## Coronal expansion and solar wind

- The large solar corona
- Coronal and interplanetary temperatures
- Coronal expansion and solar wind
- The heliosphere
- Origin of solar wind in magnetic network
- Multi-fluid models of the solar wind

Electron density in the corona


Guhathakurta and Sittler, 1999, Ap.J., 523, 812

Skylab coronagraph/Ulysses in-situ

The visible solar corona


Electron temperature in the corona


Solar wind stream structure and heliospheric current sheet


## Solar wind fast and slow streams



## Fast solar wind parameters

- Energy flux at $1 \mathbf{R}_{\mathbf{s}}$ :
$F_{E}=510^{5} \mathrm{erg} \mathrm{cm}^{-2} \mathrm{~s}^{-1}$
- Speed beyond 10 R $_{s}: \quad V_{p}=(700-800) \mathbf{k m ~ s}^{-1}$
- Proton flux at 1 AU: $n_{p} V_{p}=210^{8} \mathbf{c m}^{-2} \mathrm{~s}^{-1}$
- Density at $1 \mathrm{AU}: \quad \mathrm{n}_{\mathrm{p}}=\mathbf{3} \mathbf{c m}^{-3} ; \mathrm{n}_{\alpha} / \mathbf{n}_{\mathrm{p}}=\mathbf{0 . 0 4}$
- Temperatures at 1 AU:
$\mathrm{T}_{\mathrm{p}}=310^{5} \mathrm{~K} ; \mathrm{T}_{\alpha}=10^{6} \mathrm{~K} ; \mathrm{T}_{\mathrm{e}}=1.510^{5} \mathrm{~K}$
- Heavy ions: $\quad T_{i} \cong m_{i} / m_{p} T_{p} ; \quad V_{i}-V_{p}=V_{A}$

Model of coronal-heliospheric field


Fisk, JGR, 1996

## Correlations between wind speed and corona temperature



## On the source regions of the fast

 solar wind in coronal holes


## Magnetic network loops and funnels



Height profiles in funnel flows


- Heating by wave sweeping
- Steep temperature gradients

- Critical point at $1 \mathbf{R}_{\mathbf{s}}$

Hackenberg, Marsch, Mann, A\&A, 360, 1139, 2000

Outflow speed in interplume region at the coronal base


O VI 1031.9 A / $1037.2 \AA$ line ratio; Doppler dimming

$T_{e}=T_{i}=0.9 M K, n_{e}=1.810^{7} \mathrm{~cm}^{-3}$

[^0]Oxygen and hydrogen thermal speeds in coronal holes




Cranmer et al., Ap.
J., 511, 481, 1998

Large anisotropy: $\quad \mathrm{T}_{\mathrm{O} \perp} / \mathrm{T}_{\mathrm{O}| |} \geq 10$

Fast solar wind speed profile


Solar wind in Carrington longitude


Heliosphere and local interstellar medium

(red) $-0.3>\log \left(\mathrm{n}_{\mathrm{e}} / \mathrm{cm}^{3}\right)>-3.7$ (blue)
Kausch, 1998

Boundaries of coronal holes



## Sun's loss of angular momentum carried by the solar wind II

## Changing corona and solar wind



Sun's loss of angular momentum carried by the solar wind I

Induction equation:
$\nabla \times(\mathbf{V} \times \mathbf{B})=0 \quad-->\quad r\left(V_{r} B_{\phi}-B_{r} V_{\phi}\right)=-r_{0} B_{0} \Omega_{0} r_{0}$

| Momentum equation: |
| :--- |
| $\rho \mathbf{V} \cdot \nabla V_{\phi}=1 / 4 \pi \mathbf{B} \cdot \nabla B_{\phi}-->\quad r\left(\rho V_{r} V_{\phi}-B_{r} B_{\phi}\right)=0$ |
| $L=\Omega_{0} r_{A}{ }^{2} \quad$ (specific angular momentum) |

$$
V_{\phi}=\Omega_{0} r\left(M_{A}^{2}\left(r_{A} / r\right)^{2}-1\right) /\left(M_{A}^{2}-1\right) \quad M_{A}=V_{r}(4 \pi \rho)^{1 / 2} / B_{r}
$$

