

Earth is a terrestrial  
planet,

but not a typical one.

[ Anonymous ]

# 1. Seismology and internal structure

## 1.1 Fundamentals

Body waves  $\left\{ \begin{array}{l} \text{P-waves} \\ \text{S-waves} \end{array} \right.$

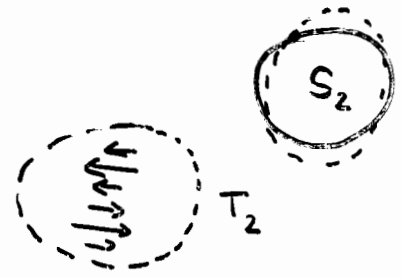
$$v_P = \sqrt{\frac{k + \frac{4}{3}\mu}{\rho}}$$

$$v_S = \sqrt{\frac{\mu}{\rho}}$$

$k$ : incompressibility     $\mu$ : shear modulus     $\rho$ : density

Surface waves  $\left\{ \begin{array}{l} \text{Rayleigh waves} \\ \text{Love waves} \end{array} \right.$     Dispersion  $v(\lambda)$ !

Free oscillations  $\left\{ \begin{array}{l} \text{spheroidal} \\ \text{toroidal} \end{array} \right.$



Earth: longest mode  ${}_0S_2$ : 54 min

Period depends on  $v_P(r)$ ,  $v_S(r)$ ,  $\rho(r)$ !

## 1.2 Body wave propagation in a spherically symmetric Earth

Continuous variation  $v_P(r)$ ,  $v_S(r)$

→ curved ray paths

At discontinuities: Refraction, Reflexion,  
Conversion (P → S, S → P)

Seismic phases

P, S, K: P-phase in core

PcP: ~~on~~ reflected from core

PPP: twice reflected at surface

- For radial symmetry, the travel time for a phase is only a function of epicentral distance!



- Evidence for core with reduced  $v_p$ : "Shadow zone" between  $\Delta = 103^\circ$  and  $\Delta = 142^\circ$
- No ~~S~~ S-waves in (outer) core  $\rightarrow$  liquid.
- Weak Pk1kP-arrivals in shadow zone  $\rightarrow$  inner core (solid)
- Knowledge of  $T(\Delta)$  allow determination of epicenter when 3 observations for an earthquake
- inversion of  $T(\Delta) \rightarrow v_p(r), v_s(r)$

### 1.3 Earth structure

Crust  $\left\{ \begin{array}{l} \text{Oceanic } 7 \text{ km} \quad \text{Basalt} \quad \text{Ca, Al-rich} \\ \text{Continental } \sim 35 \text{ km} \quad \text{(Granite)} \quad \text{SiO}_2\text{-rich} \end{array} \right.$

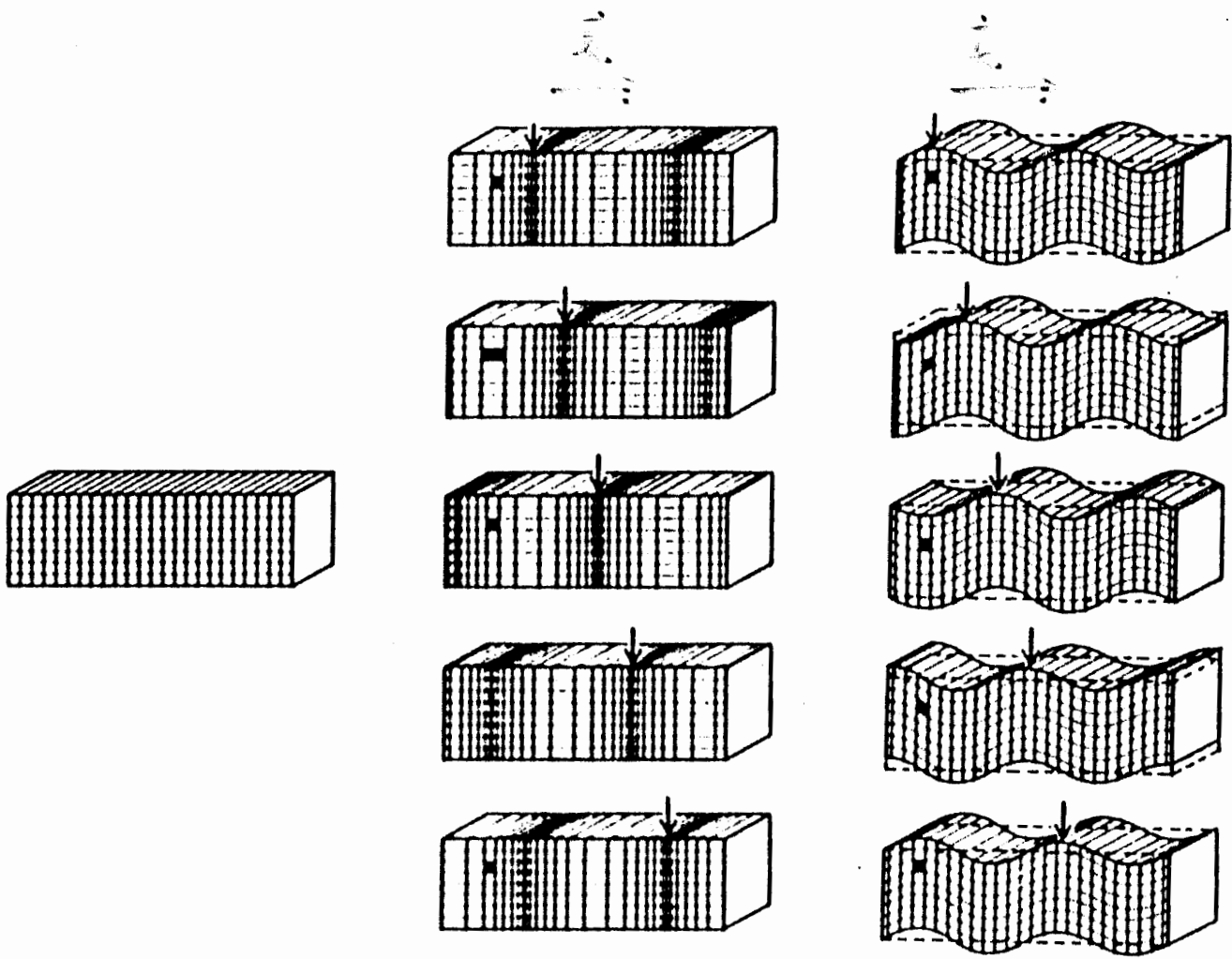
Mantle  $- 2890 \text{ km}$  Olivine  $(\text{Mg}_{0.9}\text{Fe}_{0.1})_2\text{SiO}_4$

Outer core  $r = 3480 \text{ km}$  Fe (+Ni + light element) Liquid

Inner core  $r = 1220 \text{ km}$  Fe (+...) solid

Mantle: weak discontinuities at 410, 660 km  
solid-solid phase transitions of olivine

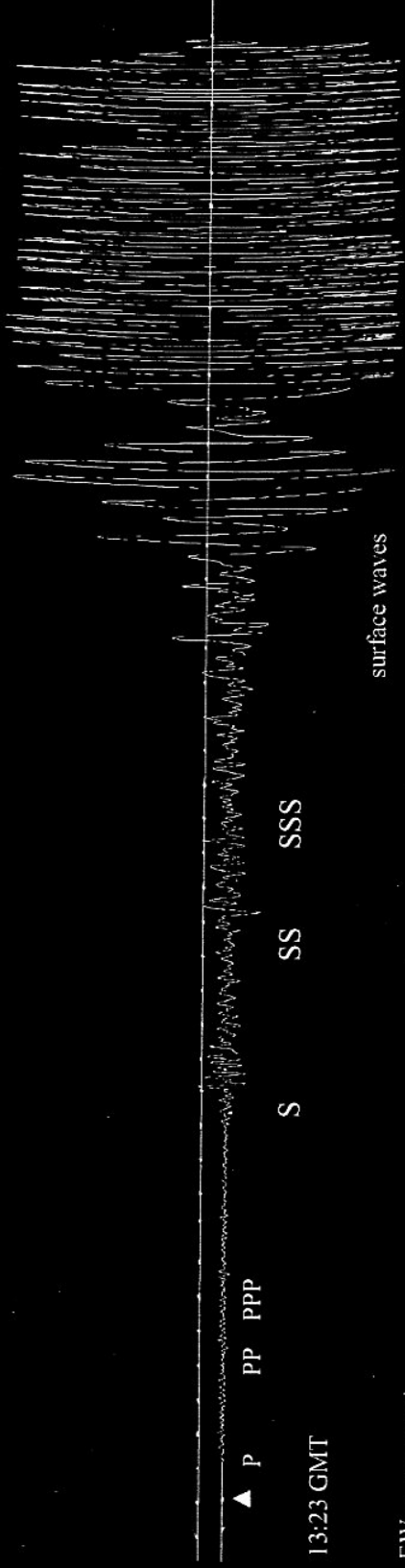
Density: not constrained by body waves  
 $\rightarrow$  free oscillations (+ gravity + rotation data)



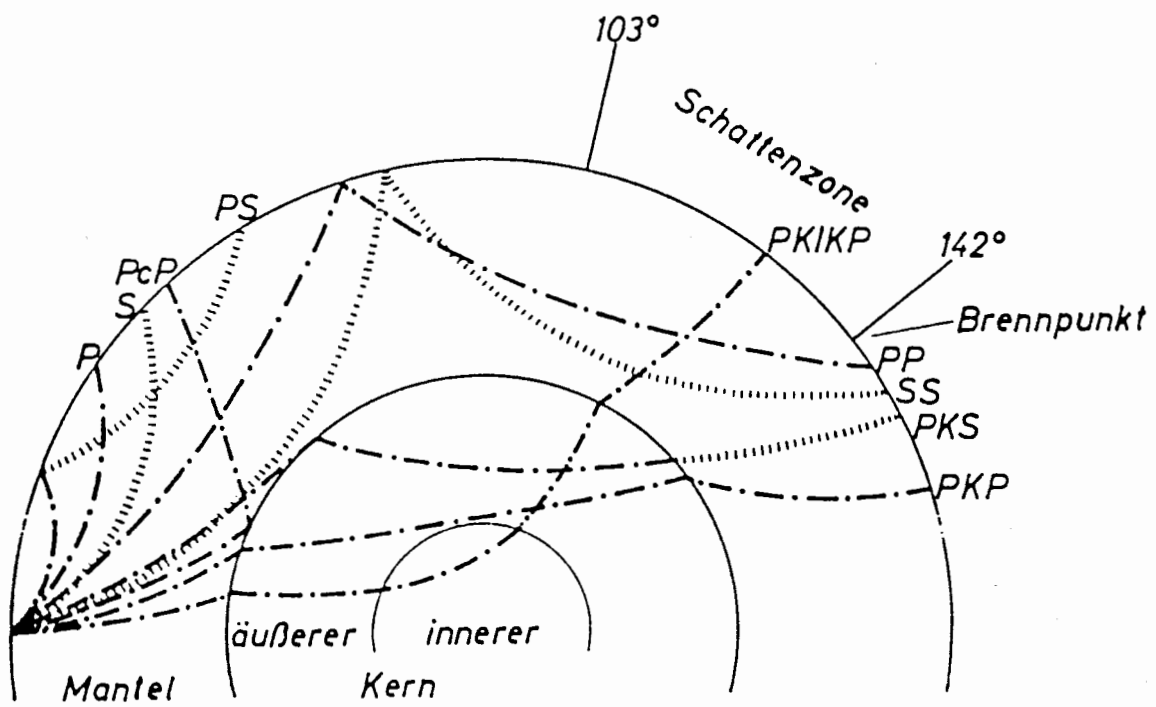
**San Francisco, 18. April 1906, 13:12 GMT  
37.7N, 122.5W**



