

Origins of Solar Systems

Lecture held for the International Max Planck Research School
“Solar System and beyond”
February 13-15, 2006

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including student lectures by
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Origin of solar systems: Organization

Lecture (KJ):

Introduction and overview
Dense molecular clouds, photo-
dissociation regions and protostars

Protoplanetary disks
Equilibrium condensation of a solar nebula

Meteorites and the early solar system

Origin of giant planets

Comets and the early solar system

Student talks:

Origin of the elements and Standard
Abundance Distribution

Agglomeration of planetesimals and
protoplanets

Isotope chronology of meteorites and
oxygen isotopes

Extrasolar planets

Transneptunian Objects

Schedule:

Monday und Tuesday: 9:30-12:15 (3*45 Min plus 2*15 Min break)

14:00-16:45

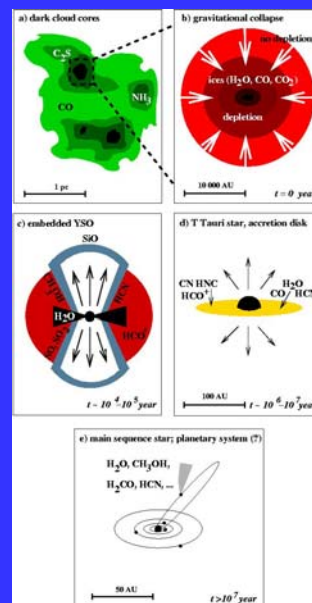
Wednesday: 9:30-12:15

Wednesday afternoon: Seminar and Colloquium

Solar system formation

Early stages (Ewine van Dieshoek, Leiden) a-d

- A lot of steps between d and e:
- Protoplanetary disk is hot near the Sun and cold far from the Sun, condensation of gas depending on temperature
- Formation and growth of planetesimals (strongly dependent on relative velocity)
- Formation of terrestrial and giant planets
- Early Jupiter prevents planetesimal growth in its neighborhood → origin of asteroids
- Comets originate in the Kuiper belt at about 40 AU from the Sun
- Long-period comets are scattered into Oort cloud, disturbed and isotropized by the influence of passing stars and the galactic bulge.
- Short-period comets go directly from Kuiper belt to the inner solar system
- Meteorites come from the surfaces of asteroids and from Mars to the Earth. Their measurement in the laboratory has contributed greatly to our knowledge about solar system formation.



Excuse on
blackbody
radiation.

Radiation laws related to Planck's law

$$B_\nu(T)d\nu = \frac{2h\nu^3}{c^2} \frac{1}{e^{h\nu/kT} - 1} d\nu \quad \text{W m}^{-2} \text{ rad}^{-2}$$

or, using

$$B_\lambda(T)d\lambda = B_\nu(T)d\nu \cdot c/\lambda^2$$

$$B_\lambda(T)d\lambda = \frac{2hc^2}{\lambda^5} \frac{1}{e^{hc/\lambda kT} - 1} d\lambda \quad \text{W m}^{-2} \text{ rad}^{-2}$$

$$\frac{h\nu}{kT} \gg 1 \quad B_\nu(T) \approx \frac{2h\nu^3}{c^2} e^{-h\nu/kT} d\nu \quad \text{Wien}$$

$$\frac{h\nu}{kT} \ll 1 \quad B_\nu(T) \approx \frac{2\nu^2 kT}{c^2} \quad \text{Rayleigh-Jeans}$$

Wien's displacement law:

$$\frac{c}{\nu_{max}} \cdot T = 5.10 \cdot 10^{-3} \quad [\text{meter K}] \quad \text{or}$$

$$\lambda_{max} \cdot T = 2.90 \cdot 10^{-3} \quad [\text{meter K}]$$

With $T = 290 \text{ K}$ (room temperature) we get $\lambda_{max} = 10^{-5} \text{ m} = 10 \mu\text{m}$.

With $T = 5800 \text{ K}$ (solar-type star) we get $\lambda_{max} = 0.5 \mu\text{m}$.

Dense molecular clouds,
photodissociation regions and protostars

Excuse: The H₂ molecule

106 F. Combes, Molecules in galaxies at all redshifts, in "The cold universe" Saas-Fee advanced course 32, Springer 2002, pp105-212

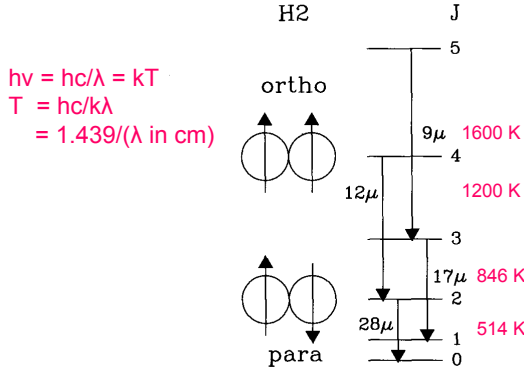


Fig. 1. Schematic of the first levels of the H₂ molecule. The even-*J* levels are the para-hydrogen, while the odd-*J* levels are from the ortho-hydrogen. The coupled levels obey $\Delta J = \pm 2$, for quadrupolar transitions, and the two species are not radiatively coupled. The four first rotational lines of hydrogen S(*J*) (where *J* is the lower state) are represented - wavelengths in μm , S(3) = 9, S(2) = 12, S(1) = 17 and S(0) = 28.

Easily observable:
 $v=1 \rightarrow 0$ S(1)
 rotation vibration
 line at 2.121 μm ,
 $T \approx 2500$ K
 in K band
 (shock waves)

Note: at the low
 temperature of
 dense molecular
 clouds H₂ does not
 radiate at all!

In contrast CO:
 $J=1$ 5.2 K above
 ground.
 CO tracer for H₂
 $[\text{CO}] = 10^{-5} [\text{H}_2]$

In dense molecular clouds H₂ is most abundant but can form only on grain surfaces.

