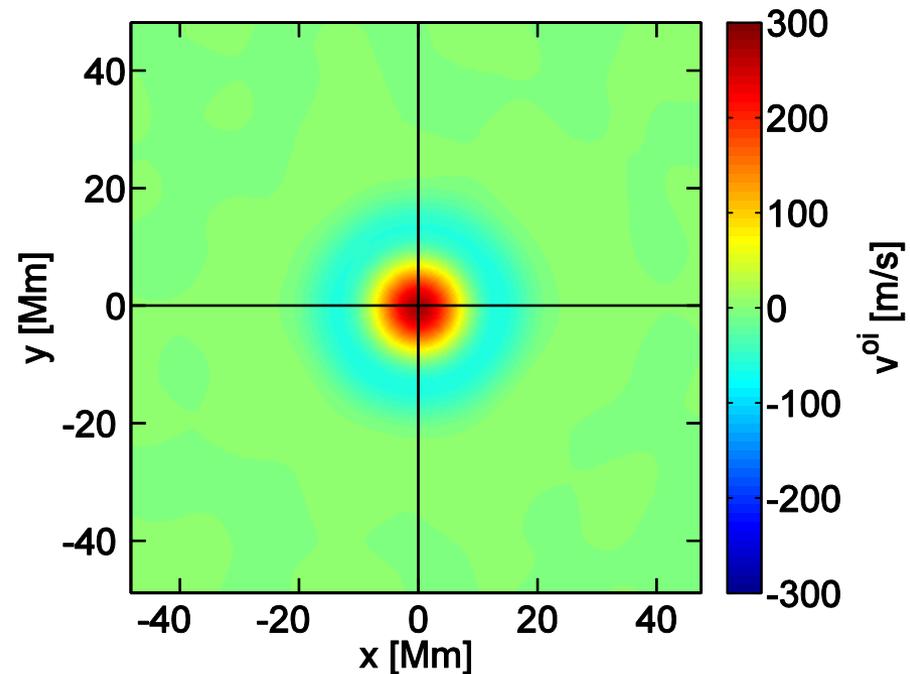
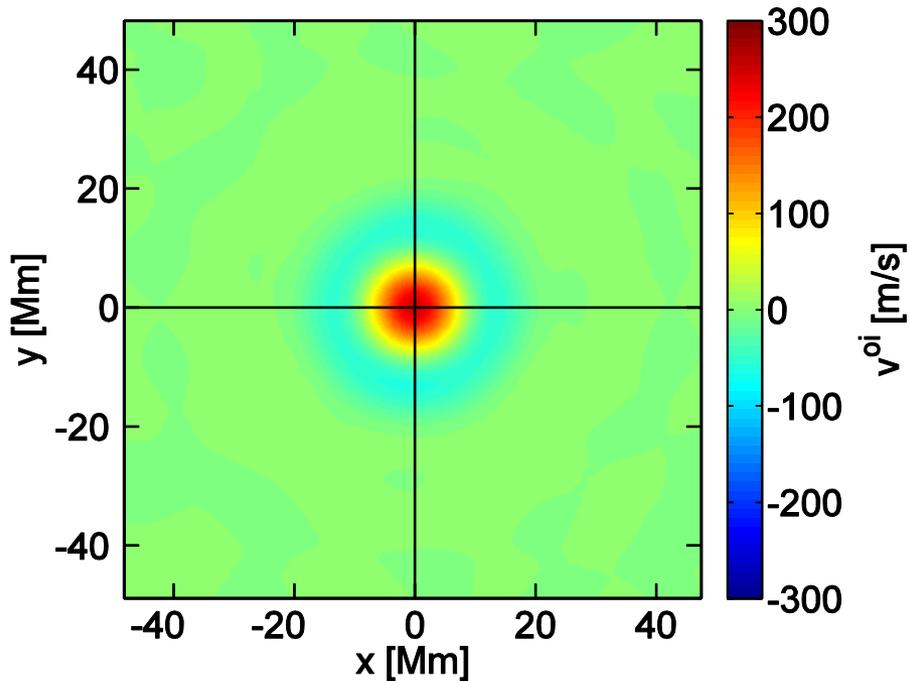