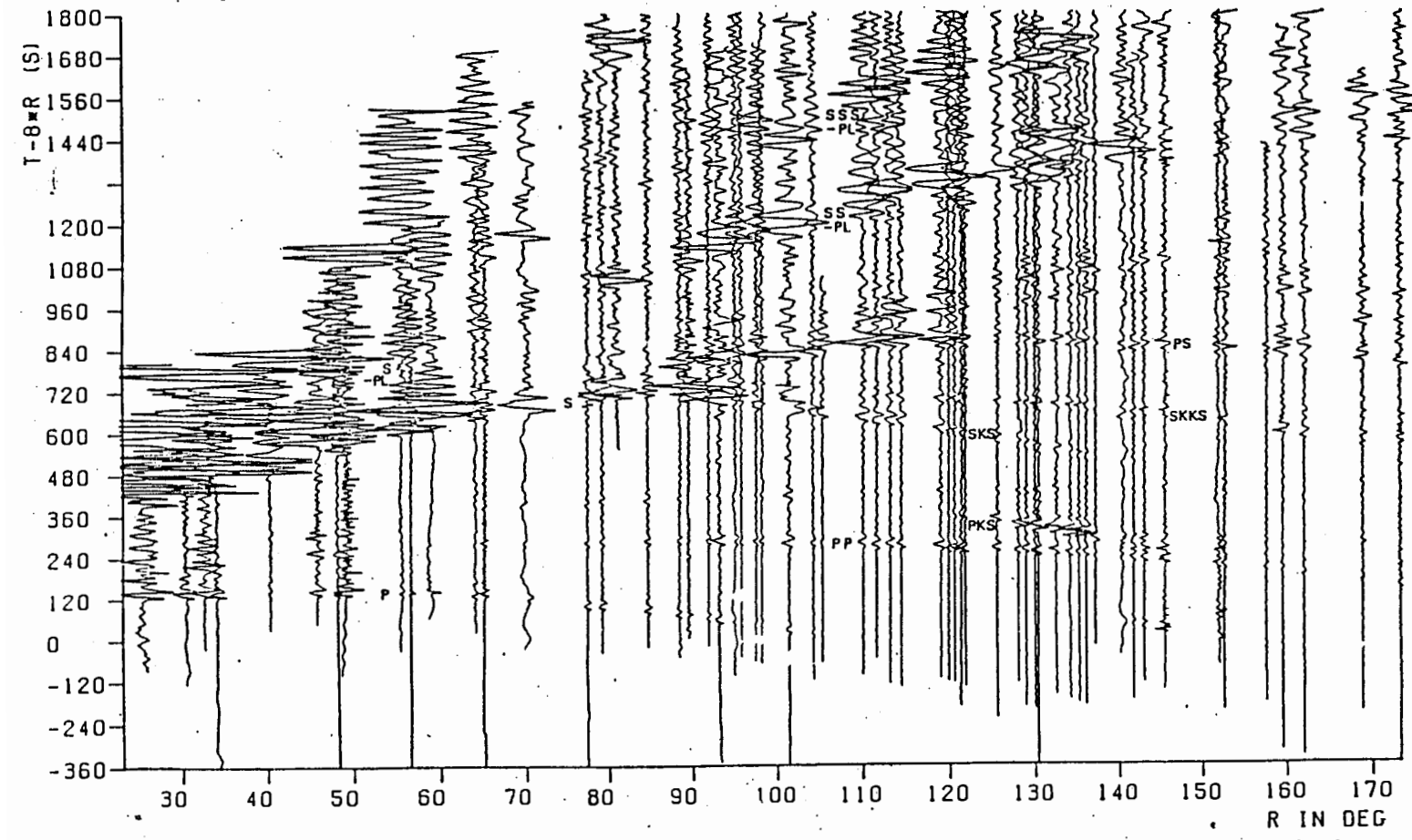
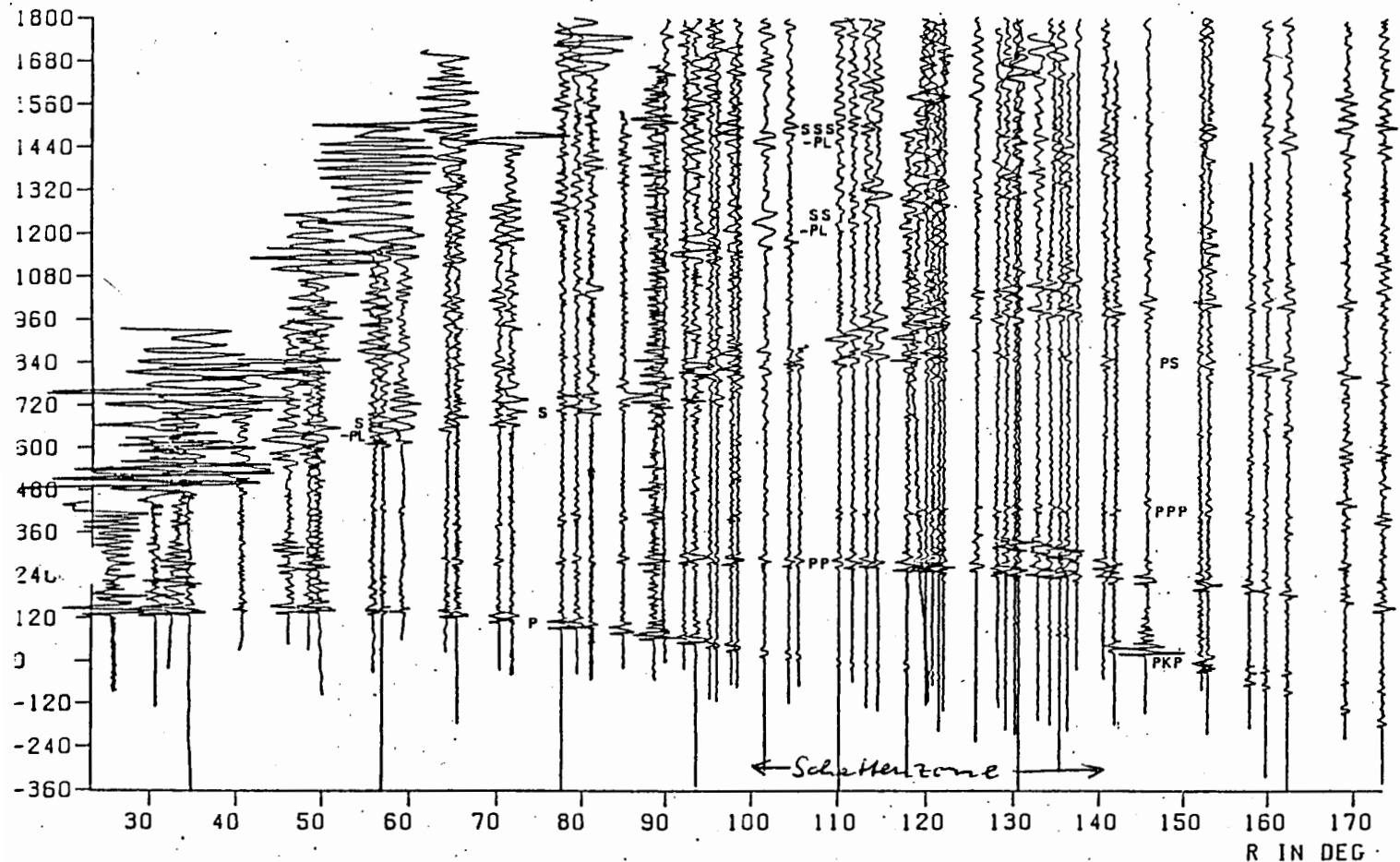
NS-component  
1200kg astatic seismograph, Göttingen



EW-component  
1200kg astatic seismograph, Göttingen

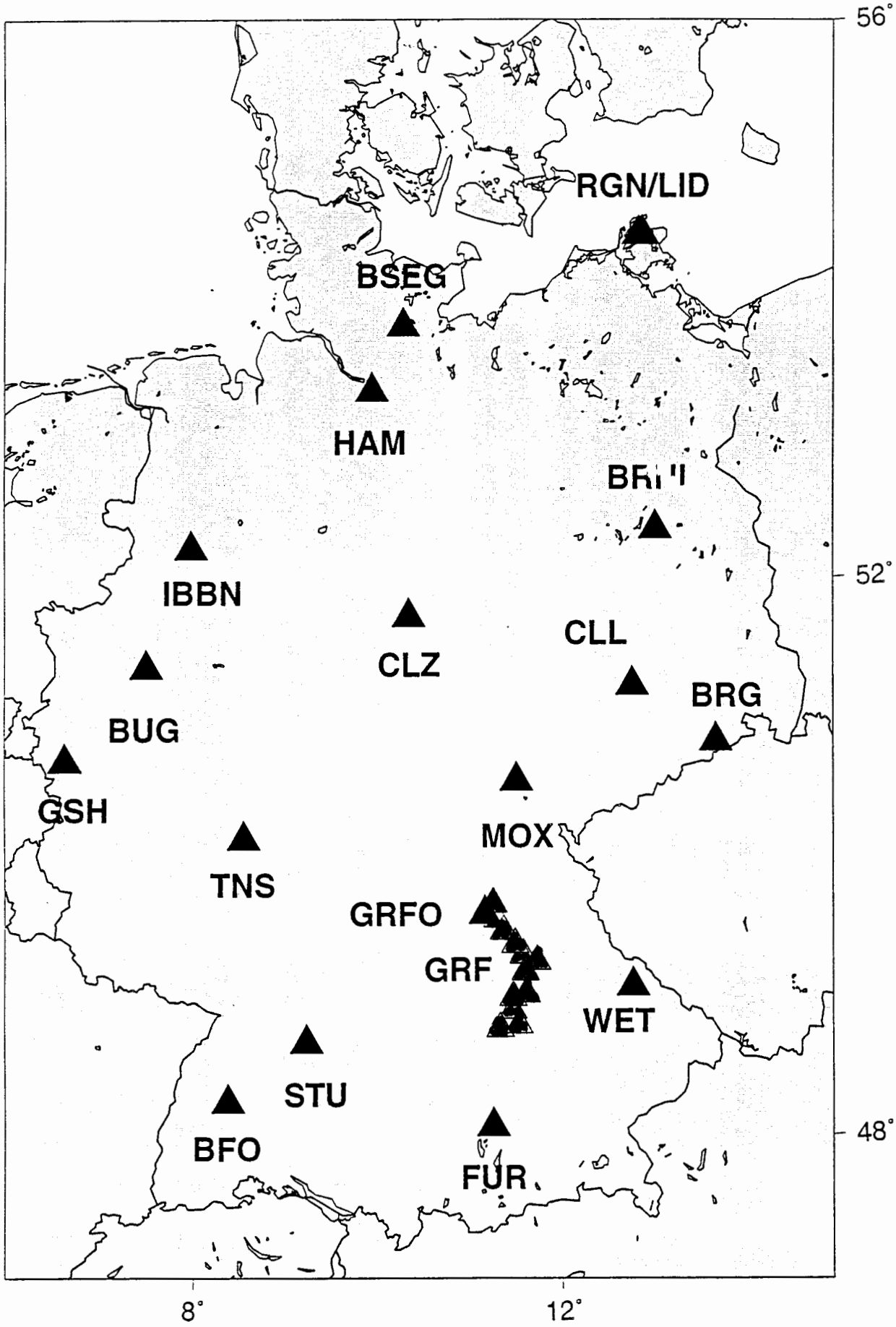


Seismische Raumwellenphasen:



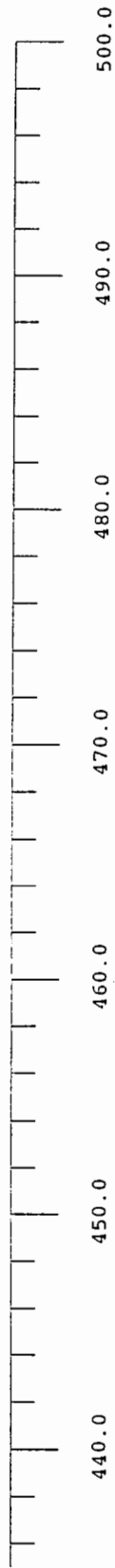
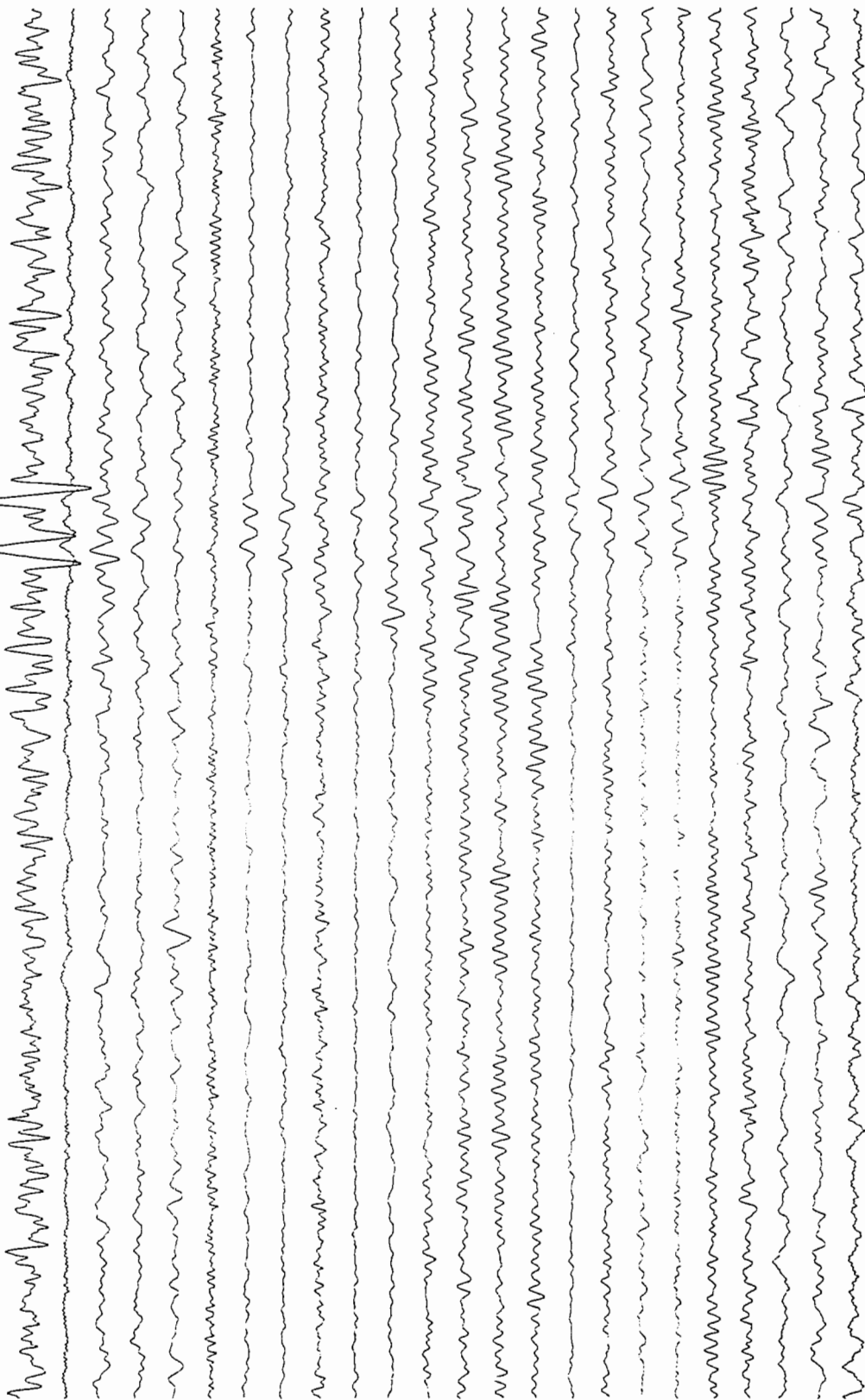
2. Radial component seismogram section of the same earthquake. Motion towards the epicentre to the left. Amplitude scale is the same as in Fig. 1.





PKIKP

- 24: SUM Z
- 23: WET Z
- 22: TNS Z
- 21: MOX Z
- 20: LID Z
- 19: FUR Z
- 18: CLZ Z
- 17: CLL Z
- 16: BUG Z
- 15: BRG Z
- 14: BFO Z
- 13: GRC4 Z
- 12: GRC3 Z
- 11: GRC2 Z
- 10: GRC1 Z
- 9: GRB5 Z
- 8: GRB4 Z
- 7: GRB3 Z
- 6: GRB2 Z
- 5: GRB1 Z
- 4: GRA4 Z
- 3: GRA3 Z
- 2: GRA2 Z
- 1: GRA1 Z



Neue Hebriden 15.4.1994  $m_b=5.3$  Herdentfernung  $138^\circ$

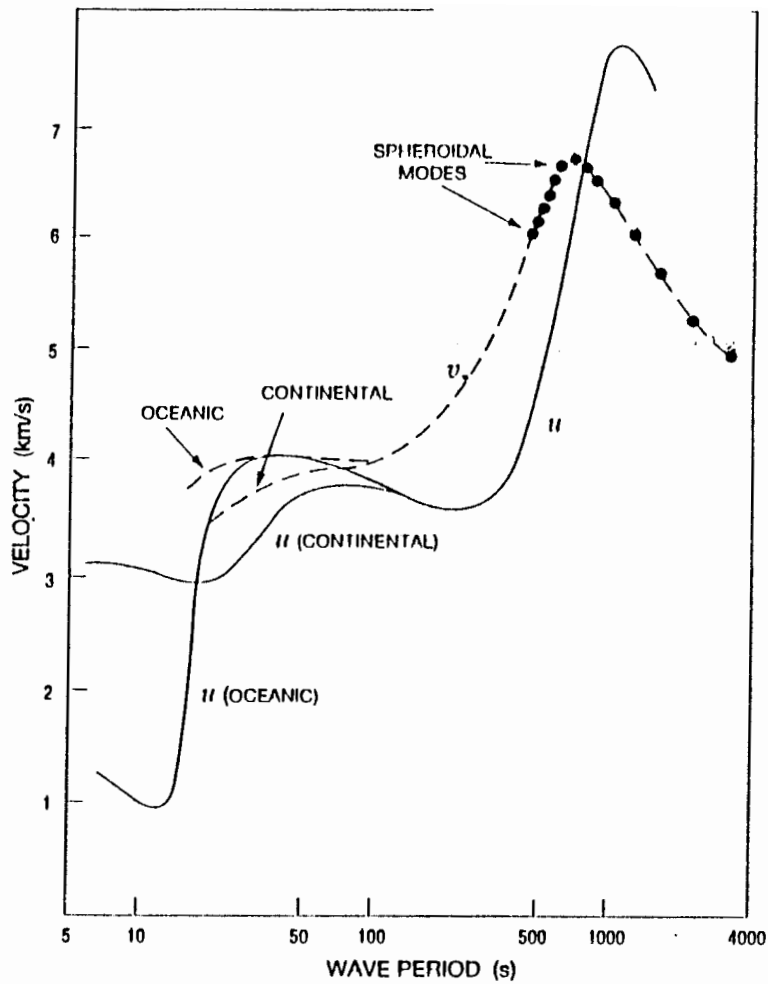


Figure 5.3(a). Fundamental mode Rayleigh wave dispersion. Group velocity,  $u$ , is shown by a solid line and inferred phase velocity,  $v$ , by a broken line, with the dispersion curve from free oscillation periods above 400s. Figure based on Oliver (1962).

23. Mai 1960

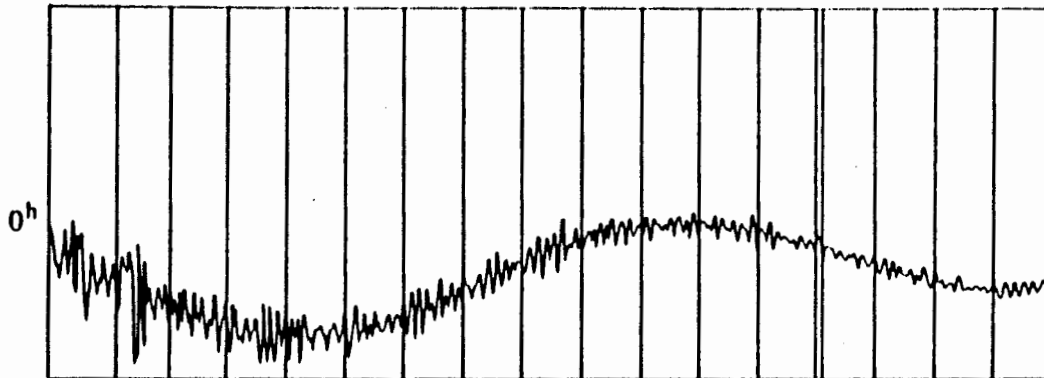


Abb. 5.45 Aufzeichnung des Ausschlagens der Erde nach dem großen Chile-Beben 1960. Die Schwingungen reiten auf der Gezeitenbewegung mit etwa halbtägiger Periodizität. Linienabstand 1 Stunde (nach Bolt 1982).

**Blatt 8:**

Oben: Dispersionskurven für Rayleighwellen.  $u$ : Gruppengeschwindigkeit,  $v$ : Phasengeschwindigkeit (Stacey)  
 Unten: Registrierung von Eigenschwingungen der Erde (Berckheimer)

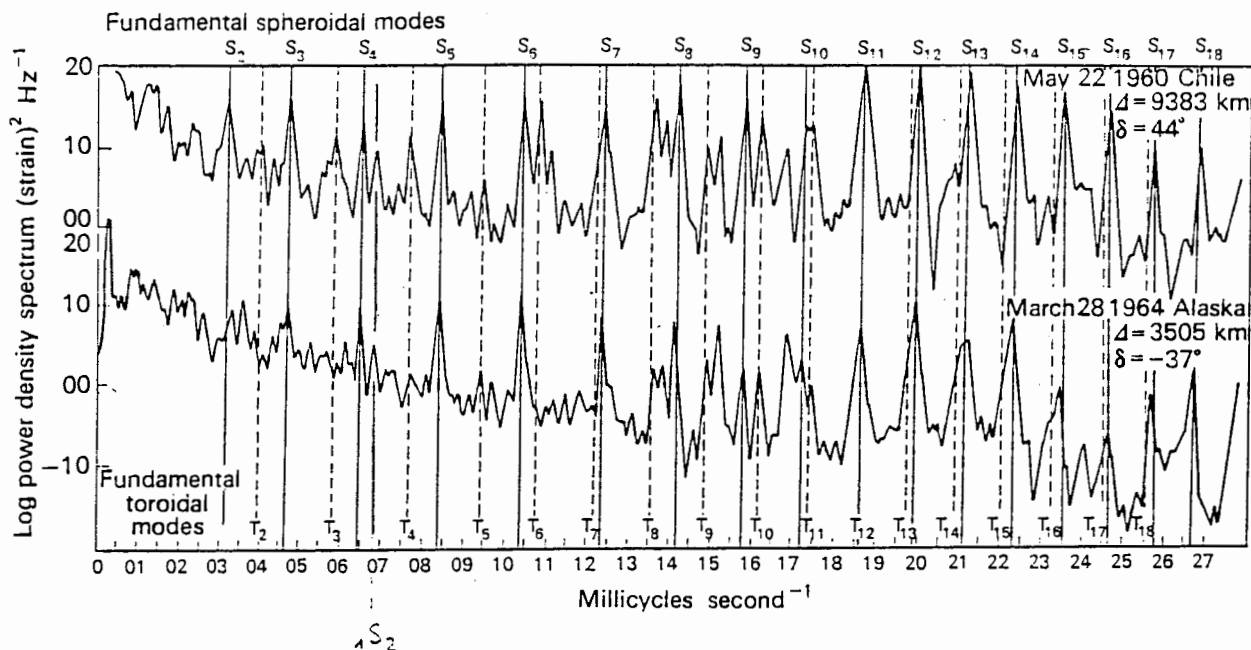


Fig. 4.9 Power spectral density of the Alaskan and Chilean earthquakes recorded on a strain seismometer at Isabella, California. The angle  $\delta$  is the deviation of the great circle path from the axis of the strain seismometer. Redrawn from SMITH (1966), *J. geophys. Res.*, 71, 1187.