Different phases of the interstellar medium

Physical Characteristics of Molecular Regions in the Interstellar Medium^a

	Density (cm ⁻³)	<i>T</i> (K)	Mass M _⊙	<i>A_V</i> (mag)	Size (pc)	ΔV (km s ⁻¹)	Examples
Diffuse Clouds	100 – 800	30 – 80	1 – 100	≲ 1	1 – 5	0.5 – 3	ζ Oph
Translucent Clouds	500 – 5000	15 – 50	3 – 100	1 – 5	0.5 – 5	0.5 – 3	HD 169454; High-latitude clouds
Cold, Dark Clouds							
complex	10 ² – 10 ³	≈ 10	10 ³ – 10 ⁴	1 – 2	6 – 20	1 – 3	Taurus-Auriga
clouds	10 ² – 10 ⁴	≈ 10	10 – 10 ³	2 – 5	0.2 – 4	0.5 – 1.5	B1, B5
cores/clumps	10 ⁴ – 10 ⁵	≈ 10	0.3 – 10	5 – 25	0.05 – 0.4	0.2 – 0.4	TMC-1, B335
Giant Molecular Clouds							
complex	100 – 300	15 – 20	10 ⁵ –3 × 10 ⁶	1 – 2	20 – 80	6 – 15	M 17, Orion
clouds	10 ² – 10 ⁴	≈ 20	10 ³ – 10 ⁵	≈ 2	3 – 20	3 – 12	Orion OMC-1, W3 A
warm clumps	10 ⁴ – 10 ⁷	25 – 70	1 – 10 ³	5 – 1000	0.05 – 3	1 – 3	M 17 clumps, Orion I'5 S
hot cores	10 ⁷ – 10 ⁹	100 – 200	10 – 10 ³	50 – 1000	0.05 – 1	1 – 10	Orion hot core

^a Table adapted from Goldsmith (1987), Turner (1989a) and Friberg and Hjalmarson (1990).

Van Dishoek E.F. et al., in Levy and Lunine eds. "Protostars and Planets III", U. of Az. Press, 1993, pp 163-241.

Van Dishoek E.F. et al., in Levy and Lunine eds. "Protostars and Planets III",
U. of Az. Press, 1993.

TABLE I
Angular Sizes of Protostellar Objects and Capabilities of Telescopes^a

Linear size	Angular Size				Telescope ^b	Angular Resolution			
	Taurus 140 pc	Orion 450 pc	M17 2.2 kpc	Galactic Center 8.5 kpc		115 GHz	230 GHz	345 GHz	810 GHz
5 AU	0".04	0".01	—	—	45 m (Nobeyama)	15"	—	—	—
Inner solar nebula 100 AU	0".7	0".2	0".05	—	30 m (IRAM)	22"	12"	7"	—
Outer solar nebula 1000 AU	7"	2"	0".5	0".1	15 m (JCMT/SEST)	44"	20"	15"	6"
Presolar nebula 0.05 pc	74"	23"	5"	1"	10 m (CSO)	—	30"	20"	9"
Cloud core 0.5 pc	12'	4'	50"	12"	Interferometer (OVRO/ BIMA/Nobeyama/IRAM)	4-7"	1-2"	—	—

^a The table only lists the capabilities of currently operating telescopes, not those of future projects.
^b IRAM = Institut de Radio Astronomie Millimétrique; JCMT = James Clerk Maxwell Telescope; CSO = Caltech Submillimeter Observatory; SEST = Swedish-ESO Submillimetre Telescope; OVRO = Owens Valley Radio Observatory; BIMA = Berkeley-Illinois-Maryland Array.

The Taurus molecular cloud in CO emission.

Note the large extent of the cloud and the many small objects embedded in it.

The map has been done in the light of the CO molecule (millimeter wavelength).

CO is a very important interstellar molecule and believed to be a tracer of the (unobservable) H₂ molecule.

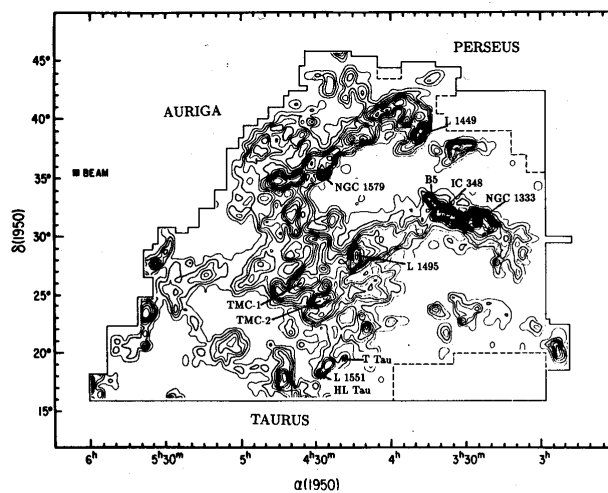


Figure 1. Velocity integrated intensity of CO emission in the Taurus molecular cloud complex. The lowest contour is 0.5 K km s⁻¹, and the separation between contours is 1.5 K km s⁻¹. The border of the surveyed region is indicated by the outer solid line. Various clouds such as B5 and cloud cores such as TMC-1 discussed in the text are indicated (figure adapted from Ungerechts and Thaddeus 1987).

Classes of Chemical Reactions

Type	Process	Rate Coefficient
Formation Processes		
Radiative association	$X + Y \rightarrow XY + h\nu$	10^{-16} – 10^{-9}
Grain surface formation	$X + Y:g \rightarrow XY + g$	$\sim 10^{-18}$
Destruction Processes		
Photodissociation	$XY + h\nu \rightarrow X + Y$	$\sim 10^{-10}$ – 10^{-8} s^{-1}
Dissociative recombination	$XY^+ + e \rightarrow X + Y$	$\sim 10^{-6}$
Collisional dissociation	$XY + M \rightarrow X + Y + M$	—
Chemical Processes		
Ion-molecule exchange	$X^+ + YZ \rightarrow XY^+ + Z$	$\sim 10^{-9}$
Charge-transfer	$X^+ + YZ \rightarrow X + YZ^+$	$\sim 10^{-9}$
Neutral-neutral	$X + YZ \rightarrow XY + Z$	$\sim 10^{-12}$

^a Approximate rate coefficients appropriate for cold dark clouds. All rate coefficients are sensitive to temperature. For photodissociation, the rates in s^{-1} in the unattenuated interstellar radiation field are listed.