**40°  
outflow**



Time-distance (f mode)

LCT



# LCT: avg. supergranule flow profiles

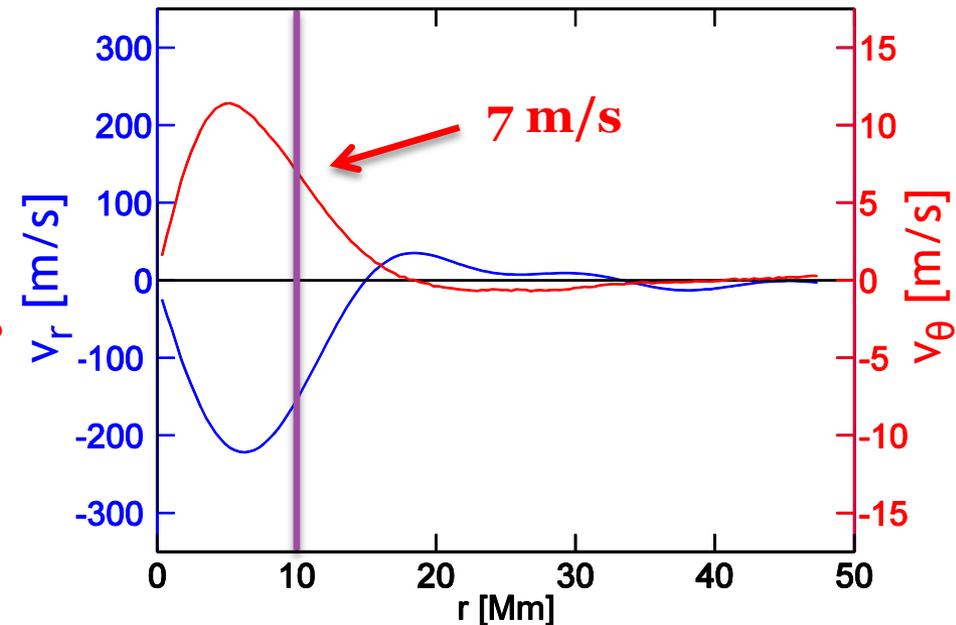
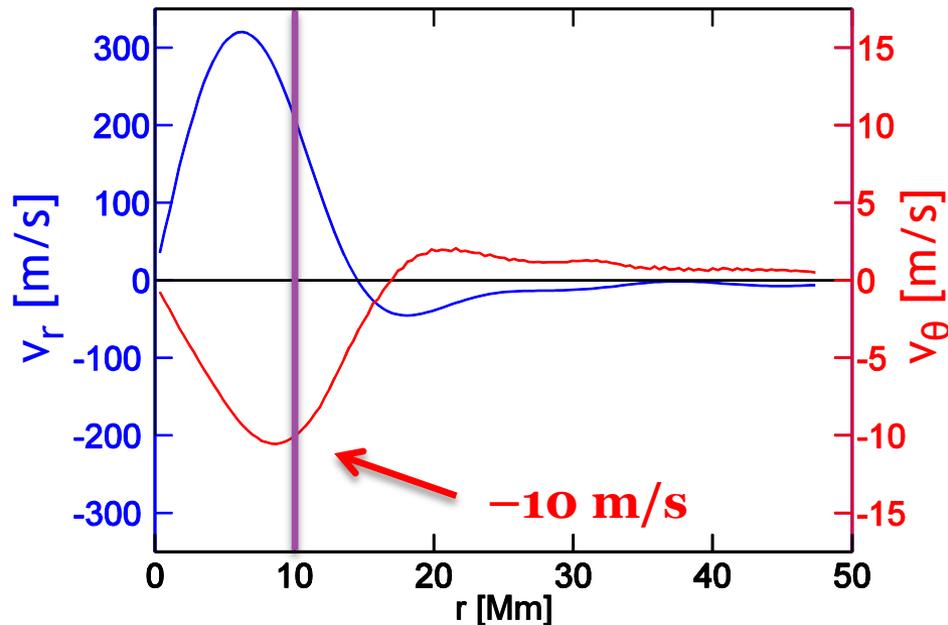
outflow