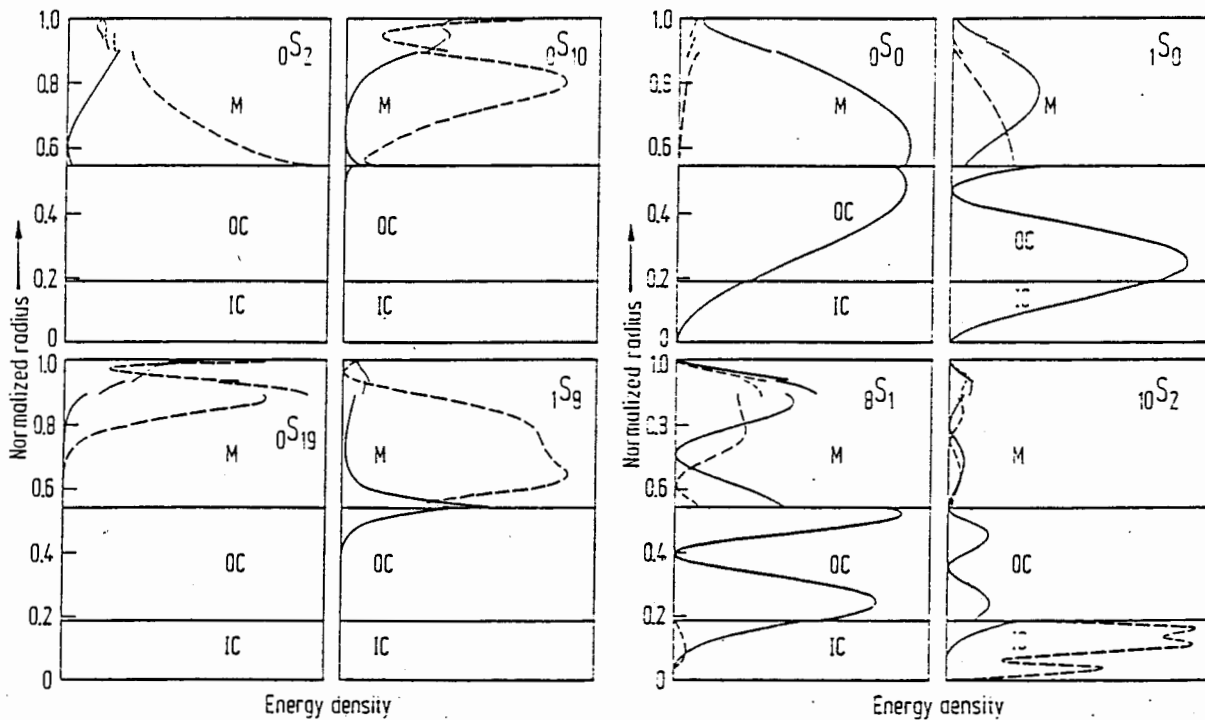
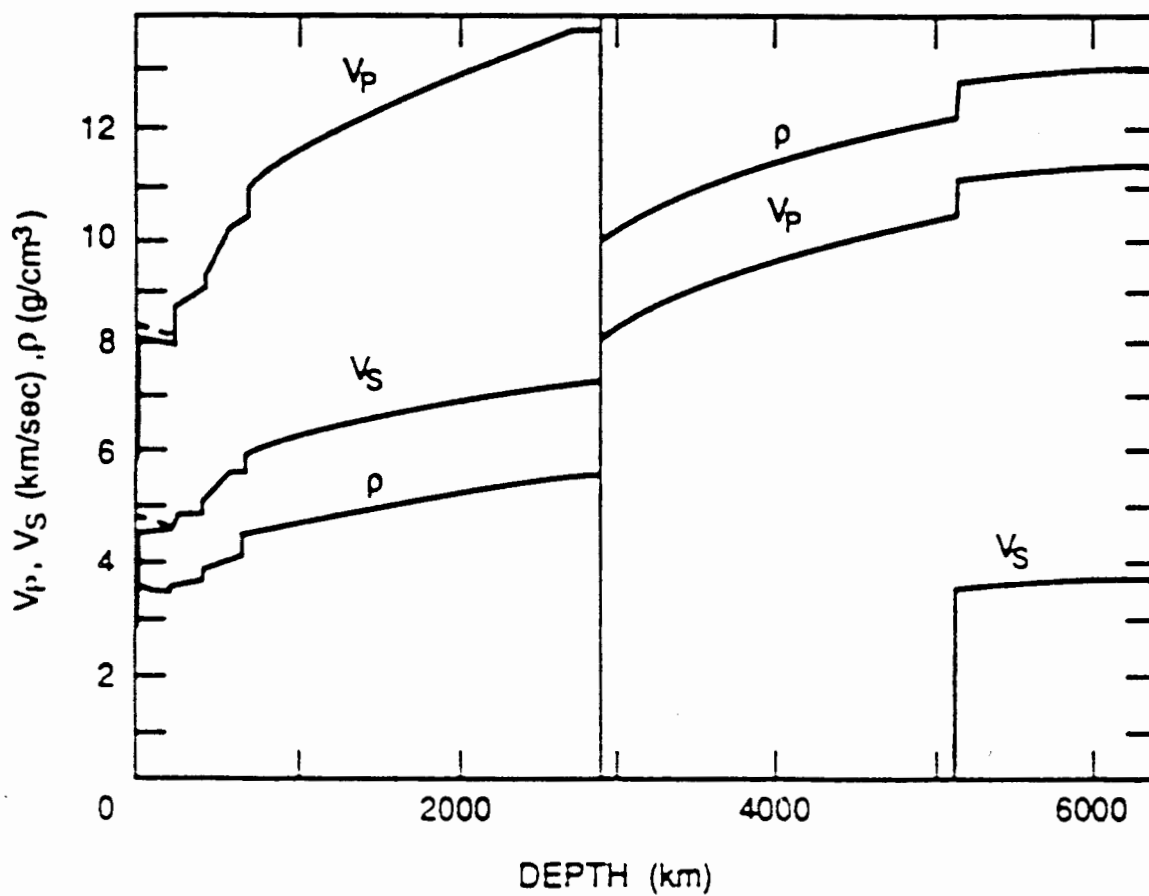


Fig. 15. Plots of compressional energy density (solid line) and shear energy density (broken line) as functions of normalized radius for modes  ${}_0S_2$ ,  ${}_0S_{10}$ ,  ${}_0S_{19}$ ,  ${}_1S_9$ ,  ${}_0S_0$ ,  ${}_1S_0$ ,  ${}_8S_1$  and  ${}_{10}S_2$  [80G]. The core-mantle boundary and the boundary between outer and inner core are indicated by solid horizontal lines. Energy densities are in relative units. (IC=inner core, OC=outer core, M=mantle.)

## 7 Earth models



7.2. PREM model: Seismic velocities and density profile (after Dziewonski and Anderson 1981).

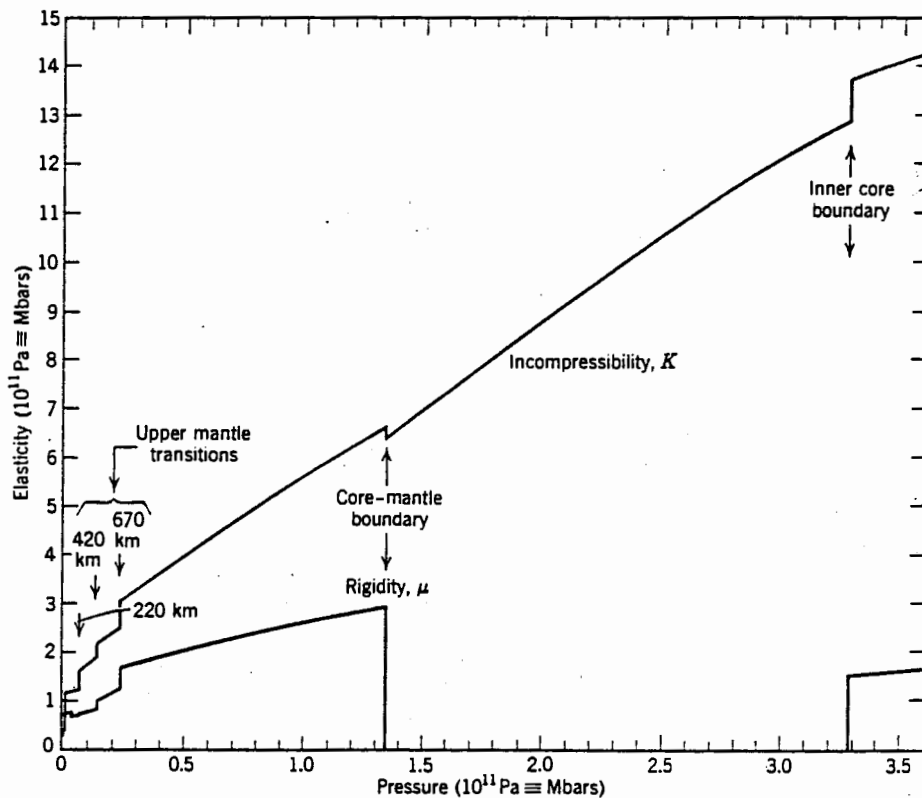
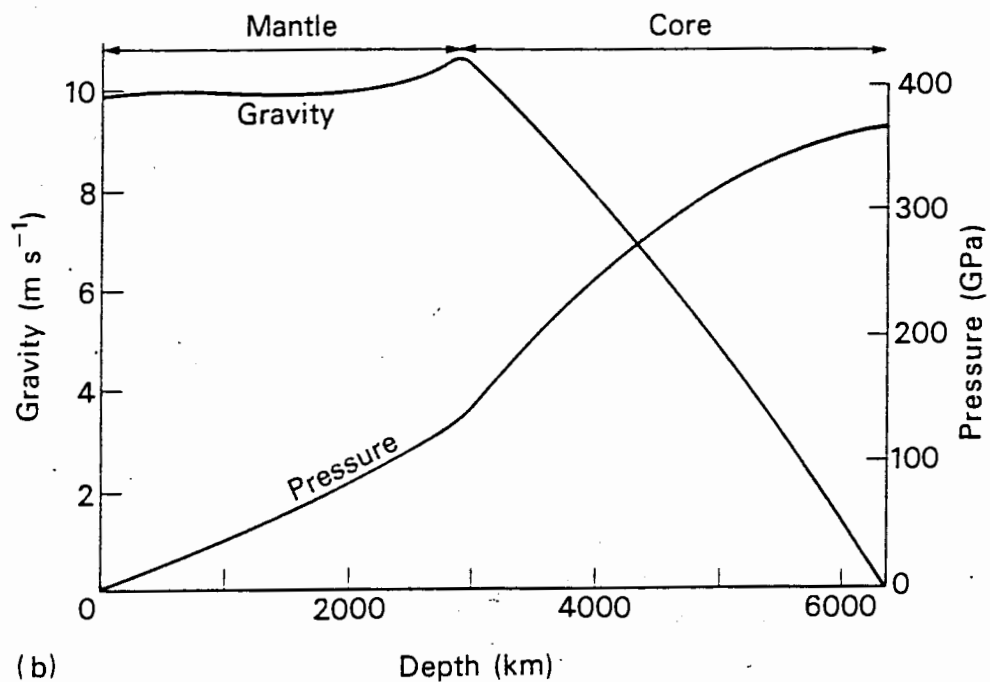
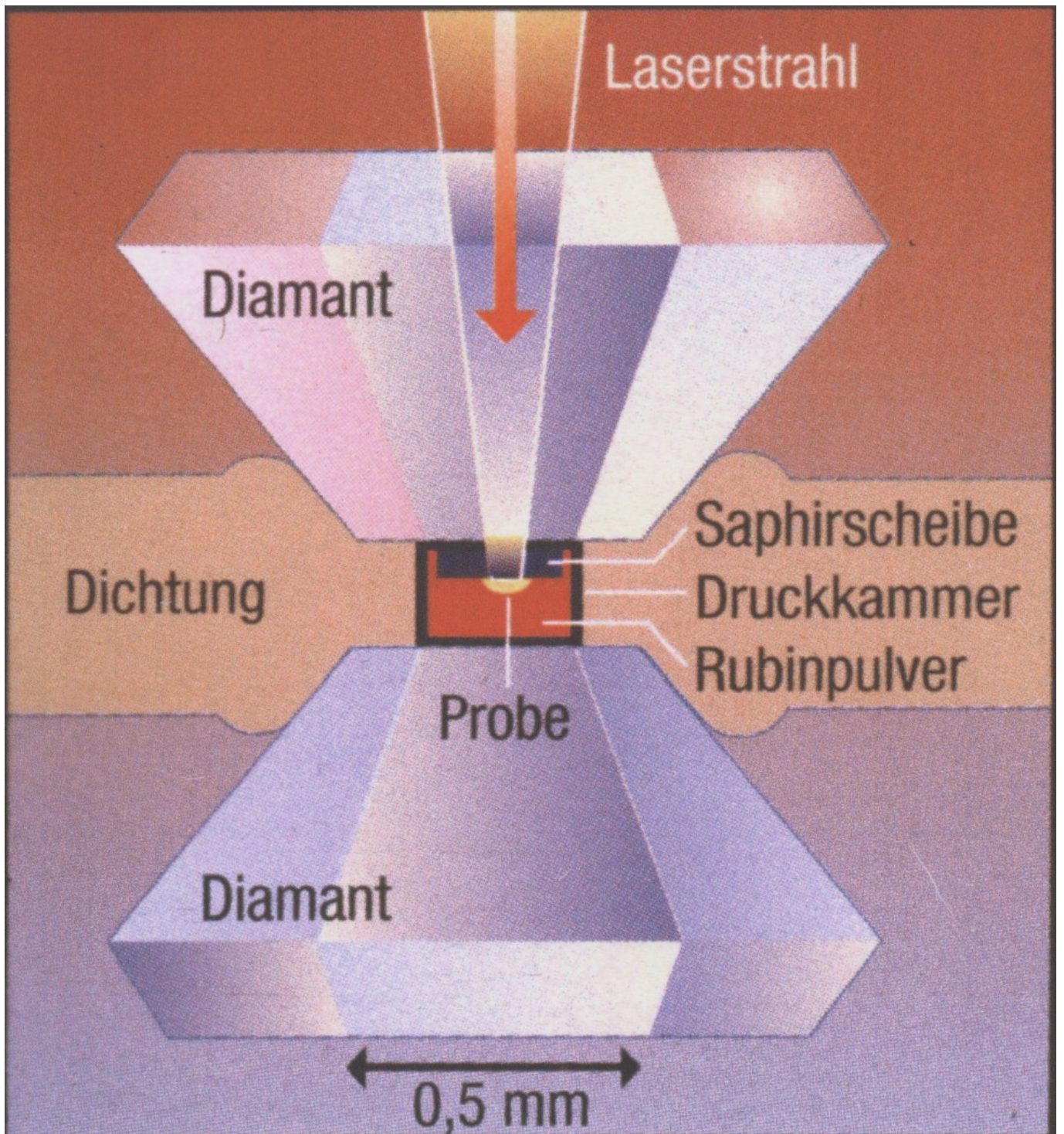