Note: minimum two compounds on each side of the reaction equation!

Build-up of complex molecules in dense molecular clouds:

- In dense molecular clouds the only available energy to activate molecules comes from cosmic rays
- Cosmic rays penetrate into molecular clouds up to column densities of 10^{24} cm^{-2} .
- Cosmic rays ionize He and H_2 at rates 10^{-17} to 10^{-16} s^{-1} .
- H_3^+ is formed: $\text{H}_2 + \text{H}_2^+ \rightarrow \text{H}_3^+ + \text{H}$ or $\text{H}_2 + \text{He}^+ \rightarrow \text{H}_3^+ + \text{H} + \text{He}$.

H_3^+ is an interesting “floppy” ring molecule. It has transitions in the L and K bands. It was first discovered on Jupiter, and in the 90th was finally discovered in the interstellar medium.

H_3^+ is the key to molecule formation in dark clouds.

Reactions with O.

→ exothermal

Similar reactions are possible with C. (next slide)

N reactions must proceed in a different way as $N + H_3^+ \rightarrow NH^+ + H_2$ is endothermic. N^+ must be formed first.

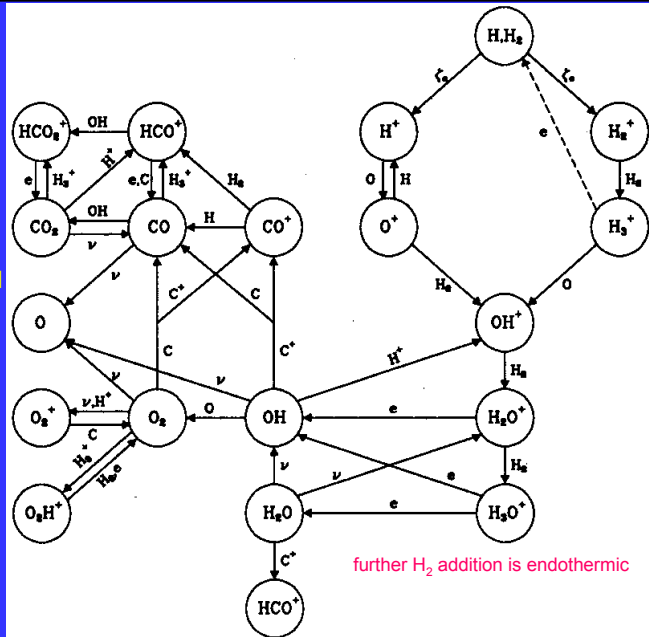
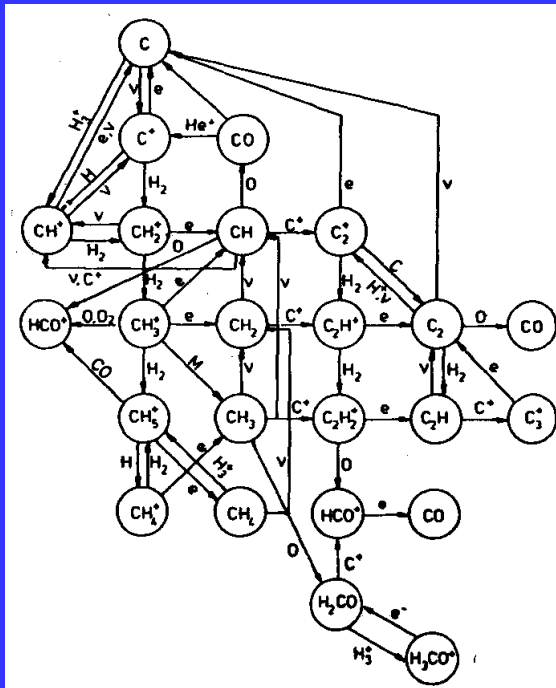
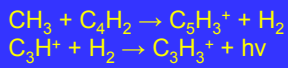


Figure A1. The most important interstellar chemical reactions involving oxygen-bearing molecules (figure from van Dishoeck 1988a).

Reactions with C



Van Dishoek E.F. et al., in Levy and Lunine eds. "Protostars and Planets III",
U. of Az. Press, 1993.

TABLE III
Identified Interstellar and Circumstellar Molecules^a

Species	Name	Species	Name	Species	Name
H ₂	molecular hydrogen	C ₂ H ₂	acetylene	C ₆ H	
C ₂	diatomic carbon	C ₃ H	propynylidyne (<i>l</i> and <i>c</i>)	CH ₂ CHCN	vinyl cyanide
CH	methylidyne	H ₂ CO	formaldehyde	CH ₃ C ₂ H	methylacetylene
CH ⁺	methylidyne ion	NH ₃	ammonia	CH ₃ CHO	acetaldehyde
CN	cyanogen	HNCO	isocyanic acid	CH ₃ NH ₂	methylamine
CO	carbon monoxide	HOCO ⁺	protonated carbon dioxide	HC ₃ N	cyanodiacetylene
CS	carbon monosulfide	HCNH ⁺	protonated hydrogen cyanide		
OH	hydroxyl	HNCS	isothiocyanic acid		
HCl	hydrogen chloride	C ₃ N	cianoethynyl	HCOOCH ₃	methyl formate
NO	nitric oxide	C ₃ O	tricarbon monoxide	CH ₃ C ₃ N	methylcyanoacetylene
NS	nitrogen sulfide	H ₂ CS	thioformaldehyde	CH ₃ C ₄ H	methyl diacetylene
SiC	silicon carbide*	H ₃ O ⁺	hydronium ion	CH ₃ CH ₃ O	dimethyl ether
SiO	silicon monoxide	C ₃ S		CH ₃ CH ₂ CN	ethyl cyanide
SiS	silicon sulfide	HC ₂ N		CH ₃ CH ₂ OH	ethanol
SO	sulfur monoxide			HC ₇ N	cyanohexatriyne
PN					
CP	*	C ₄ H	butadiynyl		
SO ⁺	sulfoxide ion	C ₃ H ₂	cyclopropenylidene	CH ₃ C ₄ CN	
NaCl	sodium chloride*	H ₂ CCC	propadienylidene	CH ₃ CH ₃ CO	acetone [†]
AlCl	aluminum chloride*	HCOOH	formic acid		
KCl	potassium chloride*	CH ₂ CO	ketene		
AlF	aluminum fluoride* [†]	HC ₃ N	cyanoacetylene	HC ₉ N	cyano-octa-tetra-yne
NH	nitrogen hydride	CH ₂ CN	cyanomethyl		

