

IMPRS Lecture @ MPS

Magnetospheres – Earth and Outer Planets

12-16 September 2005

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Outline

Part 1: Planetary Magnetospheres – Overview

Part 2: Magnetosphere of Jupiter

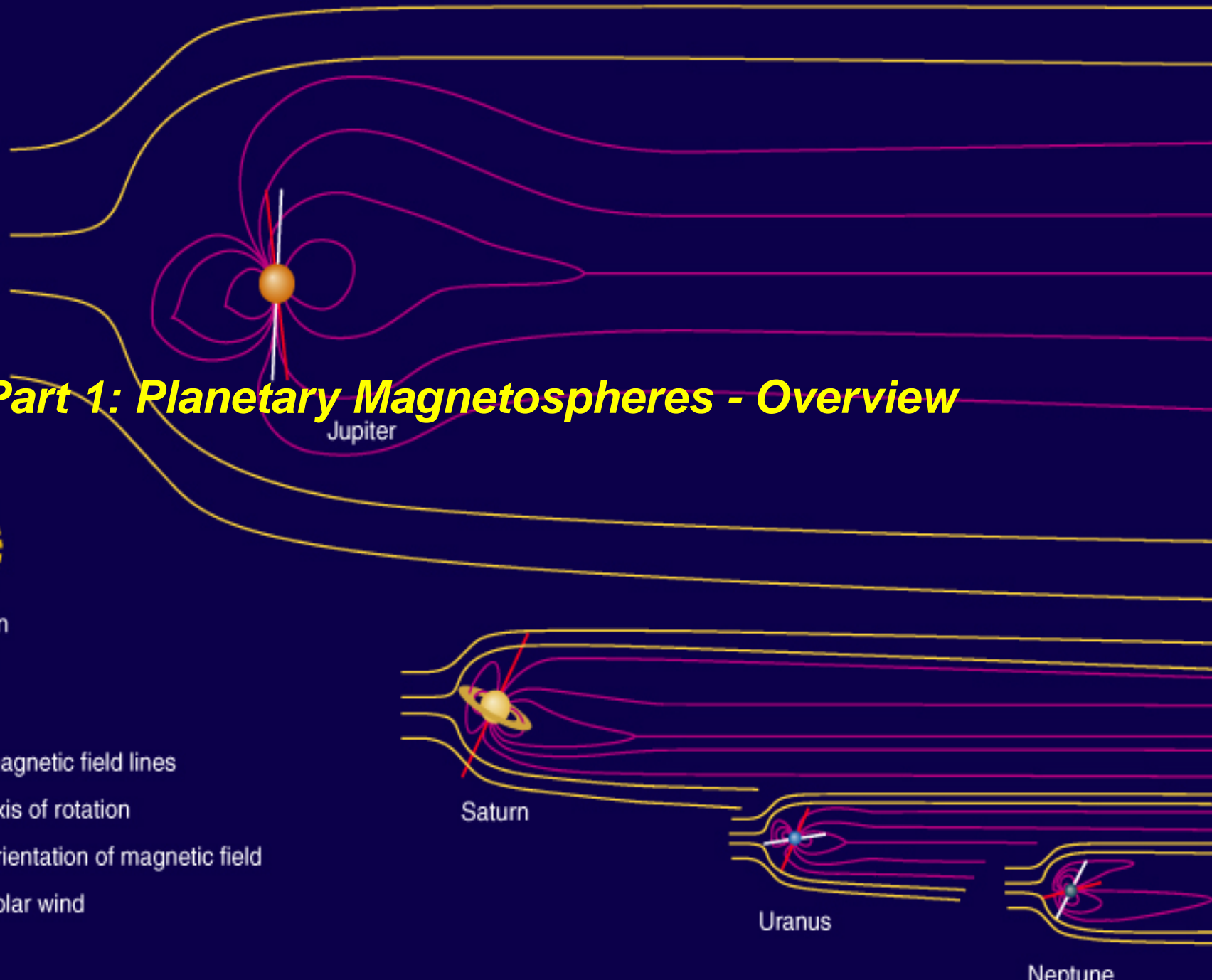
Part 3: Magnetosphere of Saturn

Part 1: Planetary Magnetospheres - Overview



size of Sun
(to scale)

- magnetic field lines
- axis of rotation
- orientation of magnetic field
- solar wind