Figure 6.18. Variations of elastic constants with pressure in the interior of the Earth (model data by Dziewonski et al. 1975—Appendix G).

## Chemical composition of Earth components

|                                | Cont. Crust                                      | Oceanic Crust                      | Mantle  | Core                  |
|--------------------------------|--|------------------------------------|---|-----------------------|
| Thickness [km]                 | 35 – 40  | 6 -7                               | 2900  | 3500                  |
| Typical rock                   | Granit   | Basalt                             | Peridotite  | (Iron)                |
| Density [kg/m <sup>3</sup> ]   | 2700   | 2900                               | 3300  | 10,000                |
| Composition [wt.-%]            |  |                                    |   |                       |
| SiO <sub>2</sub>               | 67   | 52                                 | 45  | Fe: 85                |
| MgO                            | 2  | 10                                 | 39  | Ni: 5-10              |
| FeO                            | 4  | 10                                 | 9   | other                 |
| Al <sub>2</sub> O <sub>3</sub> | 16   | 14                                 | 3   | (O,S,Si,C,H...): 5-10 |
| CaO                            | 4  | 11                                 | 3   |                       |
| other                          | 7  | 3                                  | 1   |                       |
| Main minerals                  |  |                                    |   |                       |
|                                | Quartz: SiO <sub>2</sub>                         | Plagioclase                        | Olivine: (Mg,Fe) <sub>2</sub> SiO <sub>4</sub>                          |                       |
|                                | Plagioclase:                                     | Pyroxene:                          | Pyroxene  |                       |
|                                | CaAl <sub>2</sub> Si <sub>2</sub> O <sub>8</sub> | CaMgSi <sub>2</sub> O <sub>6</sub> | Garnet: Mg <sub>3</sub> Al <sub>2</sub> Si <sub>3</sub> O <sub>12</sub> |                       |
|                                | - NaAlSi <sub>3</sub> O <sub>8</sub>             | -(Mg,Fe)SiO <sub>3</sub>           |   |                       |





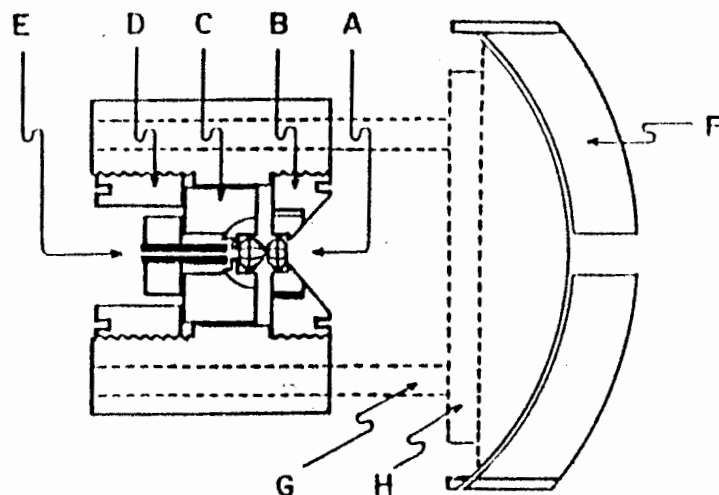


FIGURE 10-7

Cross section of diamond anvil press developed by Bassett et al., 1967. A—Diamond anvils; B—stationary piston; C—sliding piston; D—driver screw; E—collimator; F—film cassette; G—cassette mounting rods; H—cassette translating bars. (From Bassett et al., 1967; with permission.)

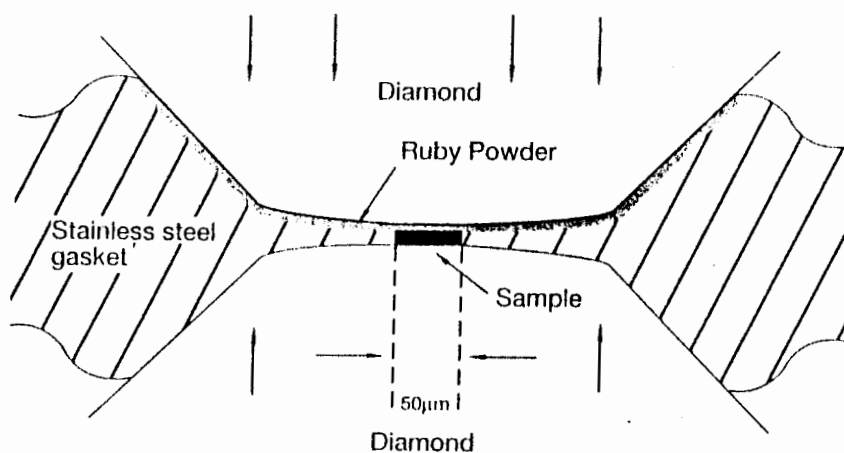


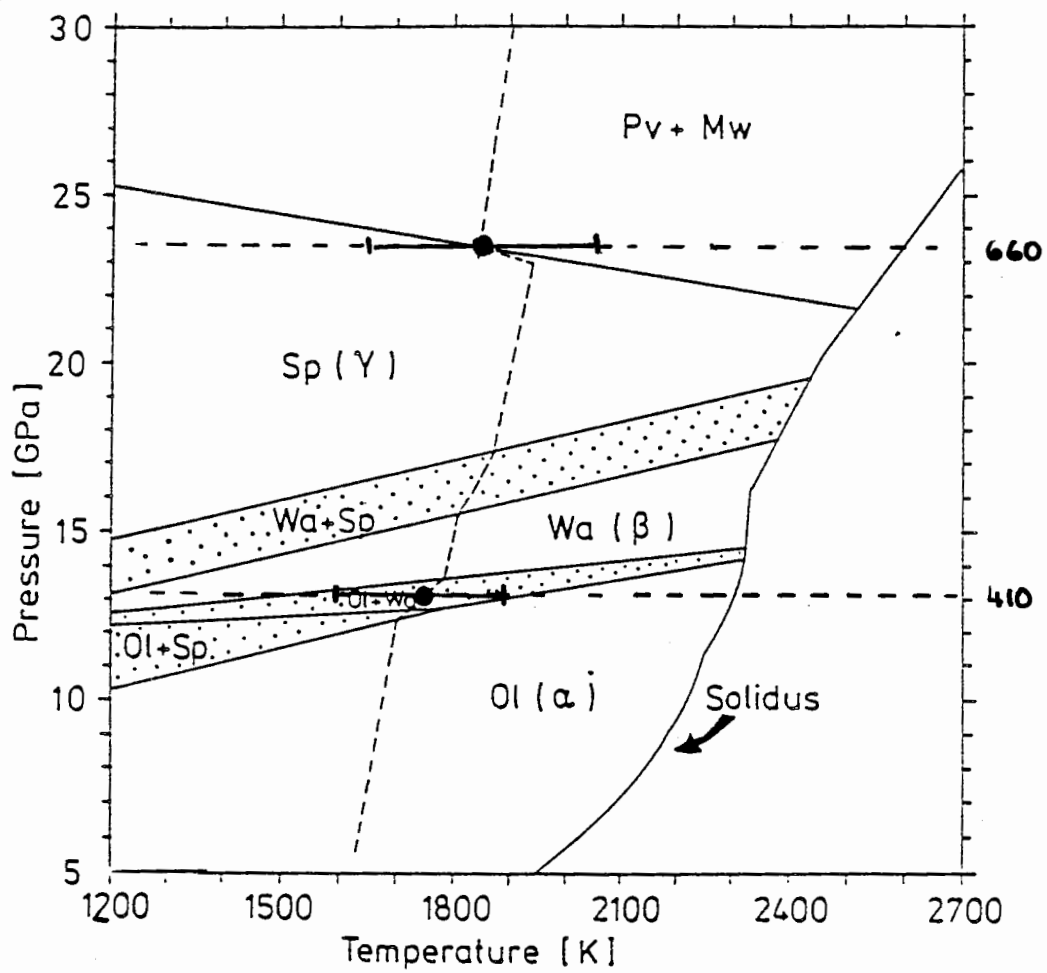
Figure 5.23. Configuration of the diamond anvil cell used by Goettel et al. (1985) to reach a static pressure of 280GPa at the centre of specimen in the form of a disc 50 $\mu$ m in diameter. The wavelength at which tiny fragments of ruby fluoresce is used as a measure of pressure.

## Blatt 17

Diamant-Stempelpresse. Die Probe kann mittels eines fokussierten Lasers auf hohe Temperatur (mehrere tausend Kelvin) aufgeheizt werden. Die Frequenz der Fluoreszenzlinie von Rubinsplittern dient als Druckmaß, die Temperatur wird aus der emittierten Schwarzkörperstrahlung bestimmt. Kristallstruktur und Gitterkonstanten (-> Dichte) werden mittels Röntgenstrukturanalyse bestimmt. Neuere Entwicklungen schließen die Probe in "Druckkammer" in Argon ein, um angenähert hydrostatische Drücke zu erzeugen.