$40^\circ$

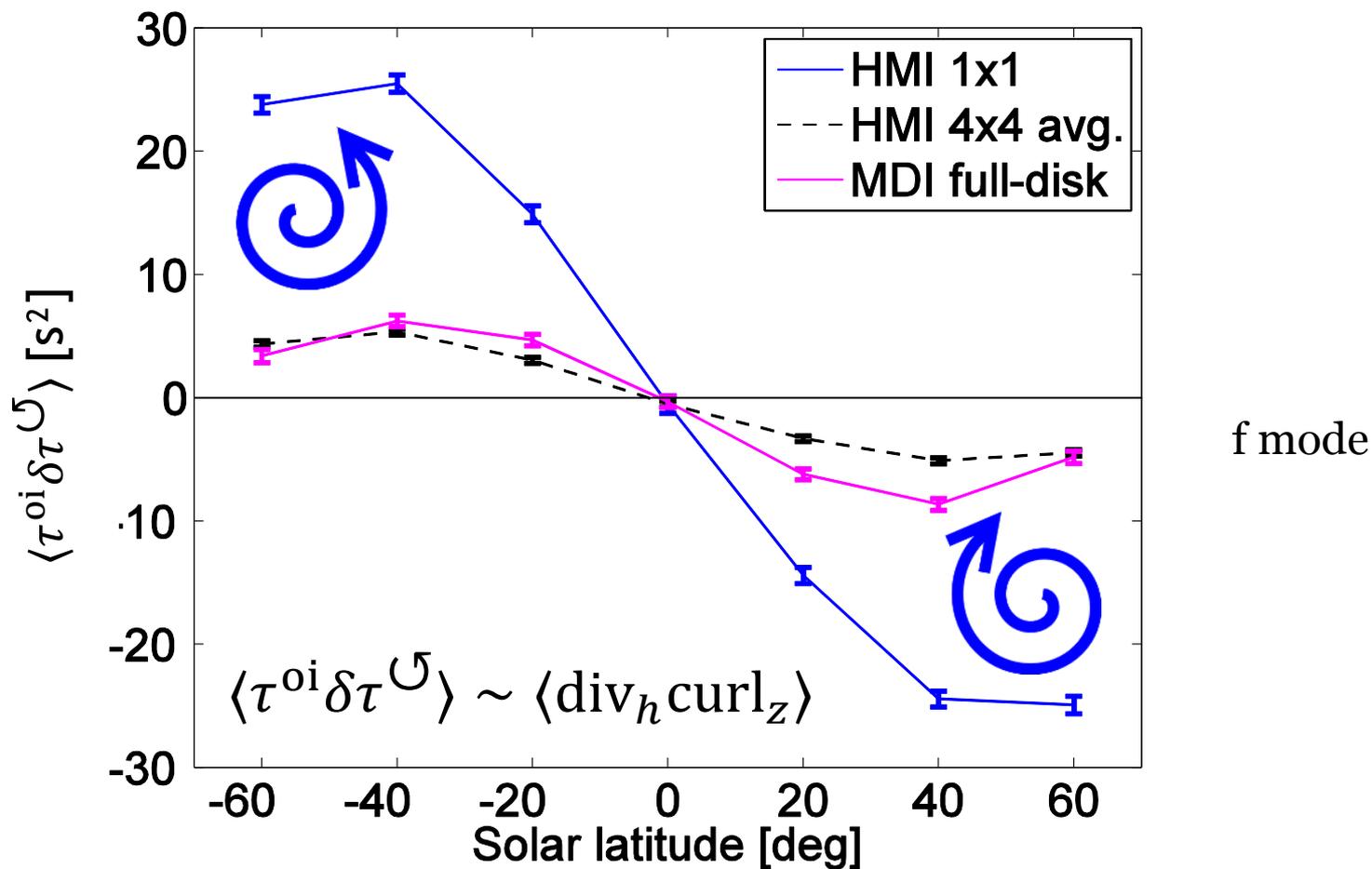
inflow

$r = 10 \text{ Mm}$

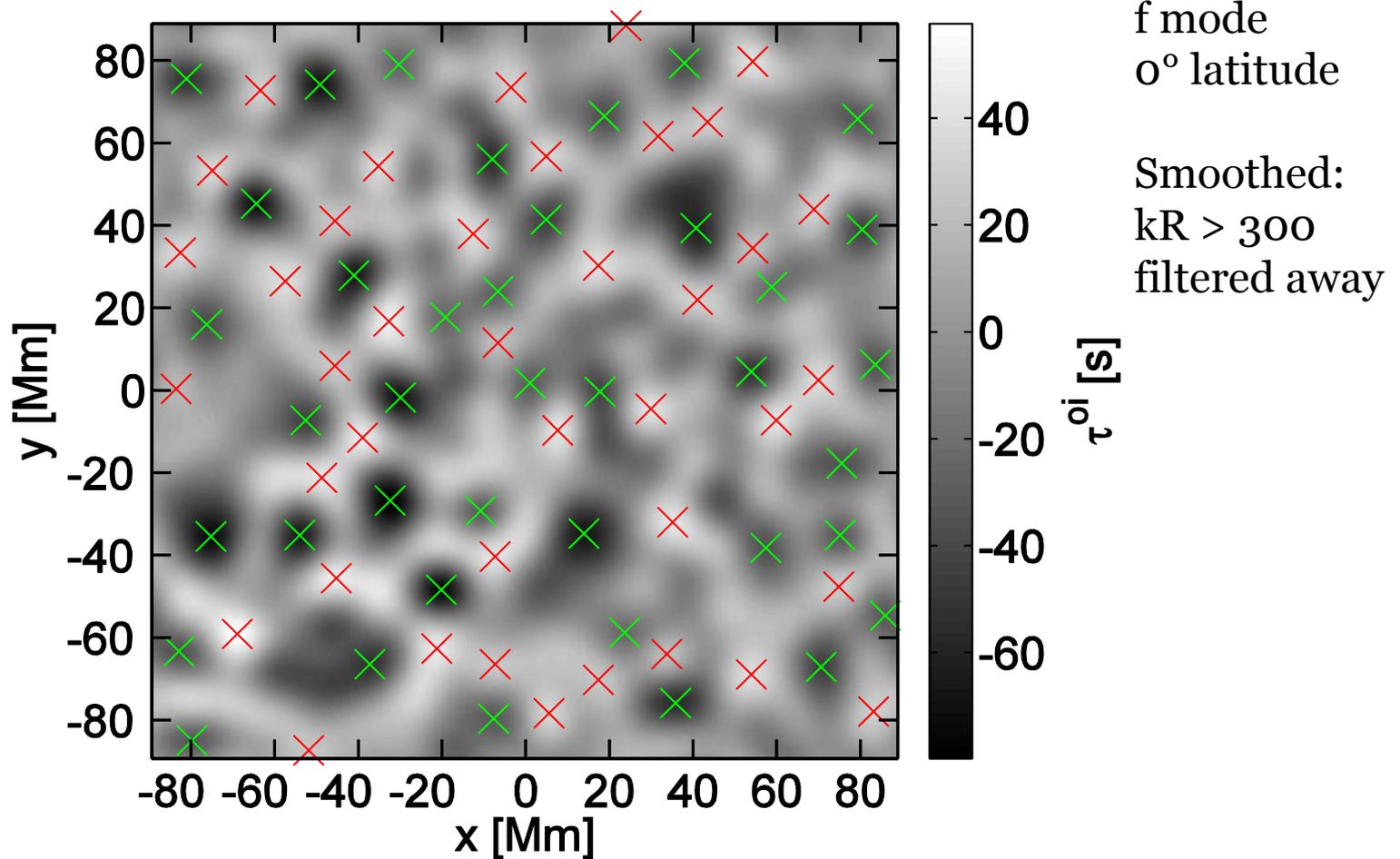
$r = 10 \text{ Mm}$