Table from previous slide continued

SiN	*	NH ₂ CN	cyanamide	HC ₁₁ N	cyano-deca-penta-yne
H ₂ D ⁺	†	CH ₂ NH	methanimine	CH ₄	methane
C ₂ H	ethynyl			SiH ₄	silane*
CH ₂	methylene [†]			C ₄ Si	*
HCN	hydrogen cyanide			C ₅	pentatomic carbon*
HNC	hydrogen isocyanide	C ₃ H	pentynylidyne	HCCNC	isocyanacetylene
HCO	formyl	C ₂ H ₄	ethylene*		
HCO ⁺	formyl ion	H ₂ CCCC	butatrienylidene		
HOC ⁺	isoformyl ion [†]	CH ₃ OH	methanol		
N ₂ H ⁺	protonated nitrogen	CH ₃ CN	methyl cyanide		
HNO	nitroxyl	CH ₃ CN	methyl isocyanide		
H ₂ O	water	CH ₃ SH	methyl mercaptan		
HCS ⁺	thioformyl ion	NH ₂ CHO	formamide		
H ₂ S	hydrogen sulfide	HC ₃ HO	propynal		
OCS	carbonyl sulfide				
SO ₂	sulfur dioxide				
SiC ₂	silicon dicarbide*				
C ₂ O	dicarbon monoxide				
C ₃	triatomic carbon*				
C ₂ S					

^a As of July 1992. Reported but doubtful, unconfirmed, or rejected: CO⁺, CS⁺, NaOH, NH₂CH₂COOH, CH₂CH₂O.

* Detected in circumstellar envelopes only.

† Tentative.

Interstellar chemistry: Photodissociation regions

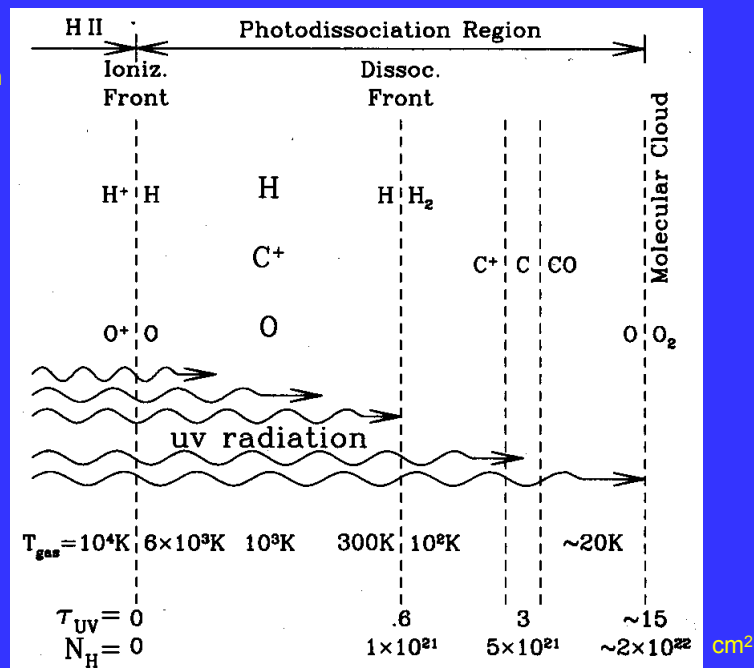
UV radiation of mass-rich, early-type stars evaporates grains and dissociates molecules.

The "elephant trunks" hide condensations of newly forming stars. These clouds are denser and therefore resist the evaporation and dissociation longer.



Schema of a photodissociation region

Lequeux J.,
"The interstellar medium",
Springer 2005



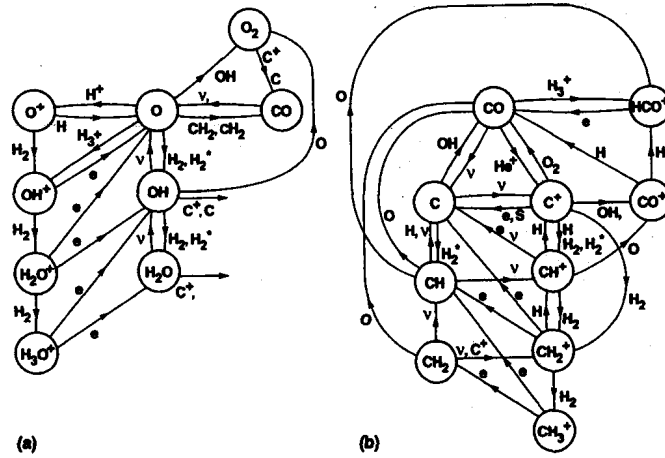
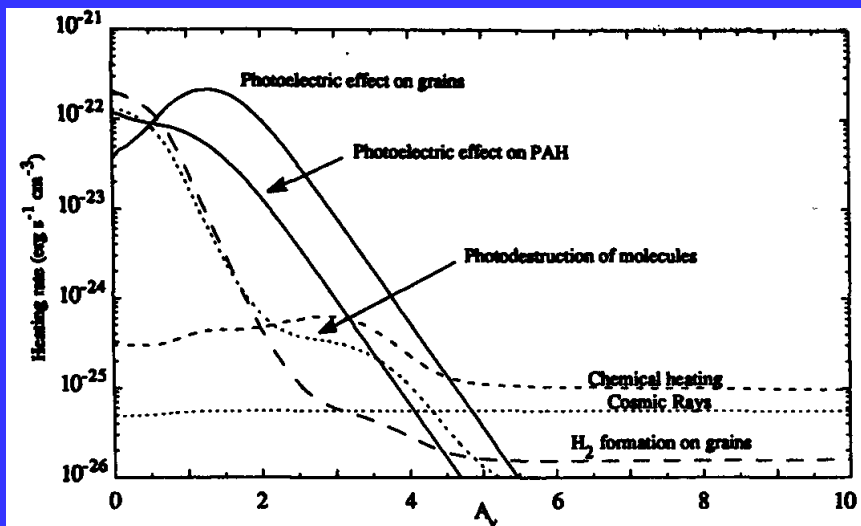


Fig. 10.2. The most important chemical reactions in photodissociation regions: (a) carbon chemistry; (b) oxygen chemistry. Compare to Figs. 9.2 and 9.3. Reproduced from Sternberg & Dalgarno [495], with the permission of the AAS.