(b)

## Olivine Phase Diagram



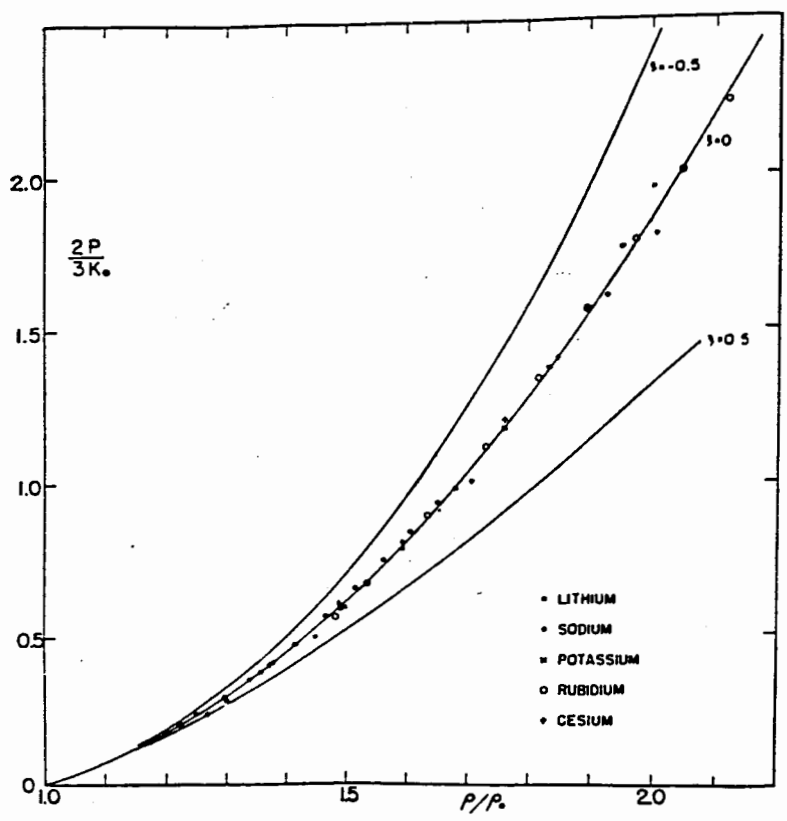


FIGURE 9-3  
Experimental measurements of compressions of the alkali metals compared with compressions calculated from Birch-Murnaghan equation (13). (From Birch, 1952, with permission.)

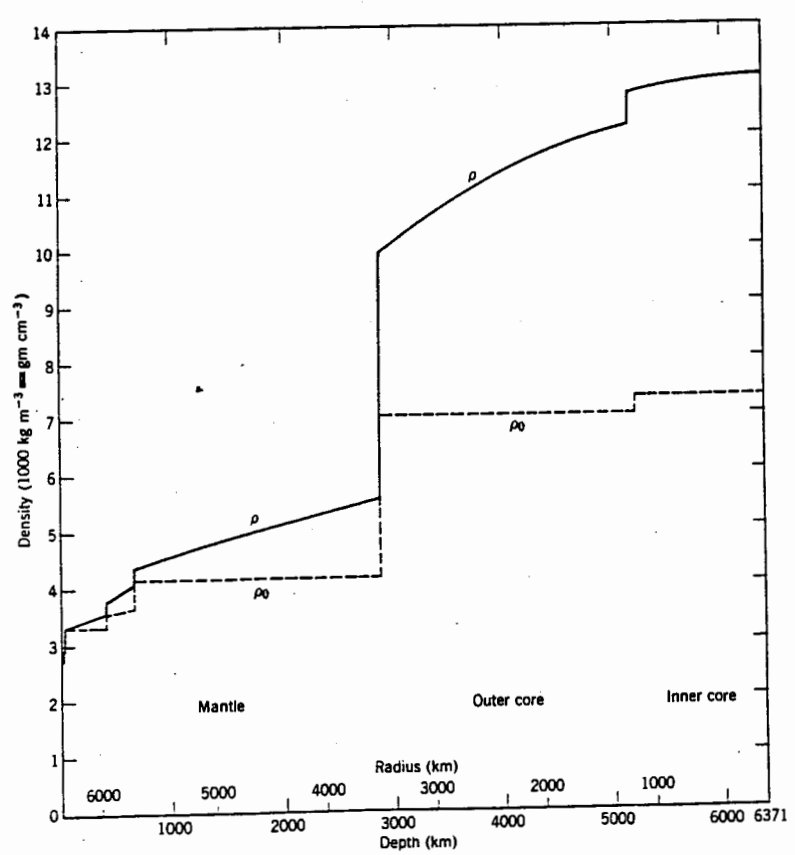
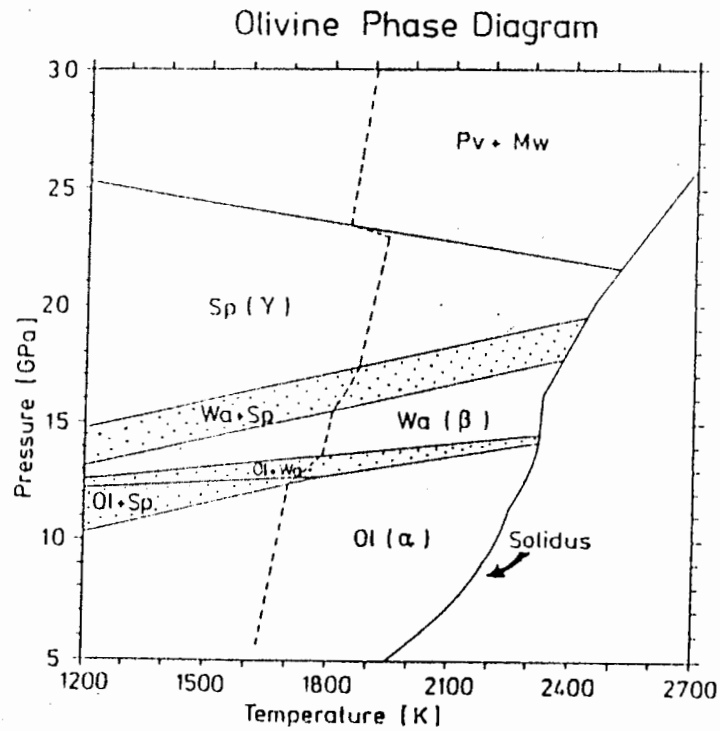


Figure 6.17. Density profile of Earth model by Dziewonski et al. (1975) (solid line) with corresponding extrapolated zero pressure (and room temperature) density (broken line).

a



b

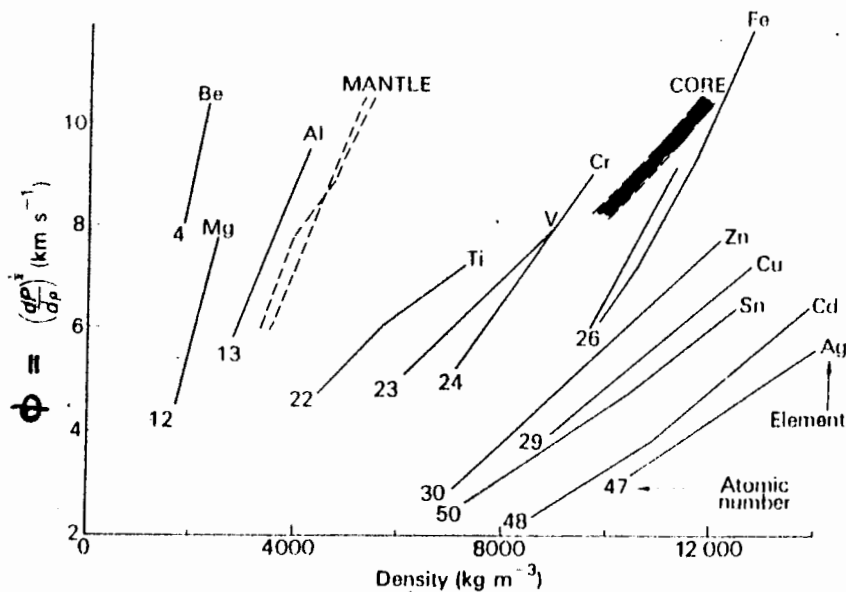
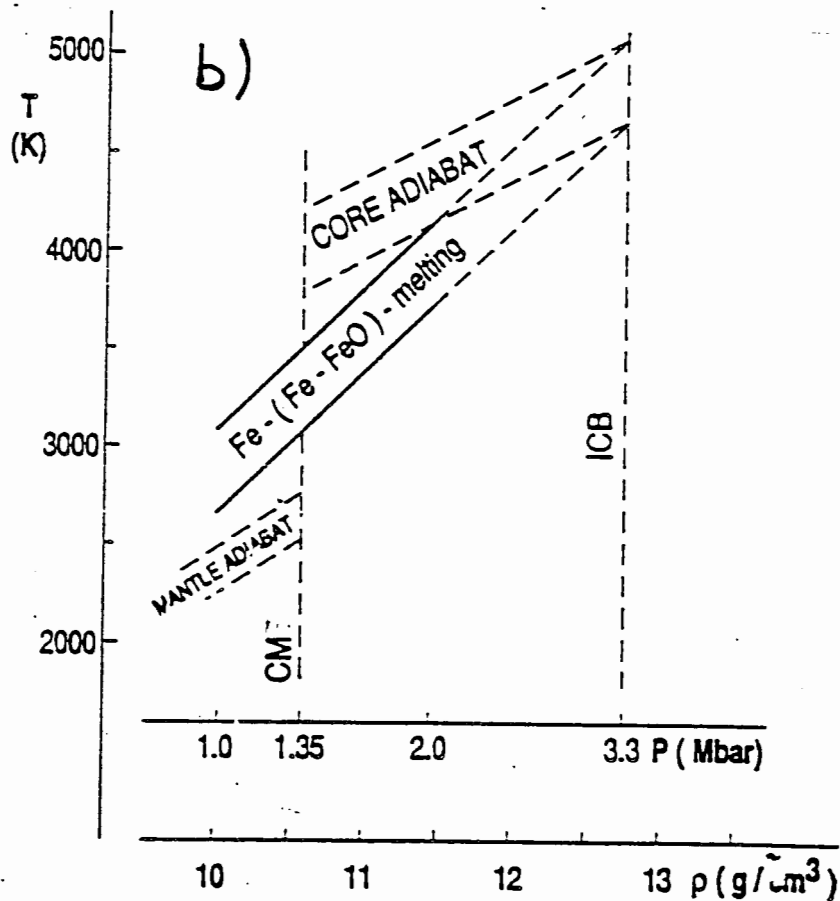
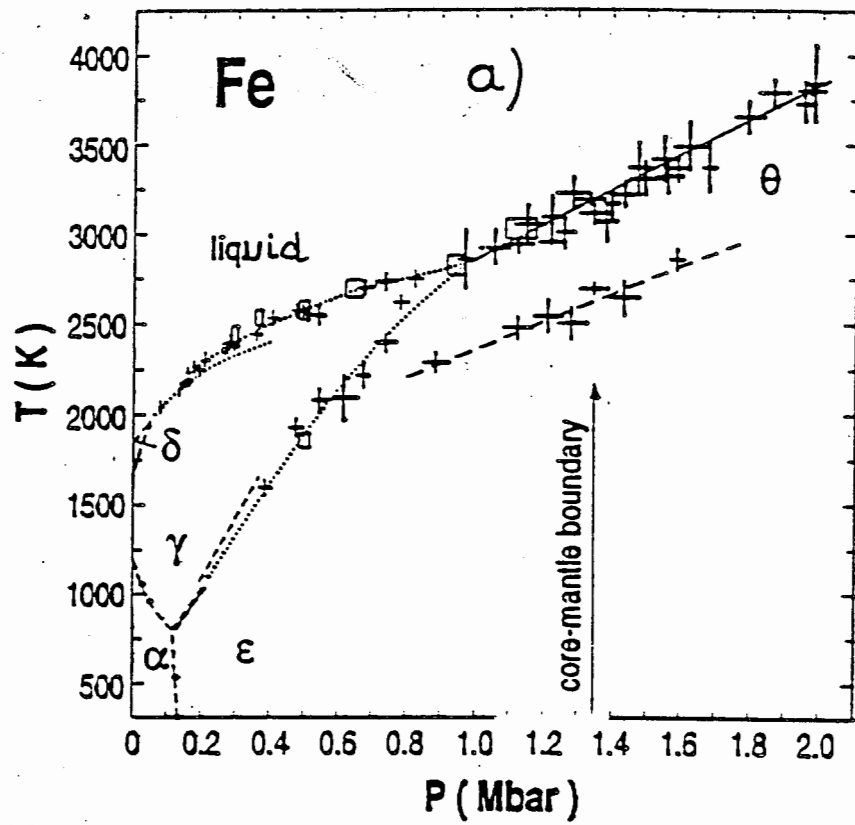


Fig. 6.6 Hydrodynamic sound velocity as a function of density shown for a selection of metals as obtained by shock wave experiments (solid lines) and for the mantle and core as obtained by seismic observations and density models (dashed lines). The numbers shown are atomic numbers. Redrawn from BIRCH (1961b), *Geophys. J. R. astr. Soc.*, **4**, 309.