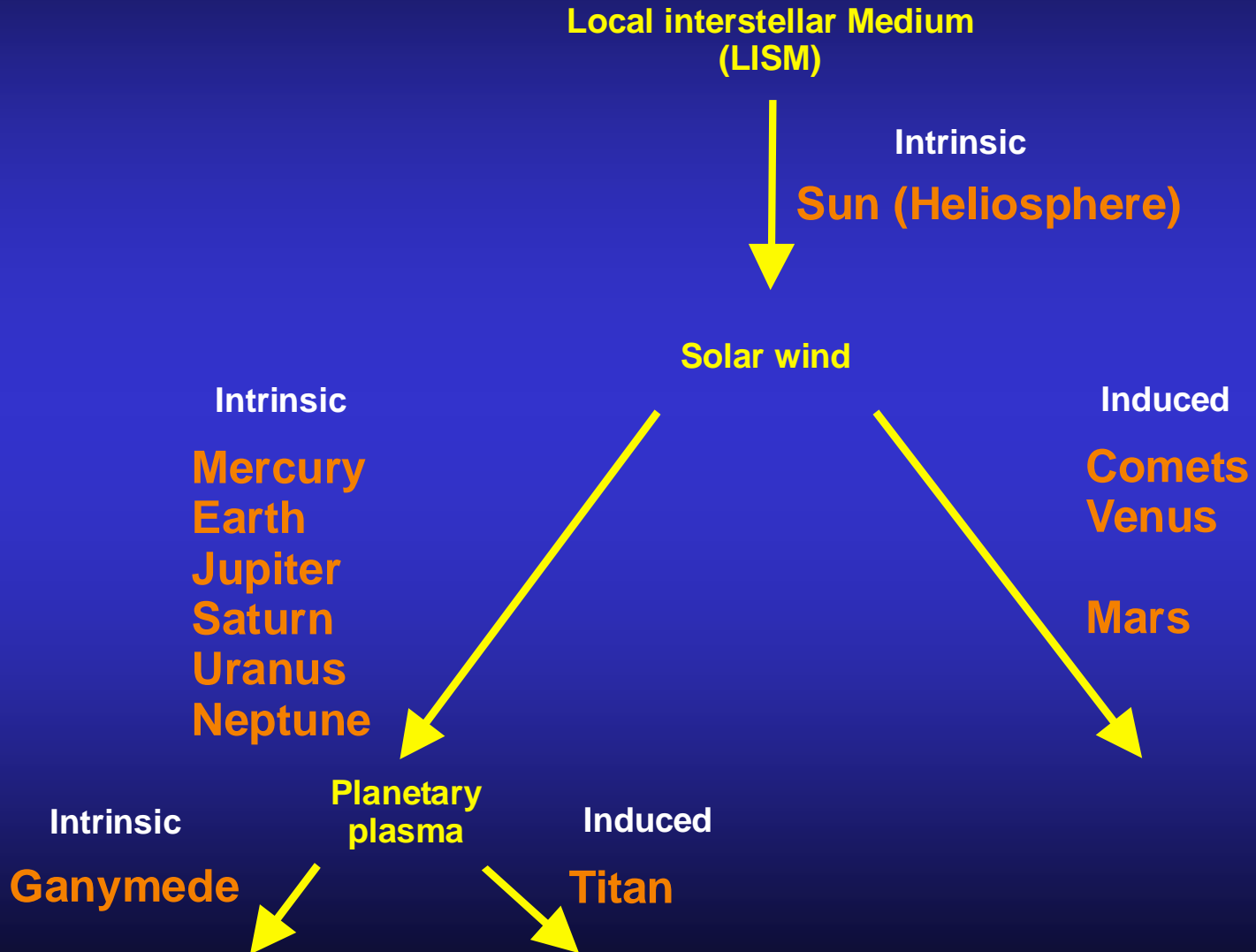
Jupiter

Saturn

Uranus

Neptune

Magnetospheres

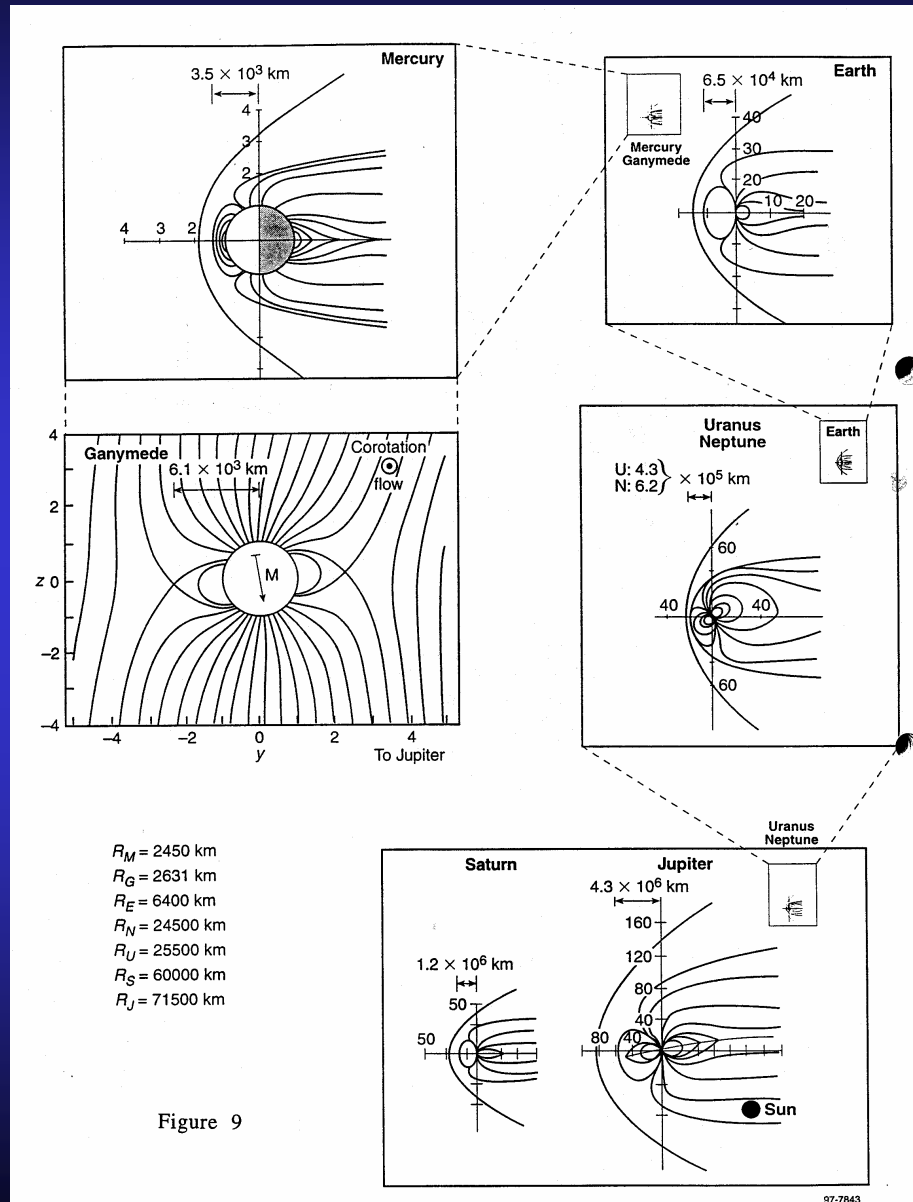


Intrinsic planetary magnetospheres - comparison

small

intermediate

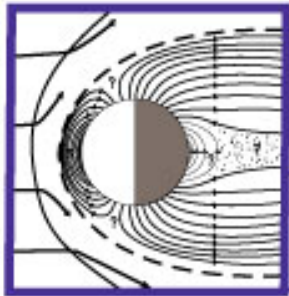
huge



Comparative magnetospheres

MERCURY:

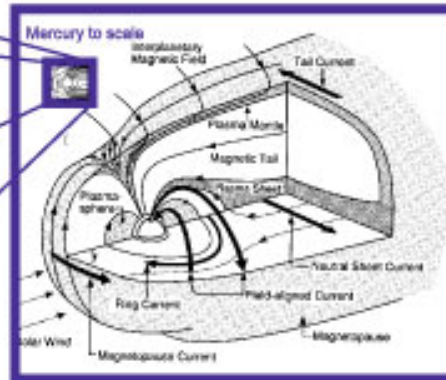
- Small
- Minute timescales
- Solar wind dominated



Mariner,
MESSENGER
Bepi Colombo

EARTH:

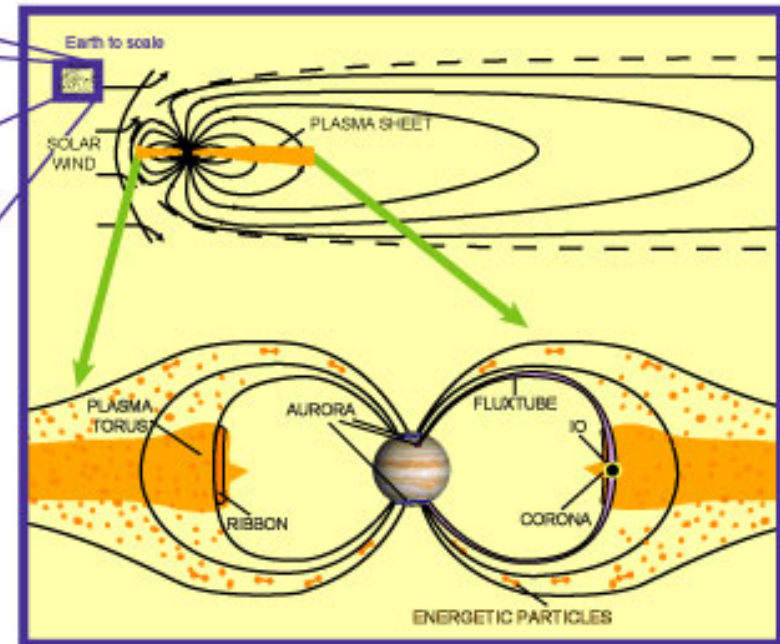
- Intermediate
- Hour timescales
- Solar wind driven



~100 missions since 1957
e.g. Polar, Geotail, FAST,
Sampex, Cluster

JUPITER: and other Gas Giants

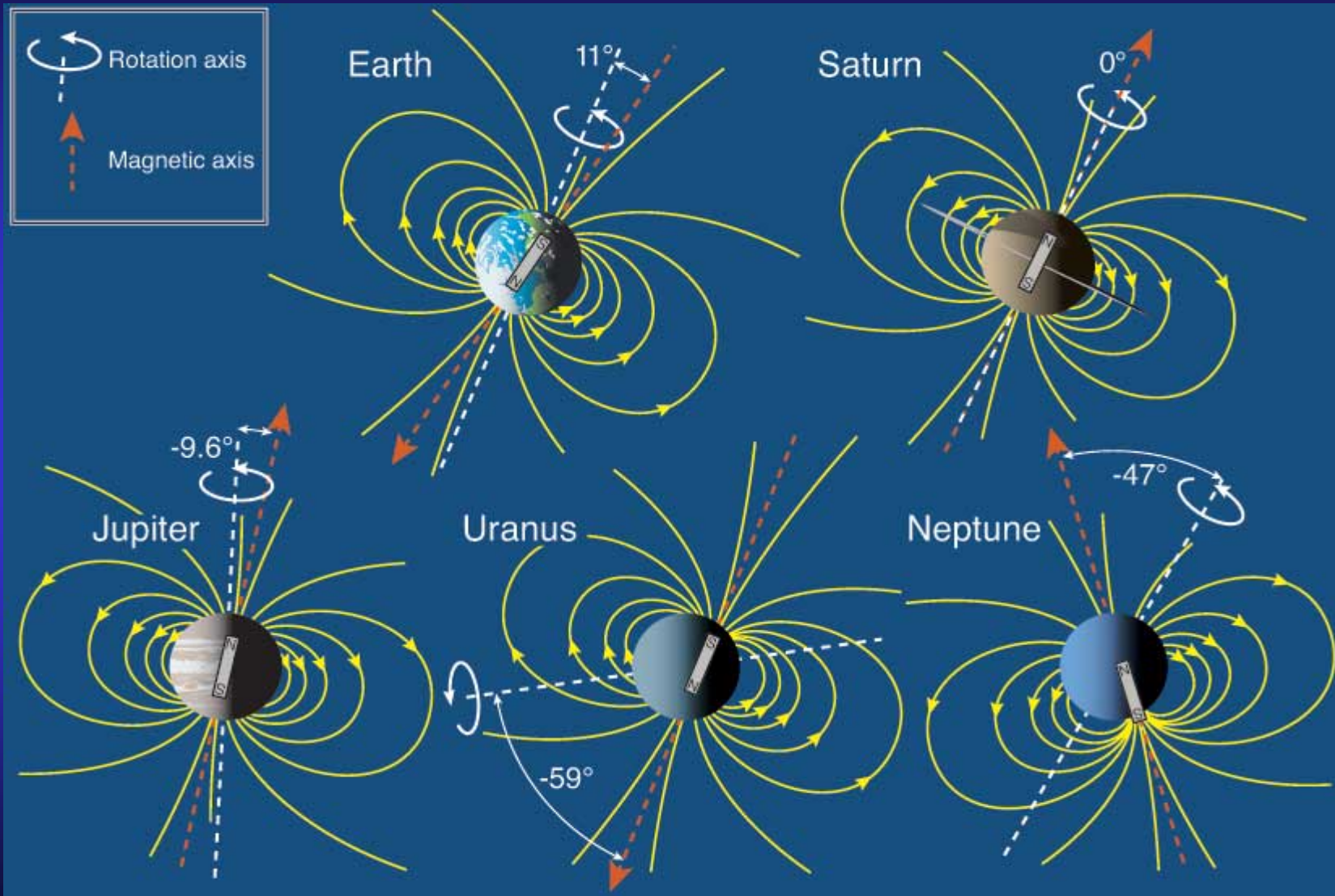
- Giant
- Timescales - minutes to months?
- Rotationally driven - solar wind triggered?