# $\langle \text{div}_h \text{curl}_z \rangle$ vs. latitude: HMI and MDI

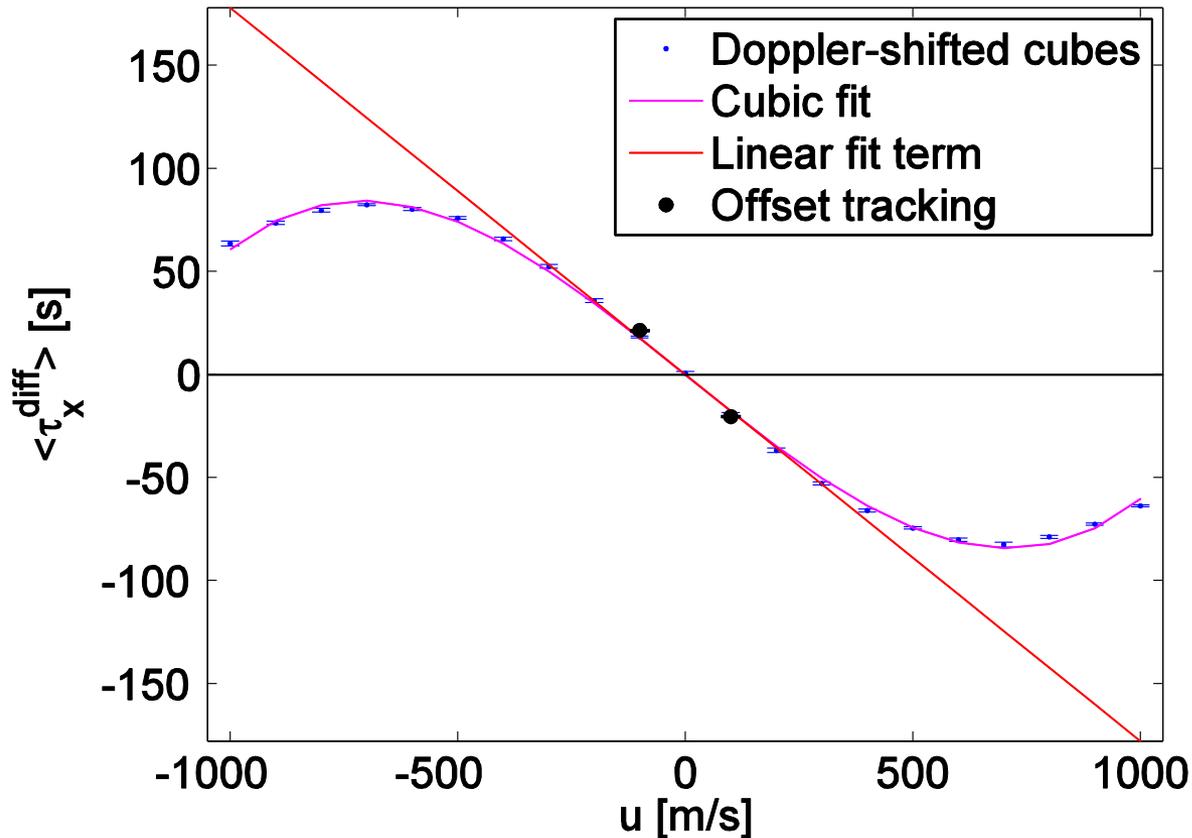


# Supergranule identification



# Conversion factor (f mode)

$\langle \tau_x^{\text{diff}} \rangle$  Doppler-shifted,  $d=10\text{Mm}$ ,  $f\text{mode}$ ,  $c=-0.17789\text{s}^2/\text{m}$



# Travel-time power spectra