## Blatt 18

(a) Phasendiagramm von Olivin  $(\text{Mg}_{0.9}\text{Fe}_{0.1})_2\text{SiO}_4$ . Ol=Olivin, Wa=Wadsleyite ( $\beta$ -Phase), Sp=Spinell, Pv=Perovskit  $(\text{Mg,Fe})\text{SiO}_3$ , Mw = Magnesiowüstit  $(\text{Mg,Fe})\text{O}$ . Die gestrichelte Linie ist eine plausible Temperatur-tiefenkurve im Erdmantel.

(b) Variation von seismischem Parameter  $\Phi = (v_p^2 - 4/3 v_s^2)^{1/2}$  und Dichte für verschiedene Metalle aus Stoßwellenexperimenten.



- Blatt 20.1 a) Phasendiagramm des Eisens nach Messungen in der Diamantstempel­presse von Boehler.  
 b) Schematische Darstellung der Berechnung der Kerntemperaturen. Ausgehend vom extrapolierten Schmelzpunkt an der Grenze zum inneren Kern wird ein adiabatischer Temp.-Verlauf im flüssigen äußeren Kern angenommen.

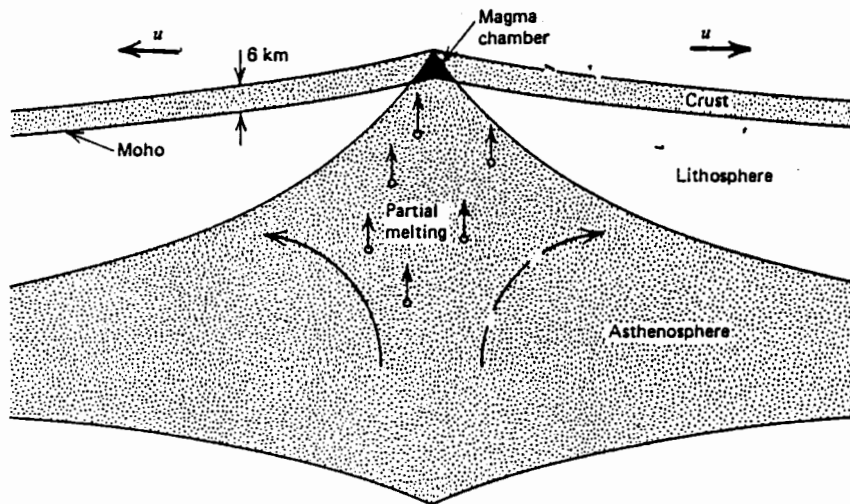
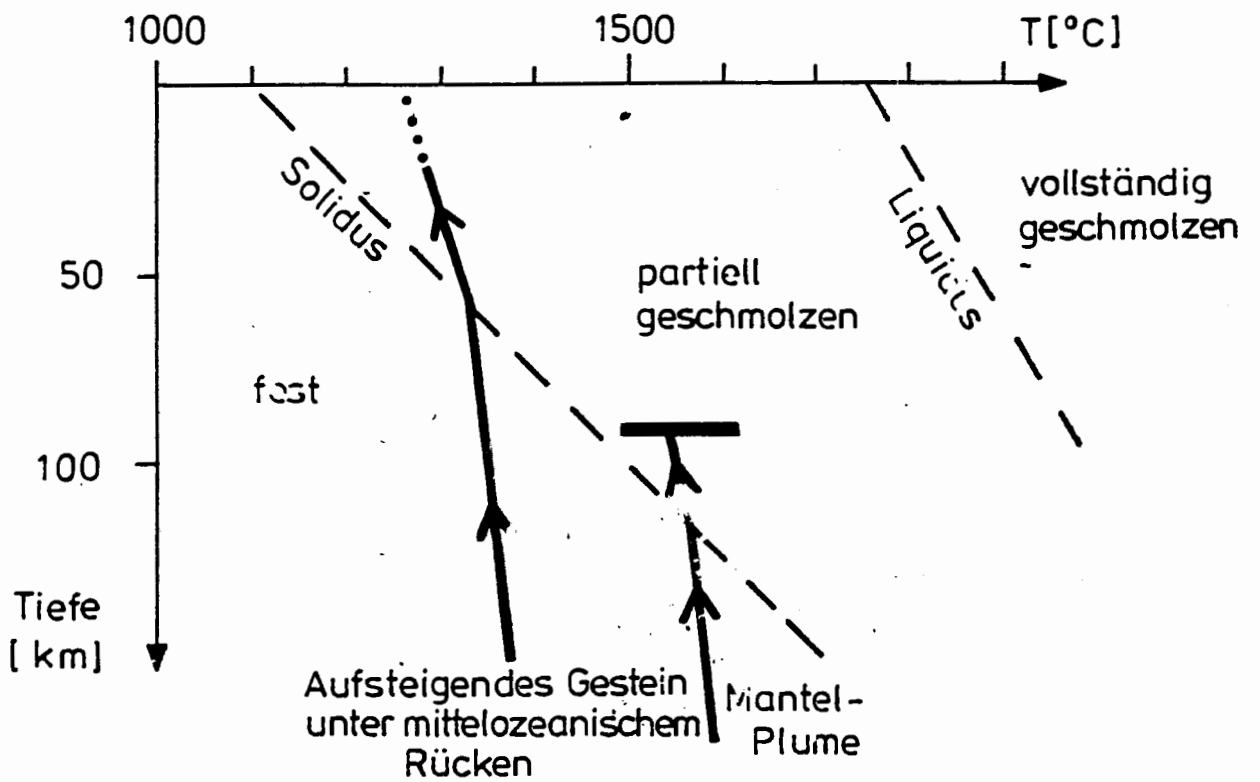


Abb. 3

An accreting plate margin at an ocean ridge.



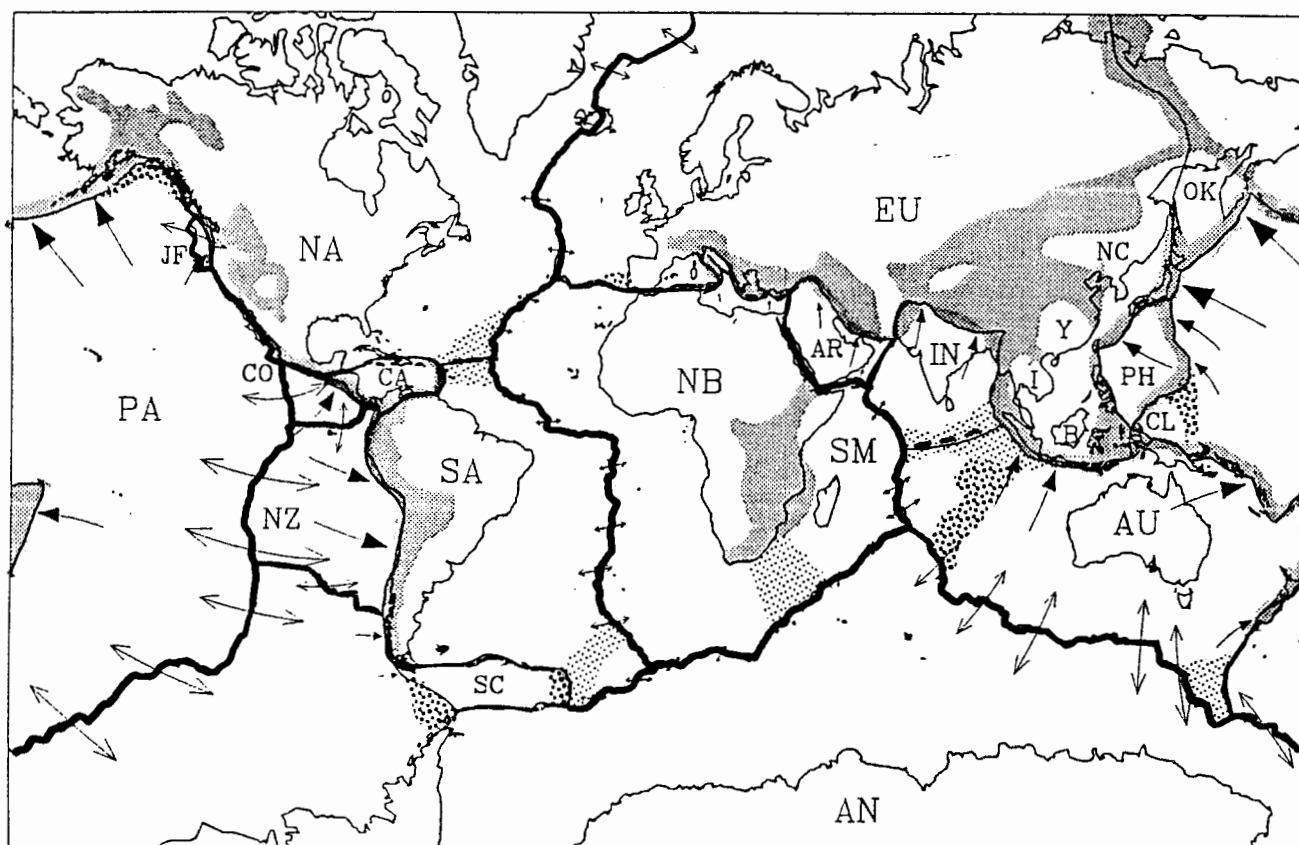


Figure 1. Map showing idealized narrow plate boundaries, velocities between plates, and regions of deforming lithosphere, which can be regarded as diffuse or wide plate boundaries. Plate velocities are shown by arrows. The length of the arrows shows what the displacement would be if the plates were to maintain their present relative angular velocity for 25 million years. The plate separation rate across mid-ocean ridges is shown by symmetrical diverging arrows with unclosed arrowheads at both ends. The plate convergence rate is shown by asymmetrical arrows with one solid arrowhead, which are shown on the underthrust plate where convergence is asymmetric and the polarity is known. Each convergence arrow points toward the overthrust plate. The outlines of deforming regions are approximate and the existence of some deforming zones is speculative. Separate small plates or blocks are labeled in southeast Asia, but their uncertainly located and possibly nonexistent boundaries are not shown in their entirety. Fine stipple shows mainly subaerial regions where the deformation has been inferred from seismicity, topography, other evidence of faulting, or some combination of these. Medium stipple shows mainly submarine regions where the nonclosure of plate circuits indicates measurable deformation; in most cases these zones are also marked by earthquakes. Coarse stipple shows mainly submarine regions where the deformation is inferred mainly from the occurrence of earthquakes. These deforming regions, which constitute wide plate boundaries, cover ~15% of Earth's surface. Future observations may demonstrate that deforming lithosphere covers an area larger or smaller than shown here. Idealized plate boundaries (solid curves) are after *Argus and Gordon* [1991] with the addition of the Scotia plate and several other minor changes. Plate abbreviations: B, Borneo; AN, Antarctica; AR, Arabia; AU, Australia; CA, Caribbean; CL, Caroline; CO, Cocos; EU, Eurasia; I, Indo-China; IN, India; JF, Juan de Fuca; NA, North America; NB, Nubia; NC, North China; NZ, Nazca; OK, Okhotsk; PA, Pacific; SA, South America; SC, Scotia Sea; SM, Somalia; Y, Yangtze. Modified with permission from *Gordon and Stein* [1992, p. 334]. Copyright 1992 American Association for the Advancement of Science.