Pioneer, Voyager, Ulysses,
Galileo, Cassini Juno

Testing our understanding of Sun-Earth connections through application to other planetary systems

Orientation of rotation and magnetic axes



Solar wind conditions in the vicinity of the magnetospheres

Planet	Magnetic field [nT]	plasma density [cm ⁻³]
Mercury	46 – 21	73 - 33
Earth	8	5
Jupiter	1	0.2
Saturn	0.6	0.06
Uranus	0.3	0.01
Neptune	0.005	0.005

The velocity is almost constant in the inner part of the heliosphere and ranges between 400 and 800 km/s

Sizes and shape of planetary magnetospheres

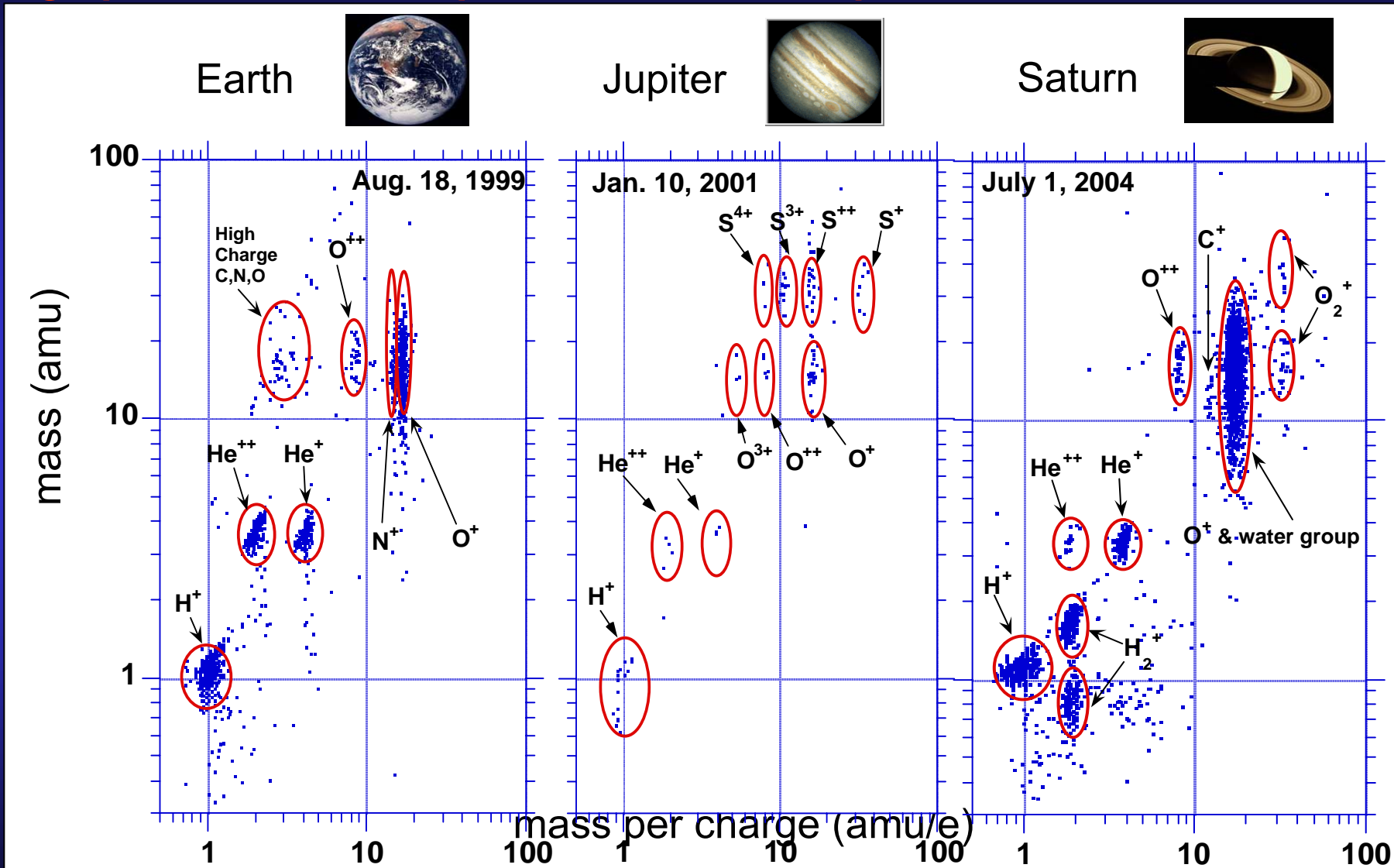
$$R_M/R_p \sim 1.2 \{B_o^2 / \rho_{sw} V_{sw}\}^{1/6}$$

	Mercury	Earth	Jupiter	Saturn	Uranus	Neptune
B_o	.003	.31	4.28	.22	.23	.14
R_M Calc.	1.4 R_M	10 R_E	42 R_J	19 R_S	25 R_U	24 R_N
R_M Obs.	1.4-1.6 R_M	8-12 R_E	50-100 R_J	16-22 R_S	18 R_U	23-26 R_N

Plasma sources of planetary magnetospheres

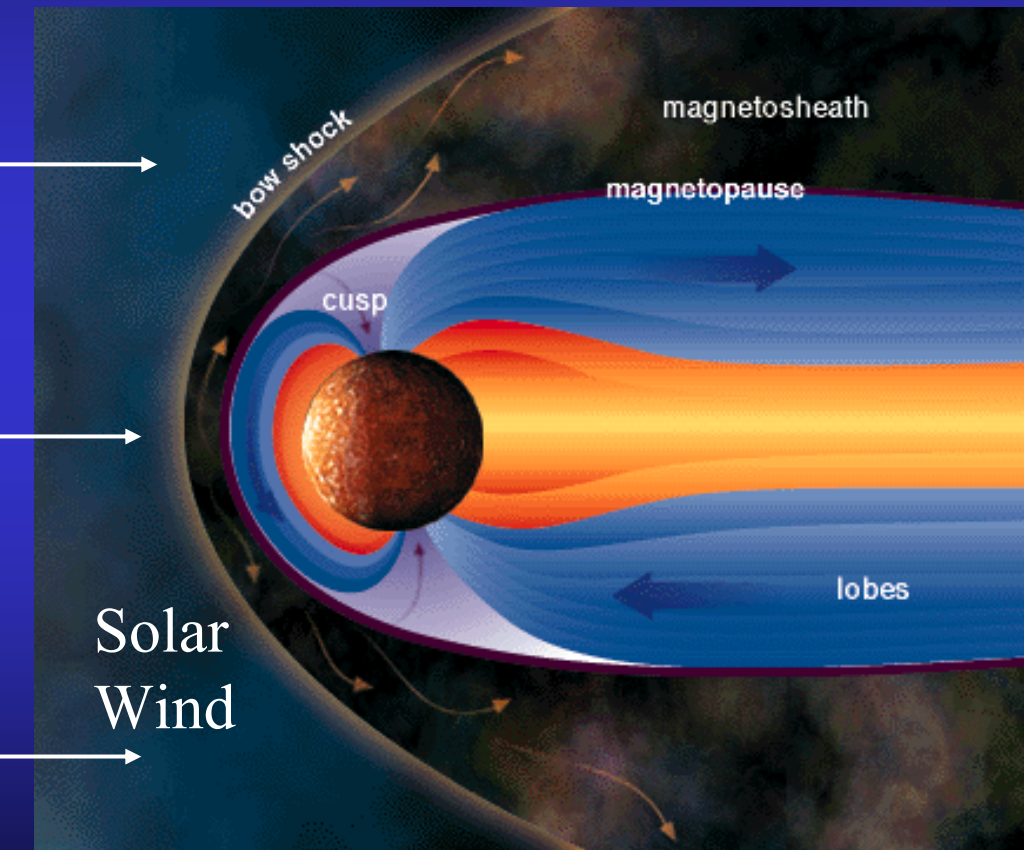
	Mercury	Earth	Jupiter	Saturn	Uranus	Neptune
N_{\max} cm^{-3}	~1	1-4000	>3000	~100	~3	~2
Compo sition	H ⁺ Solar Wind	O ⁺ H ⁺ Iono- sphere	O ⁿ⁺ S ⁿ⁺ H ⁺ Io	O ⁺ H ₂ O ⁺ H ⁺ , N ₂ Rings, icy satellites Titan	H ⁺ Iono- sphere	H ⁺ N ⁺ Triton, Iono- sphere
Source kg/s	?	5	700- 1200	~2	~0.02	~0.2