A_v : visual extinction in magnitudes

Cloud collapse:

Force balance: pressure and centrifugal force versus gravitation.

Virial theorem: Multiply the equation of motion with the radius vector.
"Virial" = torque = Drehmoment
see J. Lequeux "The interstellar medium", Springer 2003, Chap. 14.

In the absence of external pressure $E_{\text{Grav}} = -2E_{\text{Kin}}$

Jeans mass M_J :

$$M_J \approx \left(\frac{kT}{G\mu_a m_{\text{amu}}} \right)^{3/2} \frac{1}{\sqrt{\rho}}$$

The less dense the object is the more massive it must be to collapse.

Examples: galaxies, star clusters, stars, planets.

The cooler the object the easier it collapses.

$n > 10^{11} \text{ g cm}^{-3}$ and $T=10\text{K}$ needed to form a Jupiter size planet. This density is much larger than that observed in interstellar clouds .

Gravitational collapse may be triggered by supernova explosion or a galactic density wave.

Galaxy NGC 1097

observed with 8.2 m
Melipal Unit telescope of
the VLT, ESO.

Note the bright regions of
young stars and the dust
lanes along the spiral
arms of the galaxy.



Collapse of molecular cloud cores and star formation

Free fall time scale: $t_{ff} = \left(\frac{3\pi}{32G\rho} \right)^{1/2}$ For the Sun it is about 30 minutes.

Clumps are densest near their centers, collapse is inside-out.
 Angular momentum conservation leads to spin-up of the cloud, may cause the collapse to stop and to fragment the cloud. Therefore most often multiple stellar systems form.

Virtually all single stars and many multiple stars are surrounded by a flat disk during formation. The mass collects in the central star and the angular momentum in the disk.

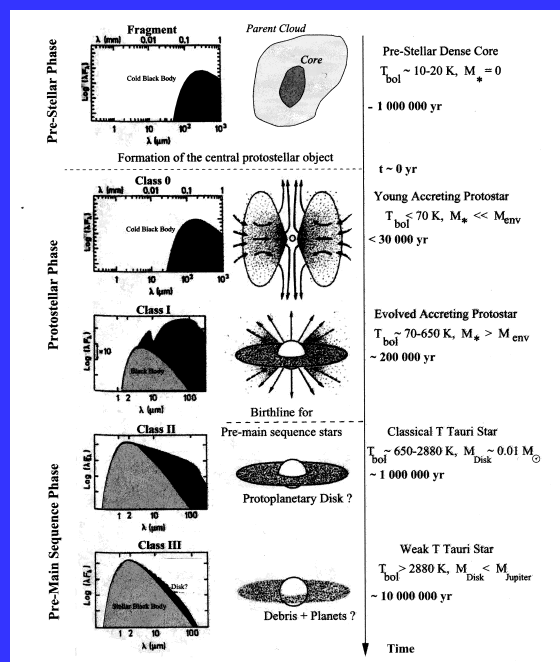
In solar system 99.8% of the mass is in the central star and 98% of the angular momentum is in planetary orbits.