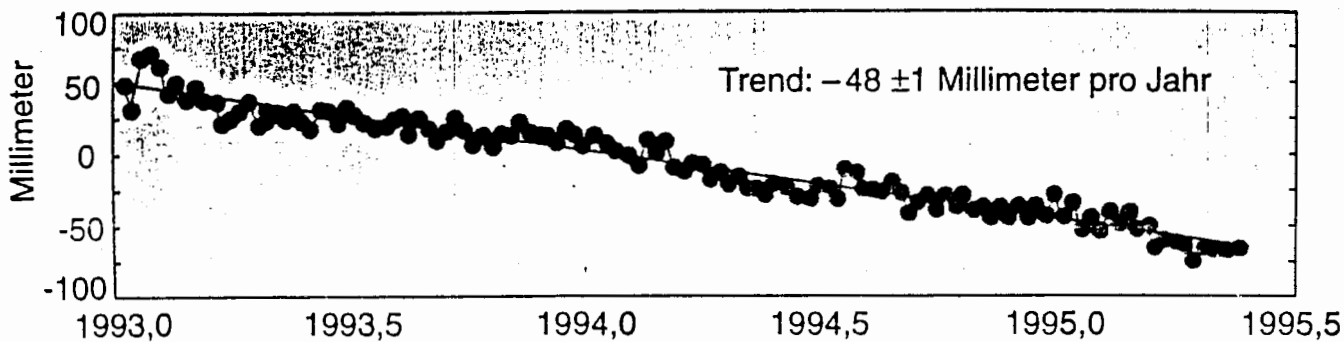


Bild 2: Streckenänderung zwischen Kokee Bay auf Hawaii und Fairbanks in Alaska, abgeleitet aus wöchentlichen Messungen der Stationskoordinaten. Die Daten streu-

en im Mittel acht Millimeter um die berechnete Gerade. Demnach bewegen sich die Stationen aufgrund der Plattentektonik pro Jahr 48 Millimeter aufeinander zu.

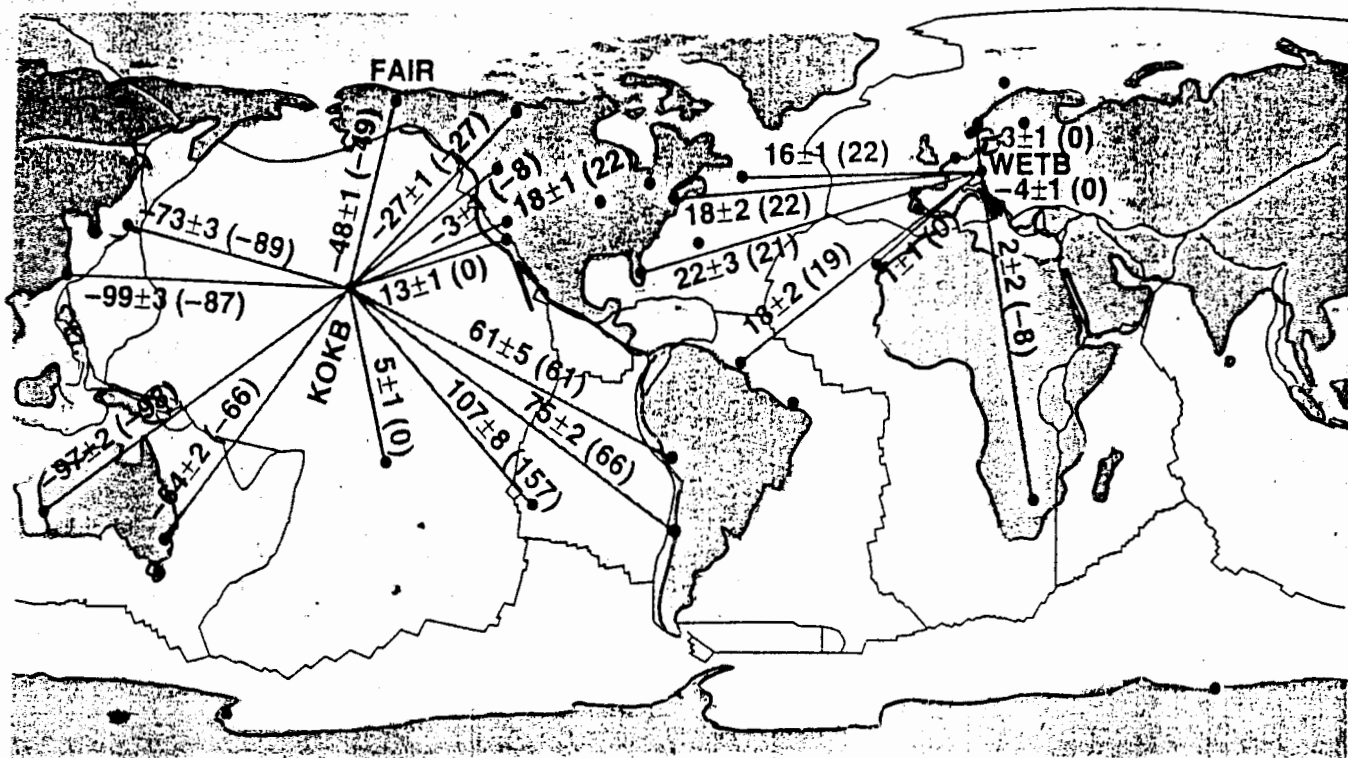
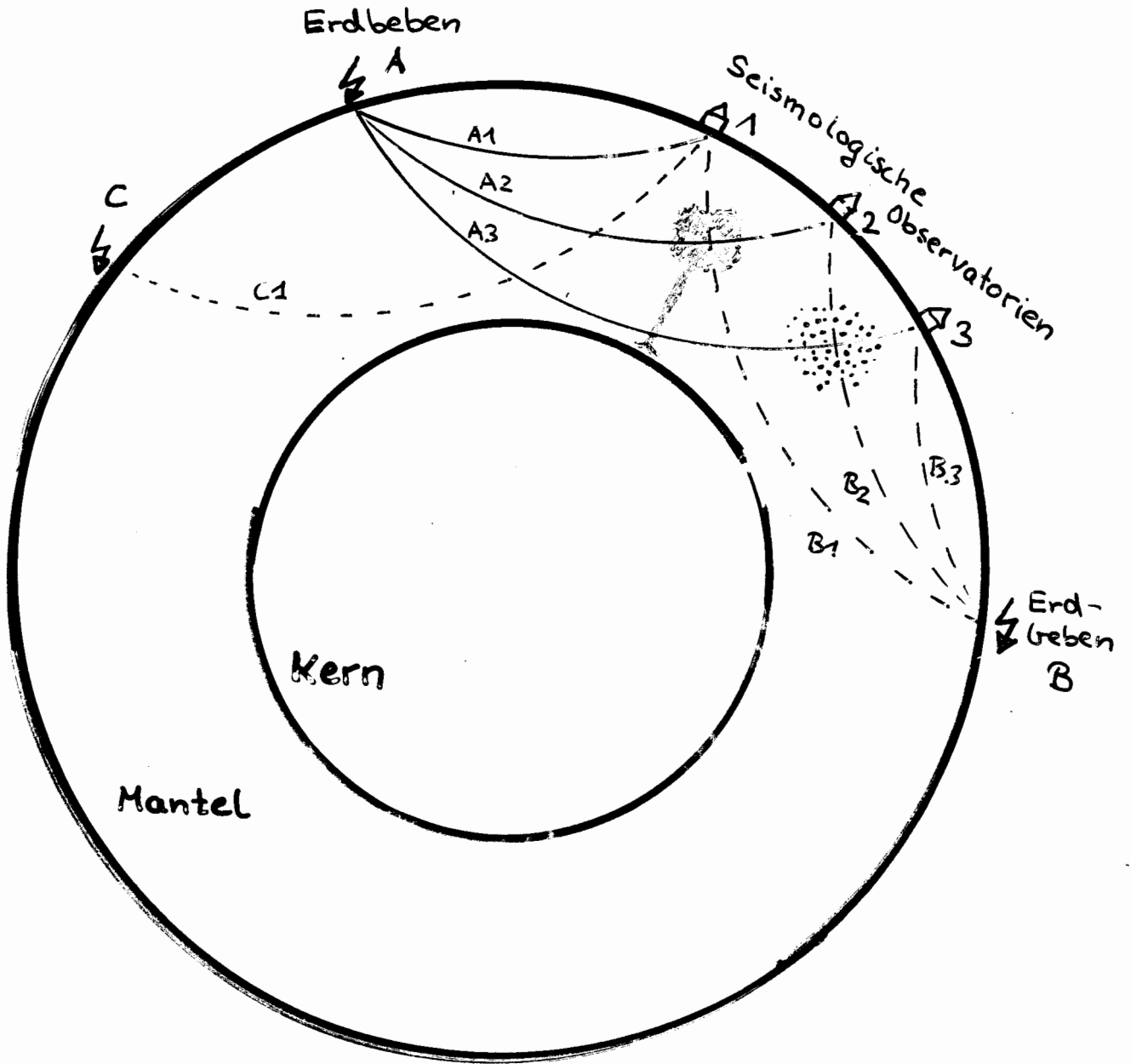


Bild 3: Änderungen der Streckenlänge zwischen Kokee Bay auf Hawaii (KOKB) beziehungsweise Wettzell im Bayerischen Wald (WETB) und benachbarten Statio-

nen von Januar 1993 bis Mai 1995 in Millimetern pro Jahr (mit dem geophysikalischen Modell NUVEL berechnete Werte in Klammern, Plattenumrisse in schwarz).

Spektrum 1/96 S. 116



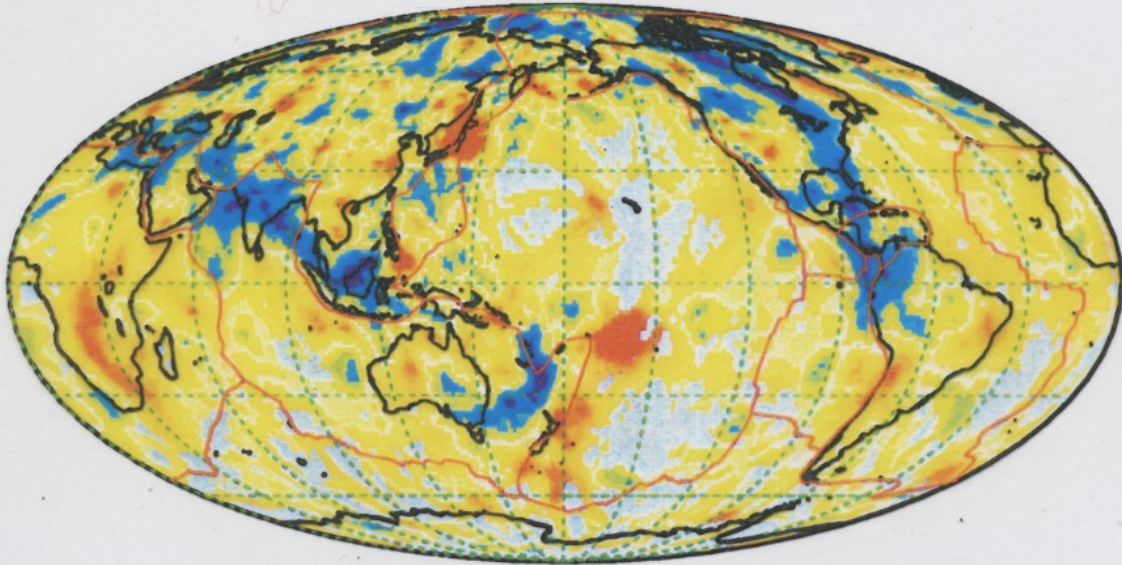


Seismische Tomographie

## Earth's structure at 1300 km depth

Tomography: Widiyantoro & Van der Hilst (1996)

Data: Engdahl, Van der Hilst, & Buland (1996)



## Plate convergence during past 109 Ma

Sources: Gordon & Jurdy (1986) and Lithgow-Bertelloni & Richards (1996)

(Compilation by Steinberger (1996))