Charge Energy Mass Spectrometer (CHEMS) on Cassini records "fingerprints" of ion composition at Earth, Jupiter, and Saturn

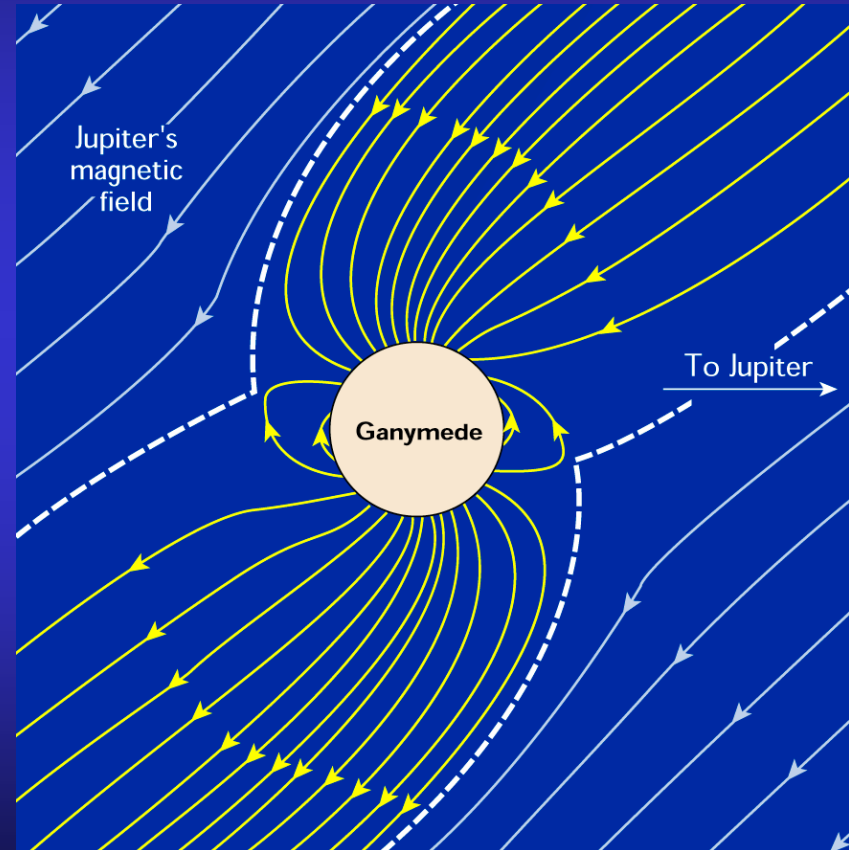


Small magnetospheres Mercury and Ganymede

Mercury - Magnetic field
detected by *Mariner 10* in 1974



Ganymede - Magnetic field
detected by *Galileo* in 1996



$B_{\text{surface}} \sim 1/100$ Earth

—————|—————| Diameter of Earth

Huge magnetospheres

Giant Planet Magnetospheres

Main differences from Earth:

1. **Rotation dominated; driving energy is the fast rotation and not the solar wind**
 - plasma is (partly) corotating with the planet

2. **Strong plasma sources inside the magnetosphere (satellites or rings)**
 - radial outward plasma transport; additional loss mechanisms

Jupiter and Saturn

- Symmetric
- ~Dipolar
- Strong plasma production
- Limited solar wind influence

Uranus and Neptune

- Highly asymmetric,
- Highly non-dipolar
- Complex transport (SW + rotation)
- Multiple plasma sources (ionosphere + solar wind + satellites)

Corotation in planetary magnetospheres

Neutral atmosphere must corotate with the planet

+

Electrical conductivity Σ must be very large (effective atmosphere/ionosphere coupling)

$$\vec{I} = \overline{\Sigma} \cdot (\vec{E} + \vec{v}_n \times \vec{B})$$

$$\vec{E} = -\vec{v}_{\text{flow}} \times \vec{B}$$



$$\vec{I} = \overline{\Sigma} \cdot (\vec{v}_n - \vec{v}) \times \vec{B}$$

Σ : height-integrated conductivity
 \vec{v}_n : neutral atmosphere velocity
 \vec{E} : horizontal electric field
 \vec{I} : height-integrated current density
 \vec{v}_{flow} : flow velocity above ionosphere

\vec{I} is coupled by field-aligned currents to the current system in the magnetosphere with current density \vec{j}

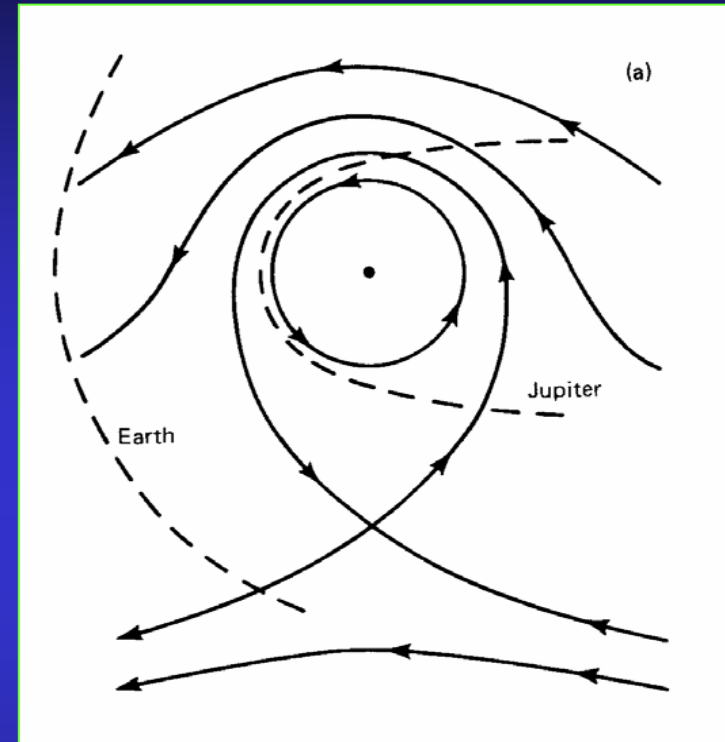
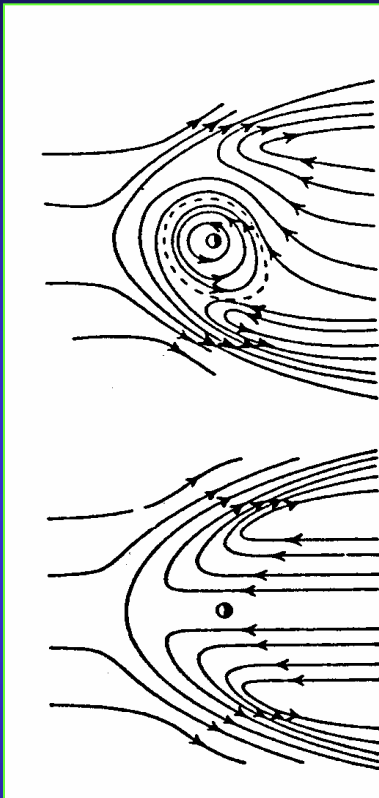
$$\rho \cdot \frac{d\vec{v}}{dt} + \nabla \cdot \overline{\vec{P}} = \vec{j} \times \vec{B}$$