Weber \& Davis, ApJ, 148, 217, 1967
Helios: $r_{A}=10-20 R_{s}$


New solar wind data from Ulysses



Speed profile of balloon-type CMEs


Srivastava et al., 1999
Wide range of initial acceleration: 5-25 ms

## Non-stationary slow solar wind



## Corona of the active sun



## Solar wind models I

Assume heat flux, $Q_{e}=-\rho \kappa \nabla T_{e}$, is free of divergence and thermal equilibrium: $T=T_{p}=T_{e}$. Heat conduction: $\kappa=\kappa_{0} T^{5 / 2}$ and $\kappa_{o}=810^{8}$ $\mathrm{erg} /(\mathrm{cm} \mathrm{s} \mathrm{K})$; with $\mathrm{T}(\infty)=0$ and $\mathrm{T}(0)=10^{6} \mathrm{~K}$ and for spherical symmetry:

$$
4 \pi \mathbf{r}^{2} \kappa(\mathbf{T}) \mathbf{d T} / \mathbf{d r}=\text { const } \quad-->\quad \mathrm{T}=\mathrm{T}_{0}(\mathrm{R} / \mathrm{r})^{2 / 7}
$$

Density: $\rho=n_{p} m_{p}+n_{e} m_{e}$ quasi-neutrality: $n=n_{p}=n_{e}$, thermal pressure: $p=n_{p} k_{B} T_{p}+n_{e} k_{B} T_{e}$, then with hydrostatic equilibrium and $p(0)=p_{0}$ :

$$
\mathrm{dp} / \mathrm{dr}=-\mathbf{G M m} \mathrm{p}^{n} / \mathrm{r}^{2}
$$

$$
p=p_{0} \exp \left[\left(7 G M m_{p}\right) /\left(5 k_{B} T_{0} R\right)\left((R / r)^{5 / 7}-1\right)\right]
$$

Problem: $\mathrm{p}(\infty)>0$, therefore corona must expand!

## Solar wind models II

Density: $\rho=n_{p} m_{p}+n_{e} m_{e}$, quasi-neutrality: $n=n_{p}=n_{e}$, ideal-gas
thermal pressure: $p=n_{p} k_{B} T_{p}+n_{e} k_{B} T_{e}$, thermal equilibrium: $T=T_{p}=T_{e}$, then with hydrodynamic equilibrium:
$\mathbf{m n}_{\mathbf{p}} \mathbf{V d V} / \mathbf{d r}=\mathbf{- d p} / \mathbf{d r}-\mathbf{G M m} \mathbf{p}_{\mathbf{n}} / \mathbf{r}^{\mathbf{2}}$
Mass continuity equation:

$$
\mathrm{mn}_{\mathrm{p}} \mathbf{V} \mathbf{r}^{2}=\mathbf{J}
$$

Assume an isothermal corona, with sound speed $c_{0}=\left(k_{B} T_{0} / m_{p}\right)^{1 / 2}$, then one has to integrate the DE:

$$
\left[\left(V / c_{0}\right)^{2}-1\right] d V / V=2\left(1-r_{c} / r\right) d r / r
$$

With the critical radius, $\mathrm{r}_{\mathrm{c}}=\mathrm{GMm} / \mathrm{P} /\left(2 \mathrm{k}_{\mathrm{B}} \mathrm{T}_{0}\right)=\left(\mathrm{V}_{\mathrm{o}} / 2 \mathrm{c}_{0}\right)^{2}$, and the escape speed, $\mathrm{V}_{\infty}=618 \mathrm{~km} / \mathrm{s}$, from the Sun's surface.

## Fluid equations

- Mass flux:

$$
F_{M}=\rho V A \quad \rho=n_{p} m_{p}+n_{i} m_{i}
$$

- Magnetic flux:

$$
F_{B}=\mathbf{B A}
$$

- Total momentum equation:
$V d / d r V=-1 / \rho d / d r\left(p+p_{w}\right)-G M_{s} / r^{2}+a_{w}$
- Thermal pressure: $\quad p=n_{p} k_{B} T_{p}+n_{e} k_{B} T_{e}+n_{i} k_{B} T_{i}$
- MHD wave pressure: $p_{w}=(\delta B)^{2} /(8 \pi)$
- Kinetic wave acceleration: $\mathbf{a}_{\mathbf{w}}=\left(\rho_{p} \mathbf{a}_{\mathbf{p}}+\rho_{\mathrm{i}} \mathbf{a}_{\mathrm{i}}\right) / \rho$
- Stream/flux-tube cross section: A(r)


## Proton and electron temperatures

Electrons are cool!

Protons are hot!