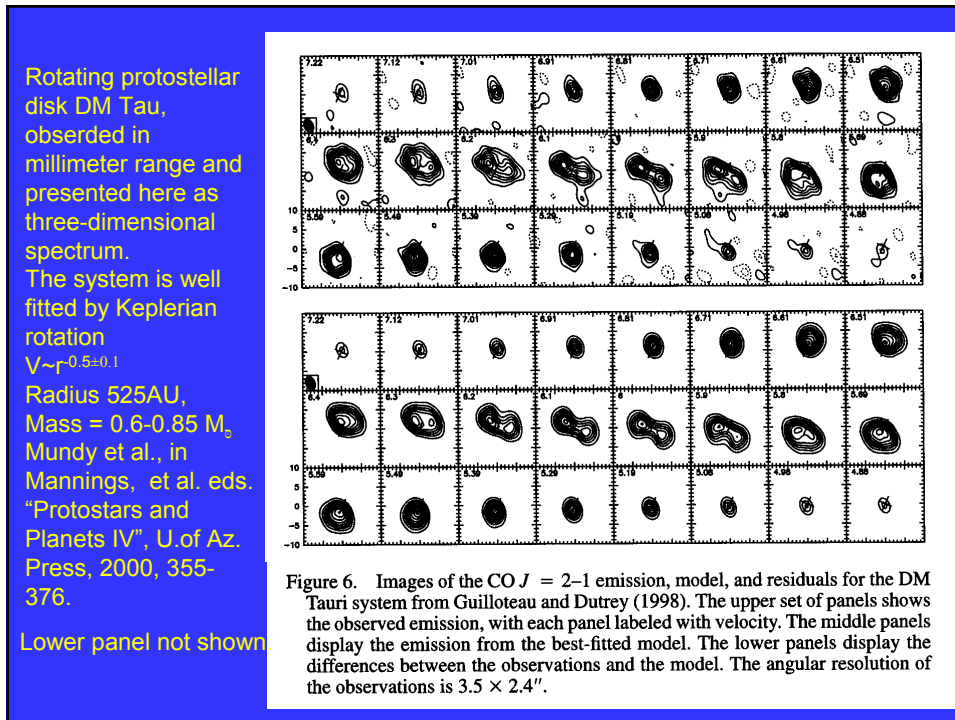
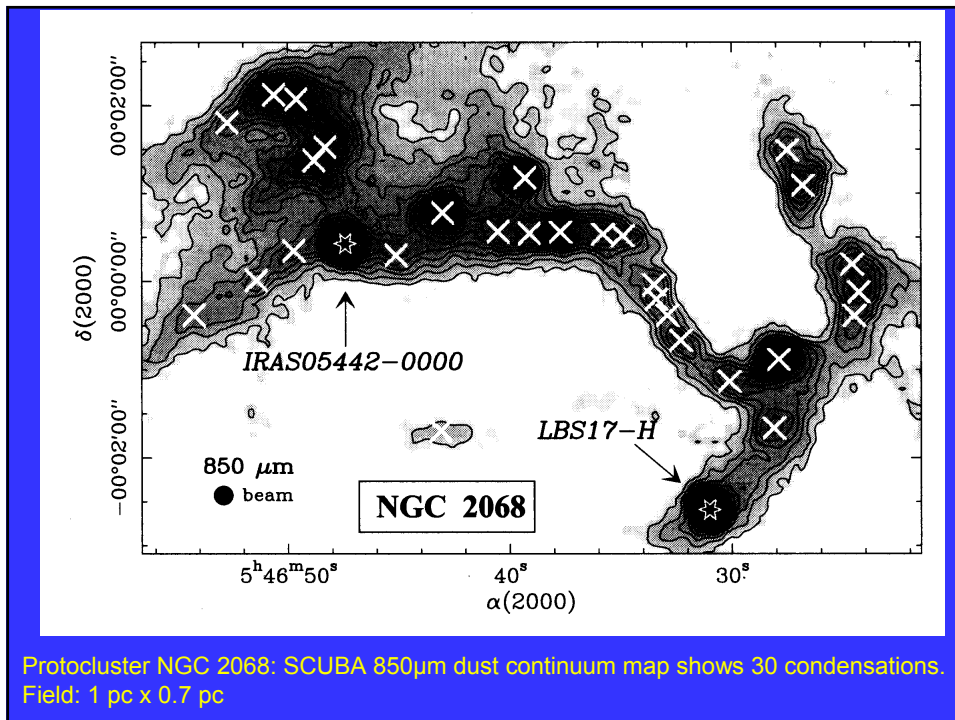
Temperature and density rise during collapse. Cloud becomes opaque, pressure builds up, D is burnt into He. When D is exhausted, star shrinks and heats further up, ^1H fusion starts.

Early phases of star formation can be observed in the microwave range, which presently is a very active part of research. Later the star becomes visible in the IR wavelength range.

Early phases of protostars

André, Ph.: "The initial conditions for protostellar collapse: Observational constraints", in Star formation and the physics of young stars, J Bouvier and J.-P. Zahn (eds.) EAS Publication Series, Vol 2., 2002

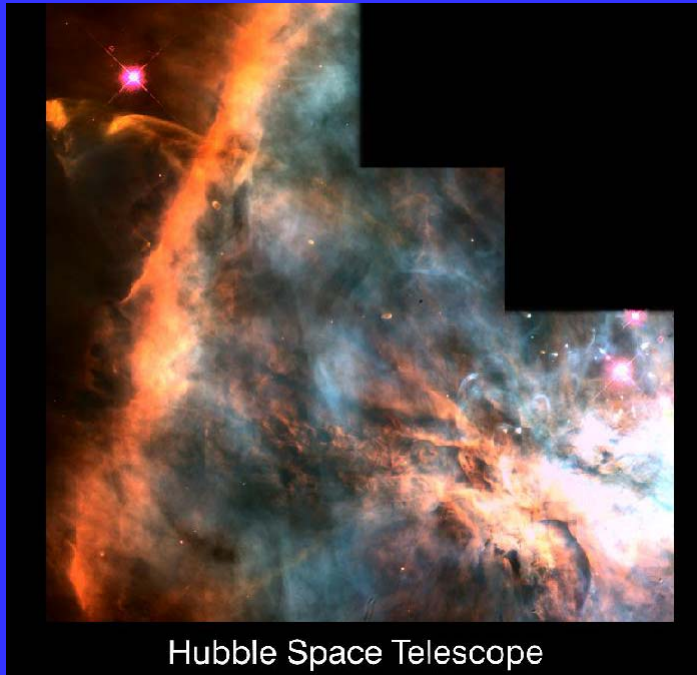




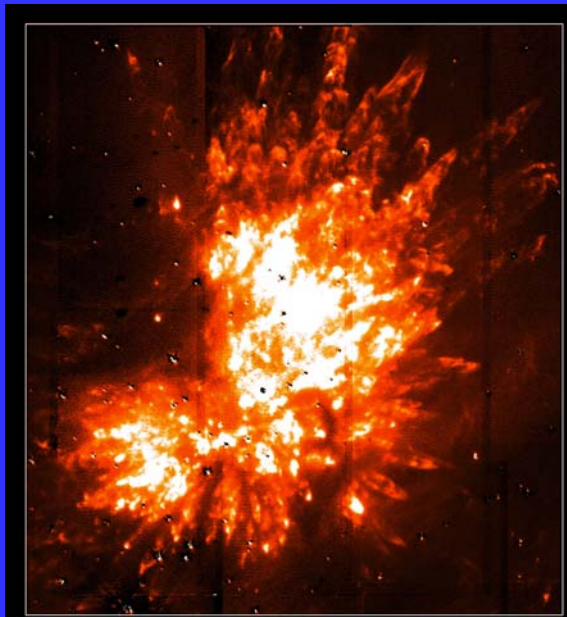
Orion Nebula

Note that HII region is *in front* of dark cloud!

see e.g. :
Herbest N.,
Marten M., The
New Astronomy,
Cambridge 1983



Hubble Space Telescope



Orion KL

Subaru Telescope, National Astronomical Observatory of Japan

CISCO (H α (v=1-0 S(1)) - Cont)