+

radial stress balance

Corotation of plasma

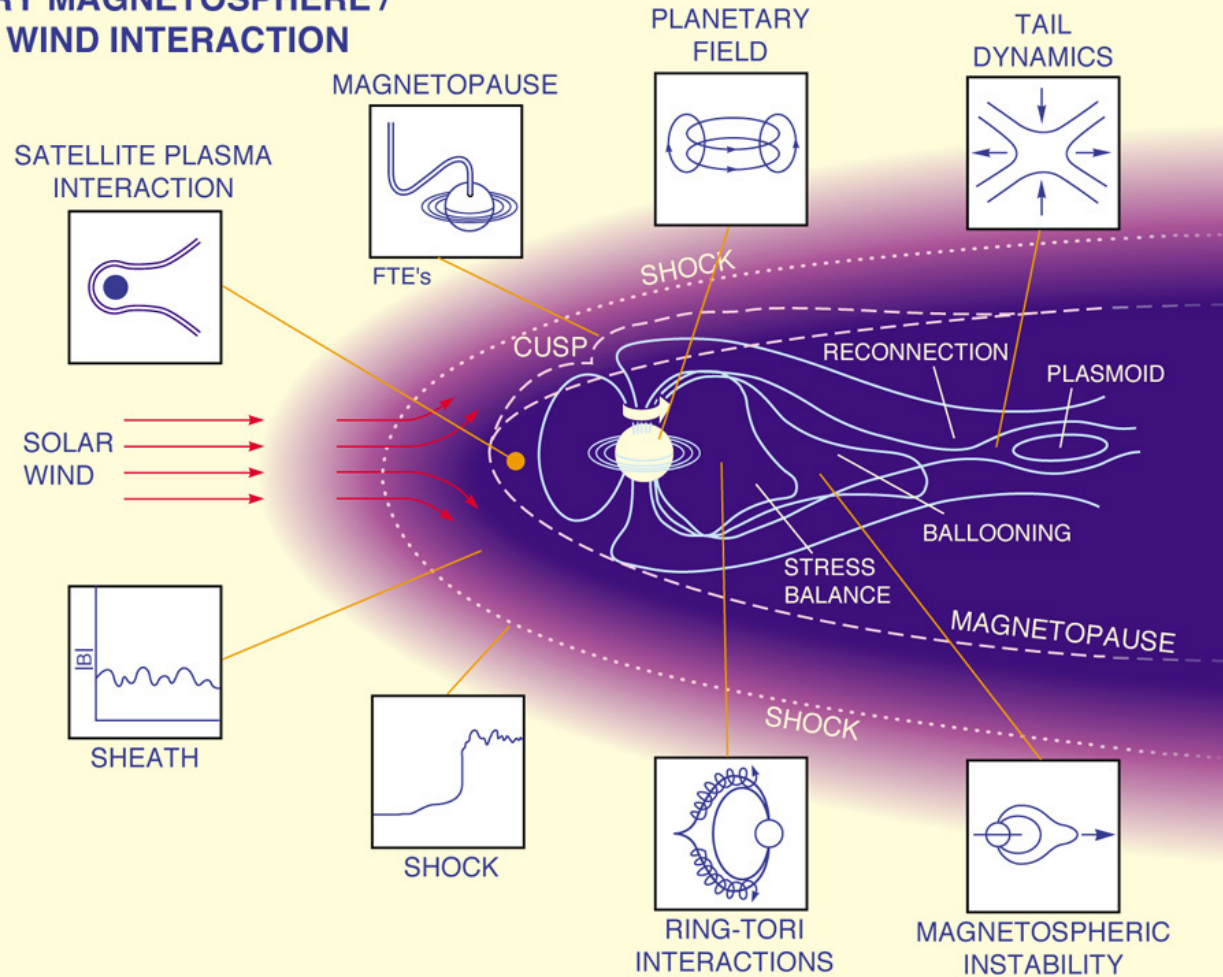
Earth's-like magnetosphere



- **plasmasphere in the inner magnetosphere with closed flow lines**
- **if scaled to Jupiter: closed flow lines outside the magnetosphere**
 - **rotation dominated**