Marsch, 1991

slow wind
$\downarrow$ fast wind
fast wind $\downarrow$
slow wind

## Solar wind models III

Introduce the sonic Mach number as, $\mathrm{M}_{\mathrm{s}}=\mathrm{V} / \mathrm{c}_{0}$, then the integral of the $D E$ ( $C$ is an integration constant) reads:
$\left(M_{s}\right)^{2}-\ln \left(M_{s}\right)^{2}=4\left(\ln \left(r / r_{c}\right)+r_{c} / r\right)+C$
For large distances, $M_{s} \gg 1$; and $V \sim(\ln r)^{1 / 2}$, and $n \sim r^{2} / V$, reflecting spherical symmetry.

Only the „wind" solution IV, with $\mathrm{C}=-3$, goes through the critical point $\mathrm{r}_{\mathrm{c}}$ and yields: $\mathrm{n}->0$ and thus $p->0$ for $r \rightarrow \infty$. This is Parker's famous solution: the solar wind.


Parker, 1958
V, solar breeze; III accretion flow


## Energy equations

Parallel
thermal
energy

$$
\frac{d}{d r} v_{\| j}^{2}=-2 v_{\| j}^{2}\left(\frac{1}{u_{j}} \frac{d u_{j}}{d r}\right)+\frac{2 q_{\| j}}{u_{j}}+\left(\mathbf{Q}_{\| \mathbf{j}}+\mathbf{S}_{\| \mathbf{j}}\right) / \mathbf{u}_{\mathbf{j}}
$$

w-p terms + sources + sinks
Perpendicular
thermal
energy
$\frac{d}{d r} v_{\perp j}^{2}=-v_{\perp j}^{2}\left(\frac{1}{A} \frac{d A}{d r}\right)+\frac{q_{\perp j}}{u_{j}}+\left(\mathrm{Q}_{\perp \mathrm{j}}+\mathrm{S}_{\perp \mathrm{j}}\right) / \mathrm{u}_{\mathrm{j}}$

Heating functions: $q_{\perp, \|} \ldots$ ?
Wave energy absorption/emission by wave-particle interactions !

Conduction/collisional exchange of heat + radiative losses

Heating and acceleration of ions by cyclotron and Landau resonance
$\left(\begin{array}{lll}\frac{\partial}{\partial t} U_{j \|} \\ \frac{\partial}{\partial t} V_{j \|}^{2} \\ \frac{\partial}{\partial t} V_{j \perp}^{2}\end{array}\right)=2 \mathrm{a}_{\mathrm{j}} \quad$ acceleration $\quad=\begin{aligned} & \text { parallel heating } \\ & =2 \perp\end{aligned}$
$=\frac{1}{(2 \pi)^{3}} \int_{-\infty}^{+\infty} d^{3} k \sum_{M} \hat{\mathcal{B}}_{M}(\mathbf{k})\left(\frac{\Omega_{j}}{k}\right)^{2} \frac{1}{1-\left|\hat{\mathbf{k}} \cdot e_{M}(\mathbf{k})\right|^{2}}$
$\times \sum_{s=-\infty}^{+\infty} \mathcal{R}_{j}(\mathbf{k}, s)\left(\begin{array}{c}k_{\|} \\ 2 k_{\|} w_{j}(\mathbf{k}, s) \\ s \Omega_{j}\end{array}\right)$
Wave spectrum ? Wave dispersion ? Resonance function ?


## Model of the fast solar wind



## Anisotropic two-fluid model of the fast solar wind


$\mathrm{T} / \mathbf{1 0}^{\mathbf{5}} \mathrm{K}$

- Anisotropic heat deposition in 1-D two-fluid model
- Alfvén wave pressure gradient
$\mathrm{v} / \mathrm{km} \mathrm{s}^{-1}$

Hu et al., JGR,
102, 14661, 1997


- Anisotropy weakly influences dynamics
- Anisotropy needed for perpendicular ioncyclotron heating and thermodynamics

Coronal base:
$\delta v \approx \mathbf{1 0 - 2 0 ~} \mathbf{k m ~ s}^{-1}$
$\xi \approx 20-30 \mathrm{~km} \mathrm{~s}^{-1}$

## Two-dimensional two-fluid MHD model of the solar corona

- Time-dependent

2-D model MHD with separate $T_{e}$ and $T_{p}$ equations

- Slow outflow at equator, fast over poles after 1 day
- Heating functions $\mathrm{Q}_{\mathrm{e}}$ and $\mathrm{Q}_{\mathrm{p}}$ latitudedependent

Suess et al., JGR, 104, 4697, 1999

## Four-fluid model for turbulence driven heating of coronal ions



## Solar Orbiter's novel orbital design




[^0]:    Patsourakos and Vial, A\&A, 359, L1, 2000