January 28, 1999

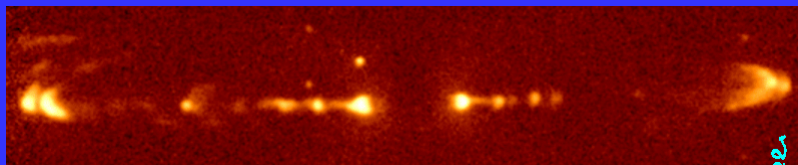
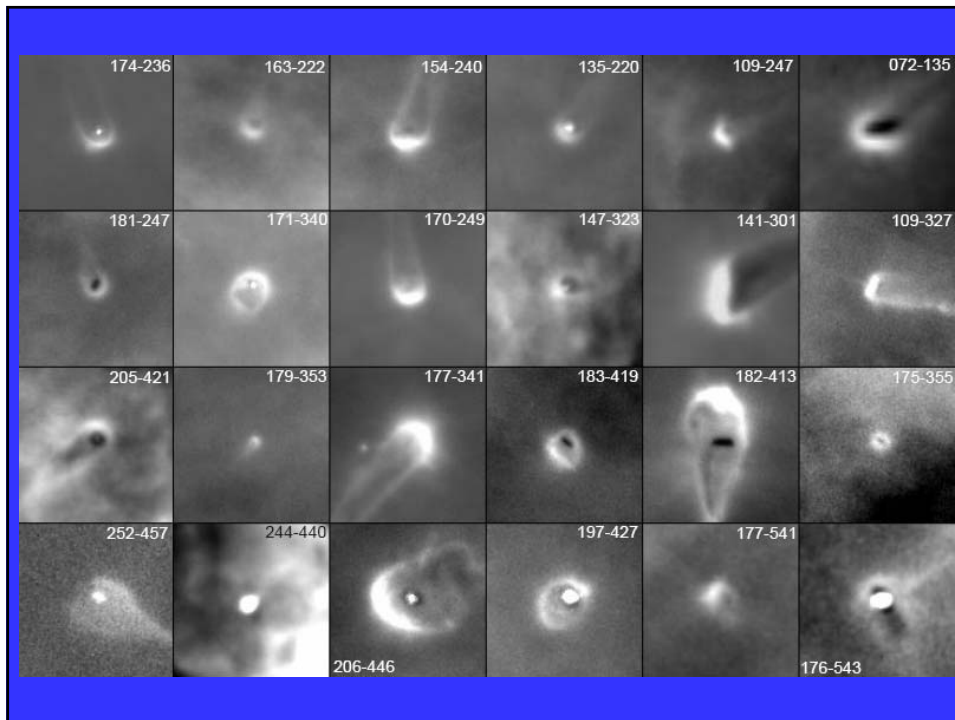
Emission-line composite image Continuum image
Orion 114-426
 500 AU McCaughrean & O'Dell 1996

Emission-line composite image Continuum image
Orion 183-405
 500 AU McCaughrean & O'Dell 1996

Hubble Space Telescope images of young circumstellar disks in the Orion Nebula. The lefthand panel of each image shows an emission-line composite, made by combining data from three narrow-band filters centred on bright emission lines from the nebula, namely [OIII] (blue), H α (green), and [NII] (red). The strong emission lines provide a bright background which reveals the circumstellar disks as silhouettes around their young stars. The righthand panel shows the corresponding continuum image taken through the medium bandwidth F547M filter. In these images, the central star shows up most clearly, and in the case of the edge-on disk, Orion 114-426, we also see faint reflection nebula above and below the plane of the silhouette disk.

Bally J., O'Dell C.R., McCaughrean M.J., 2000
 Disks, microjets, windblown bubbles, and outflows in the Orion Nebula,
 A.J. 119, 2919-2959

172-028 167-231 163-026 132-1832 121-1925
 239-334 218-354 191-232 182-332 165-254
 294-606 218-529 203-506 183-405 114-426



High-resolution deeper false-colour ($v=1-0$ S(1) line of molecular hydrogen at 2.122 microns) near-infrared image of the central knots and bowshocks in HH212. Continuum emission has not been subtracted. Data taken in November 1994 using the 256x256 pixel MAGIC infrared camera on the Calar Alto 3.5-m telescope in Spain. Field-of-view is approximately 55x85 arcsec, with the field rotated roughly 24 degrees west of north.

Credit: Mark McCaughrean (Astrophysikalisches Institut Potsdam), Hans Zinnecker (Astrophysikalisches Institut Potsdam), and John Rayner (University of Hawaii)

Star formation:

"Fundamental Astronomy", Karttunen H. et al. eds., Springer 1987

Time scales again:

Thermal time scale:

$$t_t \approx \frac{0.5 GM^2/R}{L} \approx \frac{(M/M_\odot)^2}{(R/R_\odot)(L/L_\odot)} \times 2 \times 10^7 \text{ y},$$

Dynamical (free fall) time scale

$$t_d = \frac{2\pi}{2} \sqrt{\frac{(R/2)^3}{GM}} \approx \sqrt{\frac{R^3}{GM}}.$$

Early evolution of a collapsing star:

in free-fall time

H_2 , H, H^+ (10^4 K), He^+ (10^5 K).
Radius shrinks from 100 AU to 1/4AU.
Star is convective in its center.

Hayashi track: Location of fully convective stars in the HR diagram.

Further evolution on thermal time scale.

Star continues to contract, motion is downward. Then, as the energy input changes from gravitational to nuclear energy, the convective regime is steadily transferred into a radiative one, the stellar surface becomes hotter and its luminosity increases.