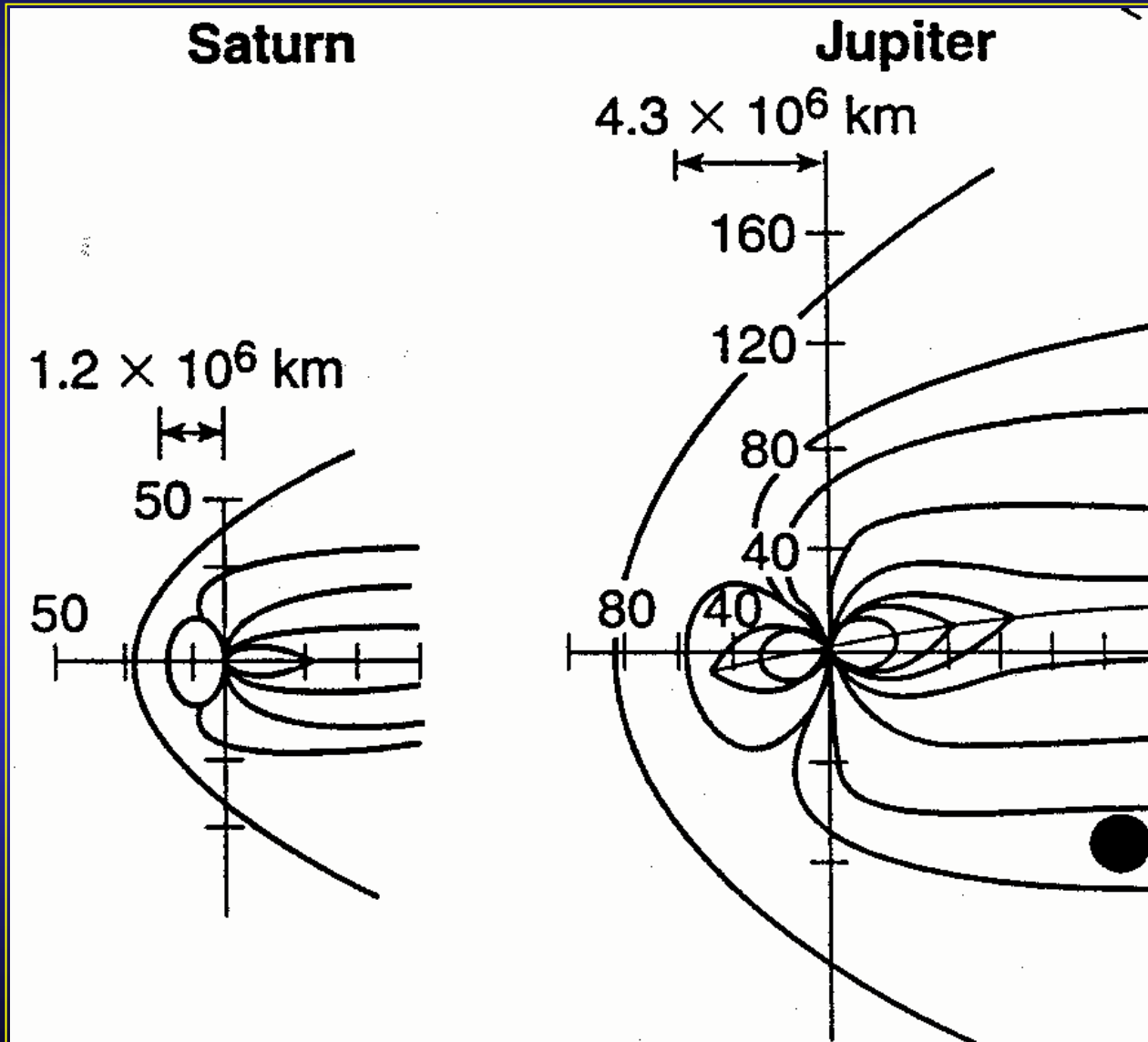
Magnetosphere interactions

PLANETARY MAGNETOSPHERE / SOLAR WIND INTERACTION

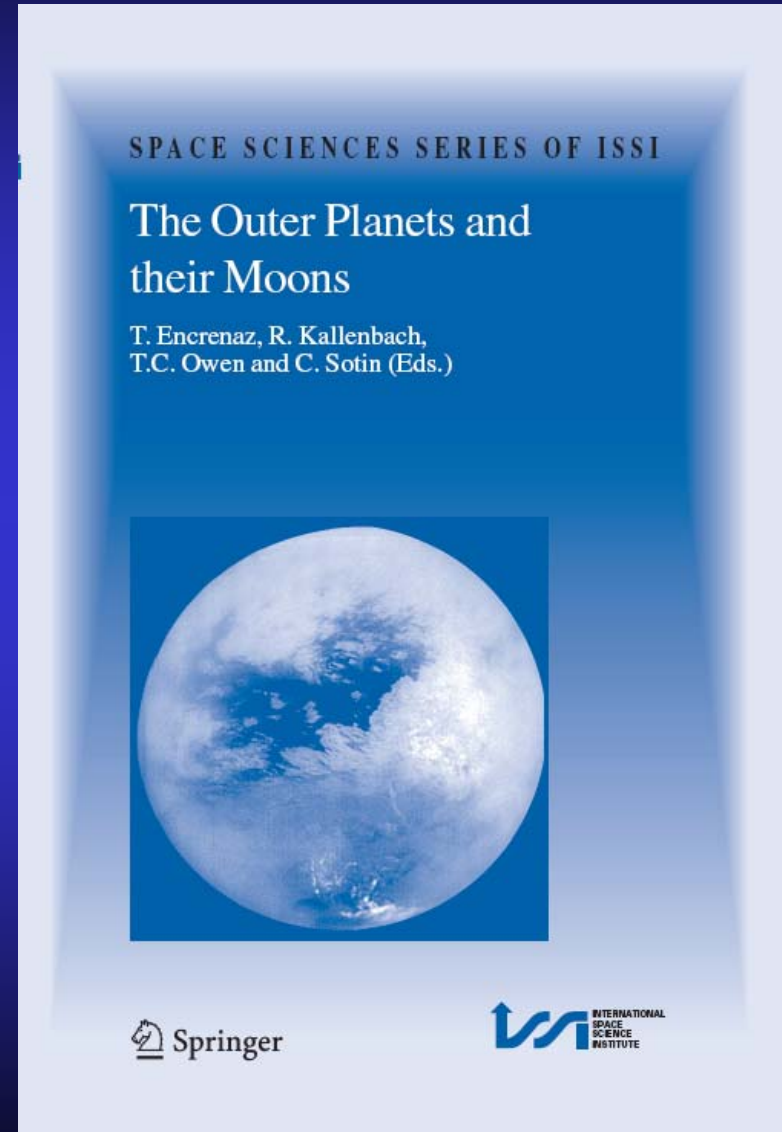
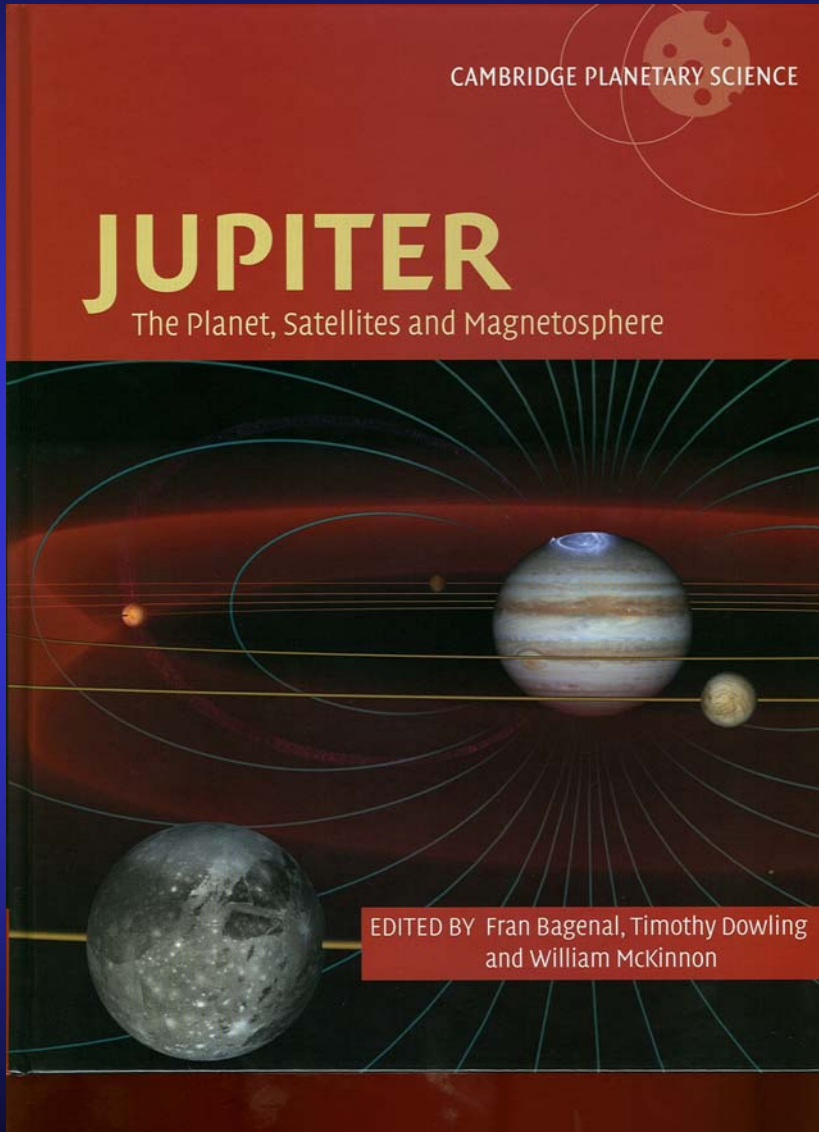


Magnetospheres of Jupiter and Saturn

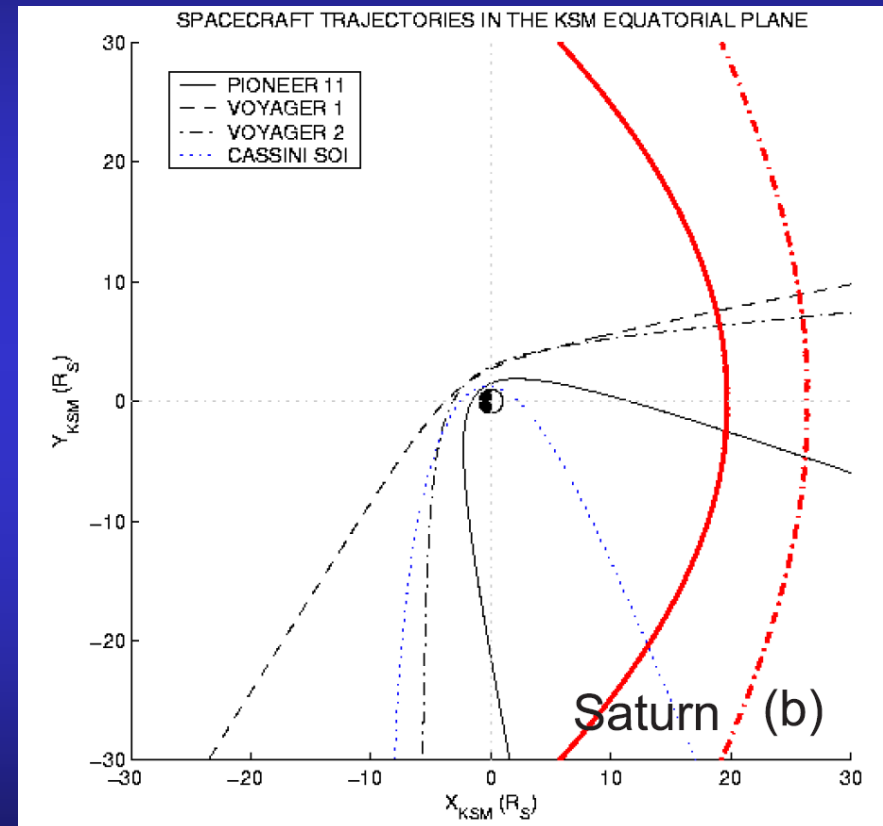
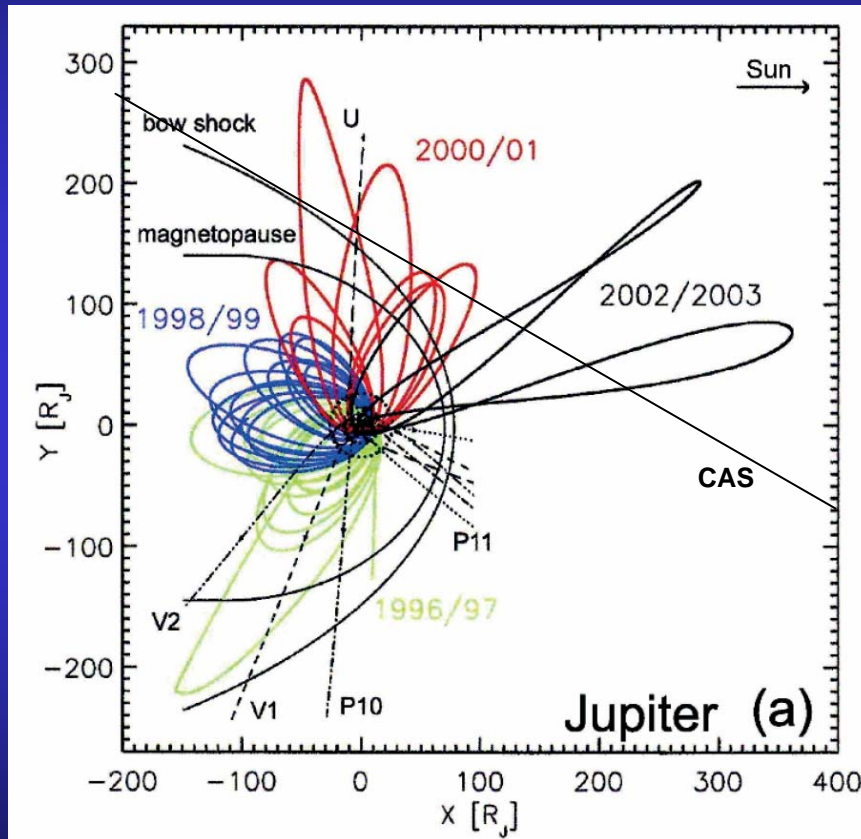
Comparison



Recently published books about outer planets



Spacecraft exploration of Jupiter and Saturn



Spacecraft exploration of Jupiter and Saturn

TABLE I
Measured positions of magnetospheric boundaries at Jupiter and Saturn.

			local time	distance BS (R_p)	standoff BS (R_p)	distance MP (R_p)	standoff MP (R_p)
P 10	1974	Jupiter	1000	108.9	102-130	96.4-50	80-96
		Jupiter	0600	124-189		98-150	
P 11	1974	Jupiter	1000	109.7-79.5	92-100	97-64.5	80-90
		Jupiter	1200	90.8-95		56.6-80	
	1979	Saturn	1000	24-20		17	
		Saturn	1200	49-102		30-40	
VG 1	1979	Jupiter	1000	85.7-55.7	77-103	67.1-46.7	62-85
		Jupiter	0400	199.2-258		158.3-165.4	
	1980	Saturn		26	23	23-24	
		Saturn		78		43-47	
VG 2	1979	Jupiter	1000	98.8-66.5	79-95	71.7-61.9	70-101
		Jupiter	0300	282.3-283.3		169.1-279.4	
	1981	Saturn		32-24	18.5	19	
		Saturn		78-88		50-70	
ULS	1992	Jupiter	1000	113	85-104	110-87	72-104
		Jupiter	1800	109-149		83-124	
GLL	1995	Jupiter	0600	130-214	100-130	120	90
		Jupiter	1750			107-149	
		Jupiter	1920	130-133	82-105	120-150	88-98
		Jupiter	1625	108-125		82-96	
CAS	2001	Jupiter	1900	> 450		204	111
		Saturn	0750	49.2-40.5		35	
			-0800				
	(SOI)	Saturn	0540				

Cassini trajectory around Saturn



The background features a stylized representation of the solar system. A central yellow and orange sun is surrounded by several planets on elliptical orbits. Jupiter is prominently shown on the left, with its magnetosphere depicted as a complex, glowing blue and cyan structure that extends far beyond its atmosphere. The magnetosphere consists of numerous field lines and a large, ring-like structure. The text is overlaid on this scene in a yellow, bold, sans-serif font.

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Part 2: The Magnetosphere of Jupiter

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Outline Jupiter

- **Global configuration**
 - regions
 - the special role of Io
 - particle flow pattern
 - global ion composition
 - neutrals
- **Dynamics**
 - interchange motion
 - aurora
 - particle injections
 - substorm-like processes (particle bursts)
 - boundary phenomena
- **Moon phenomena**
 - Ganymede's magnetosphere
 - Io torus
 - Europa torus

Global configuration of the Jovian magnetosphere

regions

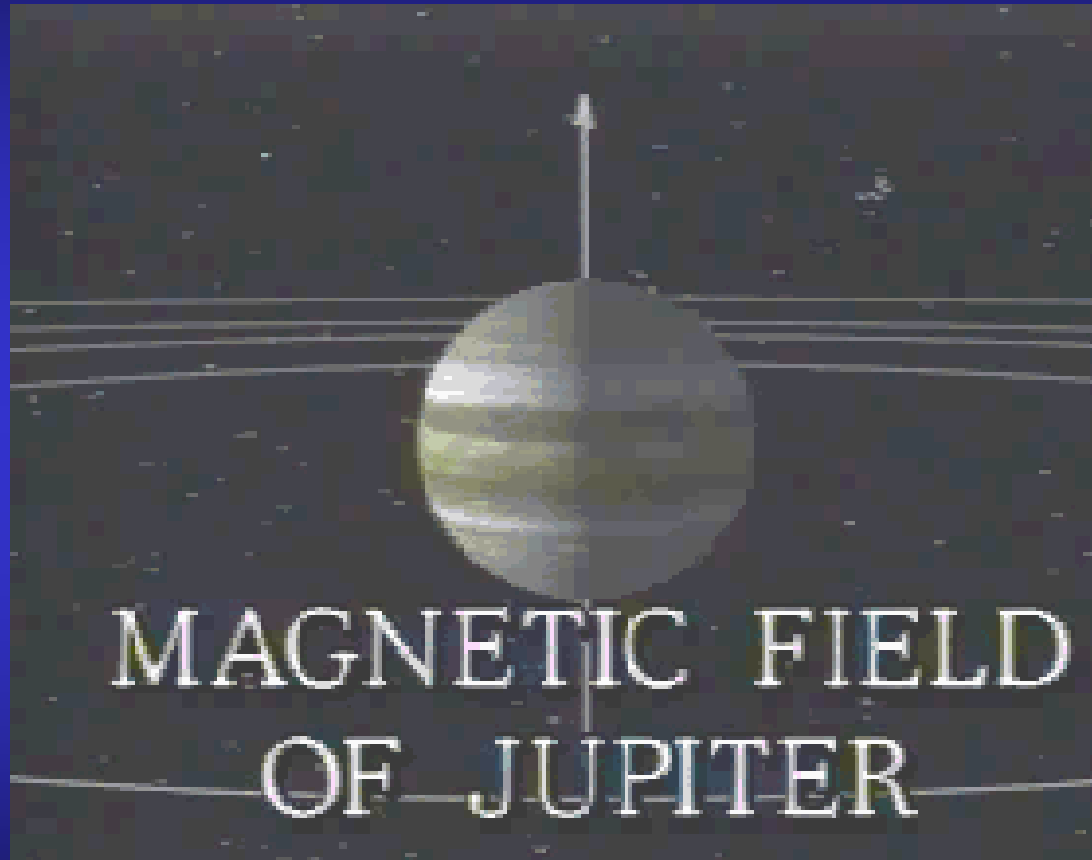
the special role of Io

particle flow pattern

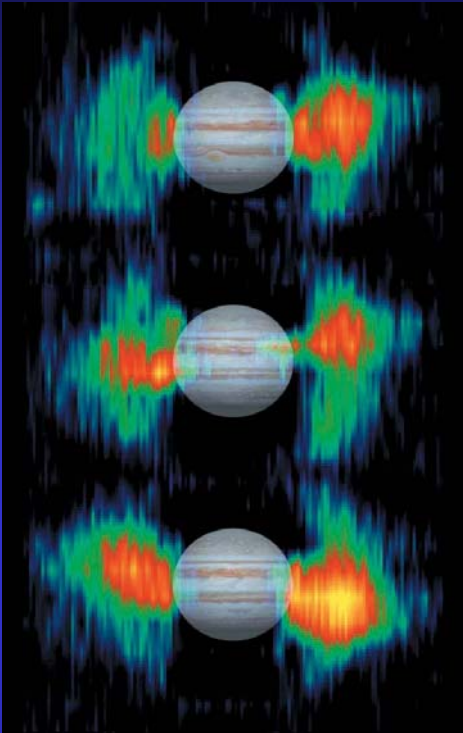
global ion composition

neutrals

Jupiter's magnetosphere



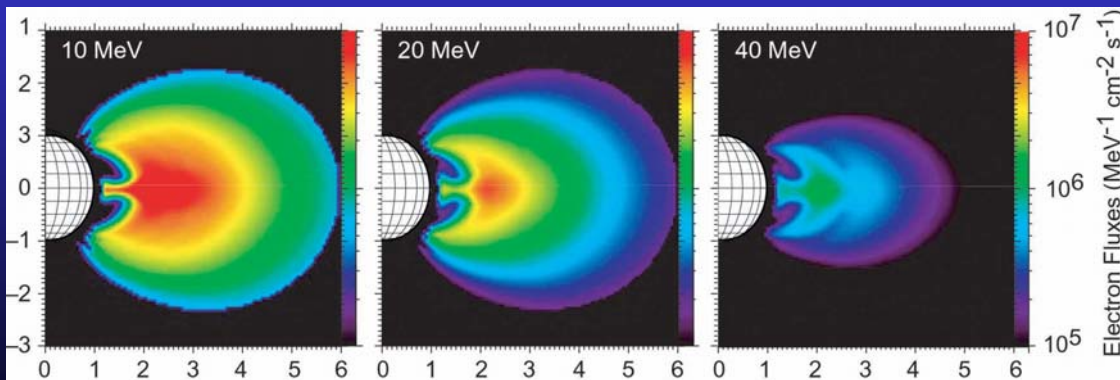
Jupiter's inner radiation belts inside $r = 5 R_J$



discovered after the detection of bursts in the radio waves Burke and Franklin (1955):

synchrotron emission from trapped particles in radiation belts was used to determine the rotation period