12.2 The Contraction of Stars Towards the Main Sequence

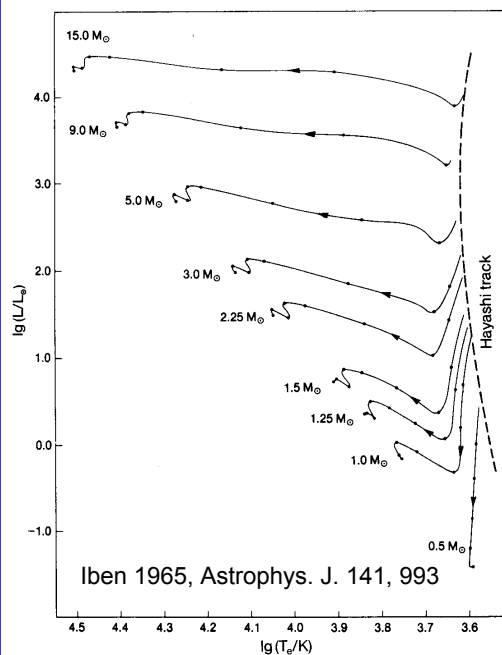
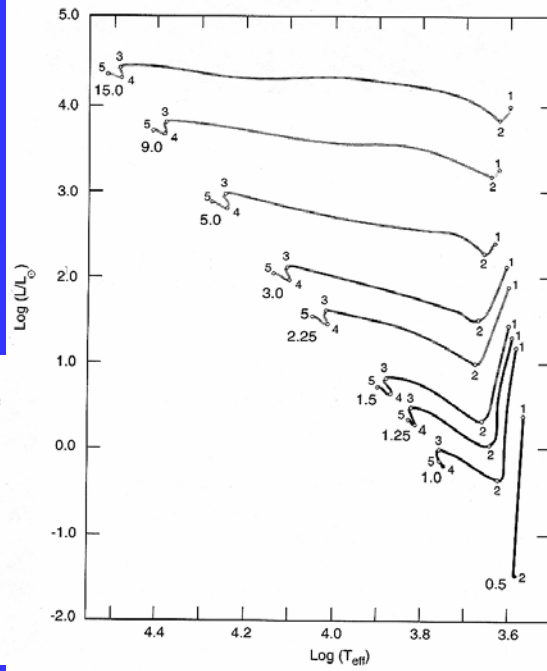


Table 8.1 Evolutionary lifetimes (years)

M/M_{\odot}	1-2	2-3	3-4	4-5
15	6.7(2)	2.6(4)	1.3(4)	6.0(3)
9	1.4(3)	7.8(4)	2.3(4)	1.8(4)
5	2.9(4)	2.8(5)	7.4(4)	6.8(4)
3	2.1(5)	1.0(6)	2.2(5)	2.8(5)
2.25	5.9(5)	2.2(6)	5.0(5)	6.7(5)
1.5	2.4(6)	6.3(6)	1.8(6)	3.0(6)
1.25	4.0(6)	1.0(7)	3.5(6)	1.0(7)
1.0	8.9(6)	1.6(7)	8.9(6)	1.6(7)
0.5	1.6(8)			

Note: powers of 10 are given in parentheses.



Early evolution of a collapsing star (continued):

A star of 15 solar masses condenses to the main sequence in 60000 years, for a star with 0.1 solar masses the process takes hundreds of millions of years.

Very young stars (T Tauri stars) difficult to observe as they are enshrouded into dense clouds.

T Tauri stars have high Lithium content (central temperature not yet high enough to destroy Lithium).

Bonnor-Ebert-Sphere:

Equilibrium isothermal sphere of finite size with a fixed temperature and boundary pressure; such a configuration might be relevant to star formation if prestellar cloud cores when formed are nearly in equilibrium and in approximate pressure balance with a surrounding medium. For a fixed sound speed c and boundary pressure P , an isothermal sphere is unstable to collapse if its radius and mass exceed the critical values

$$R_{\text{BE}} = \frac{0.48 c^2}{G^{1/2} P^{1/2}}, \quad M_{\text{BE}} = \frac{1.18 c^4}{G^{3/2} P^{1/2}} \quad (\text{Bonnor-Ebert sphere}).$$

These results can be related to the Jeans length and mass discussed above by noting that in an isothermal medium the pressure and density are related by $P = \rho c^2$ (c is sound speed);

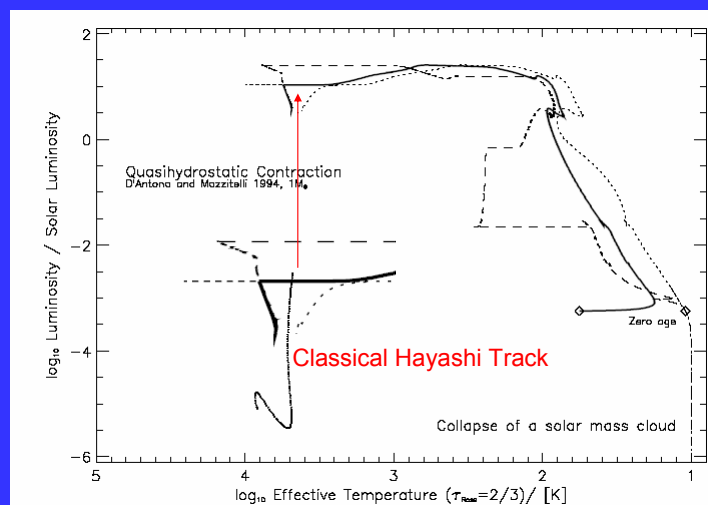
thus, R_{BE} and M_{BE} have the same dimensional form as the Jeans length and mass, but with smaller numerical coefficients that reflect the fact that a Bonnor-Ebert sphere contains only matter whose density is higher than the background density, while a region one Jeans length across also includes matter of lower density that may or may not collapse along with the denser material.

(R.B. Larson, The physics of star formation, Rep. Prog. Phys. 66, 1651-1697, 2003)

Calculation of collapse of "Bonnor-Ebert" sphere prior to reaching Hayashi-line by taking full account of supersonic compressible motion of the cloud gas, but assuming spherical symmetry and grey Eddington approximation.

Note that the initial star may be brighter as expected and therefore better observable.

r_T radius where
 $\tau_{\text{ROSS}} = 2/3$
 (photospheric
 radius)
 thick line:
 $L = 4\pi r_T^2 \sigma T_{\text{eff}}^4$,
 dashed line:
 $L = 4\pi r_T^2 \sigma T^4$,
 dotted line:
 T at r_T .



Wuchterl G., W.M. Tscharnuter, A&A 398, 1081-1090 (2003)