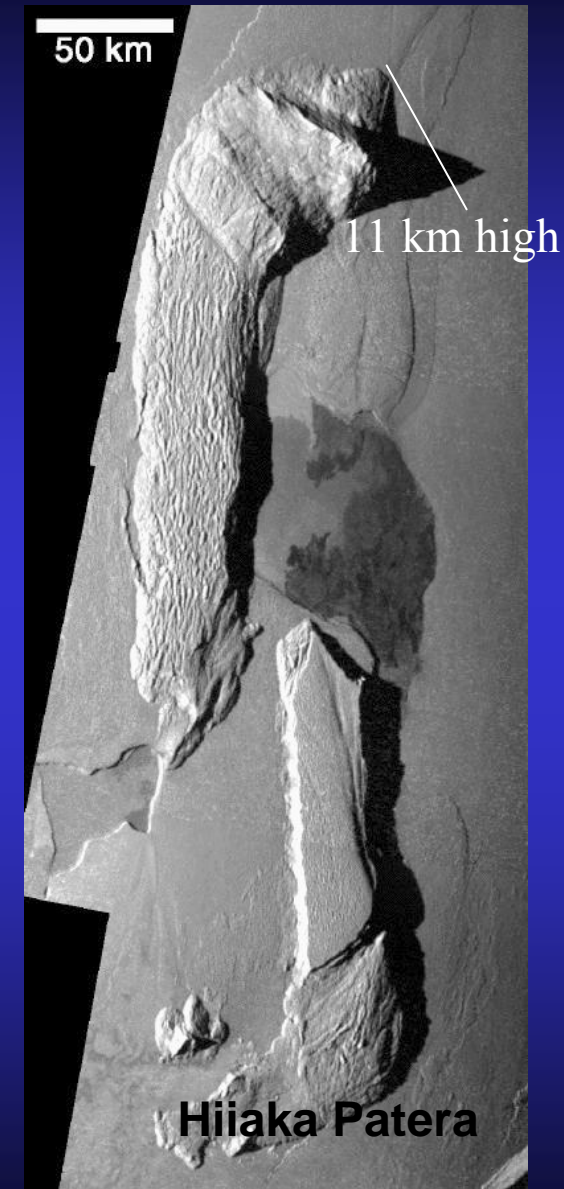
particles in this region interact with the moons (Metis, Adrastea, Amalthea, Thebe); the Jovian rings



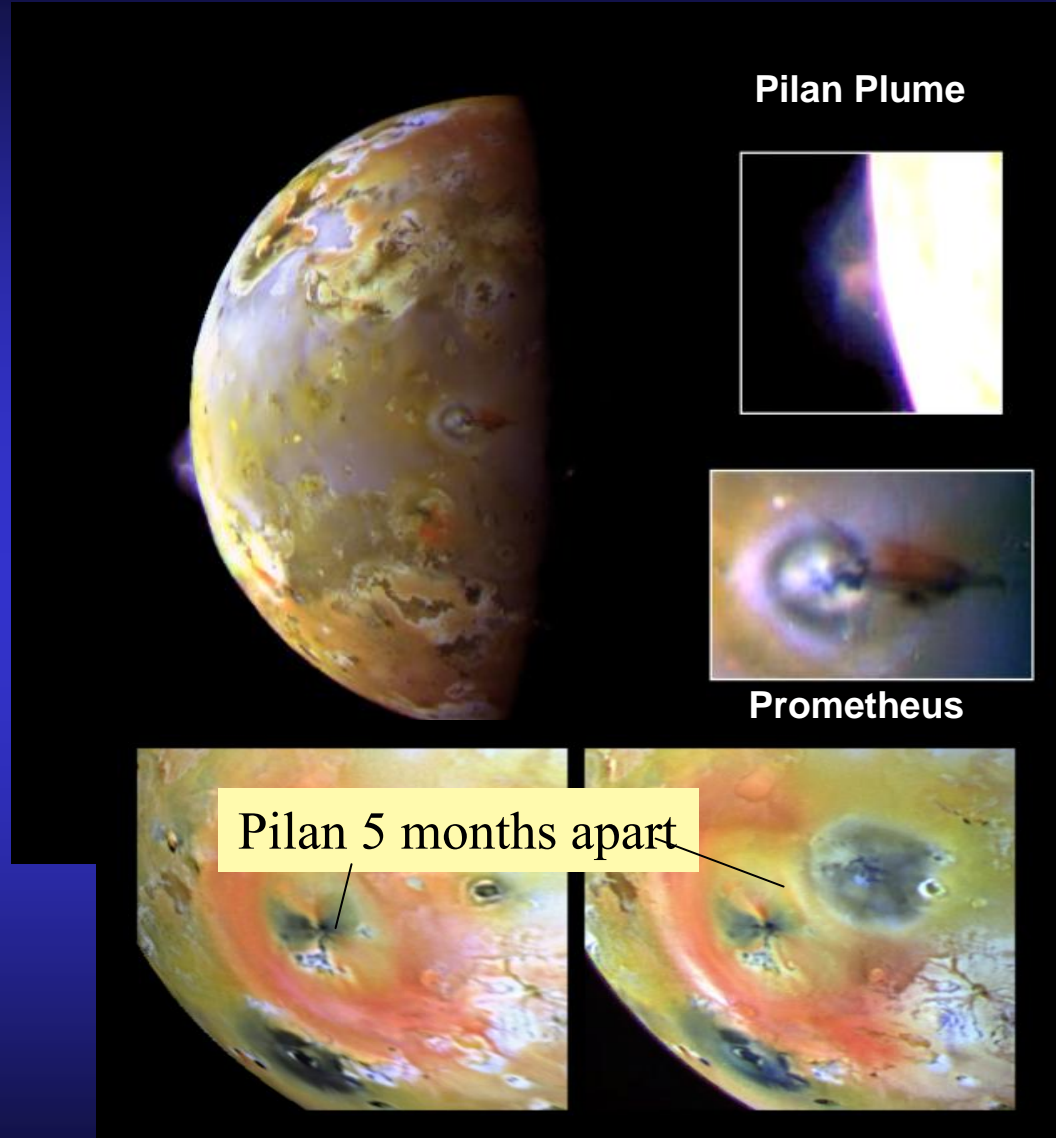
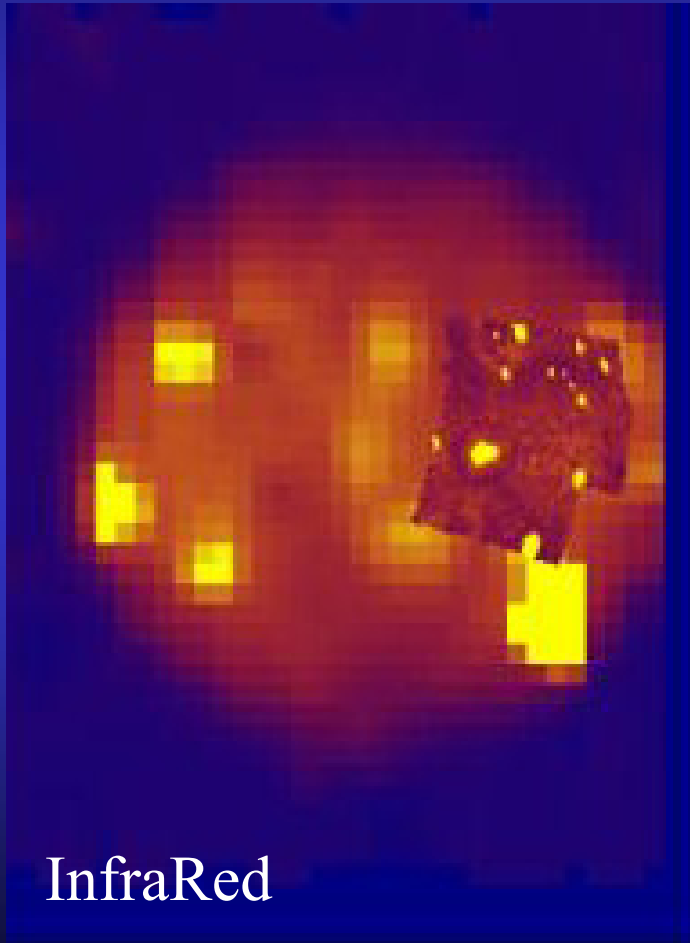
Jupiter's moon Io

source of sulfur and oxygen in Jupiter's magnetosphere

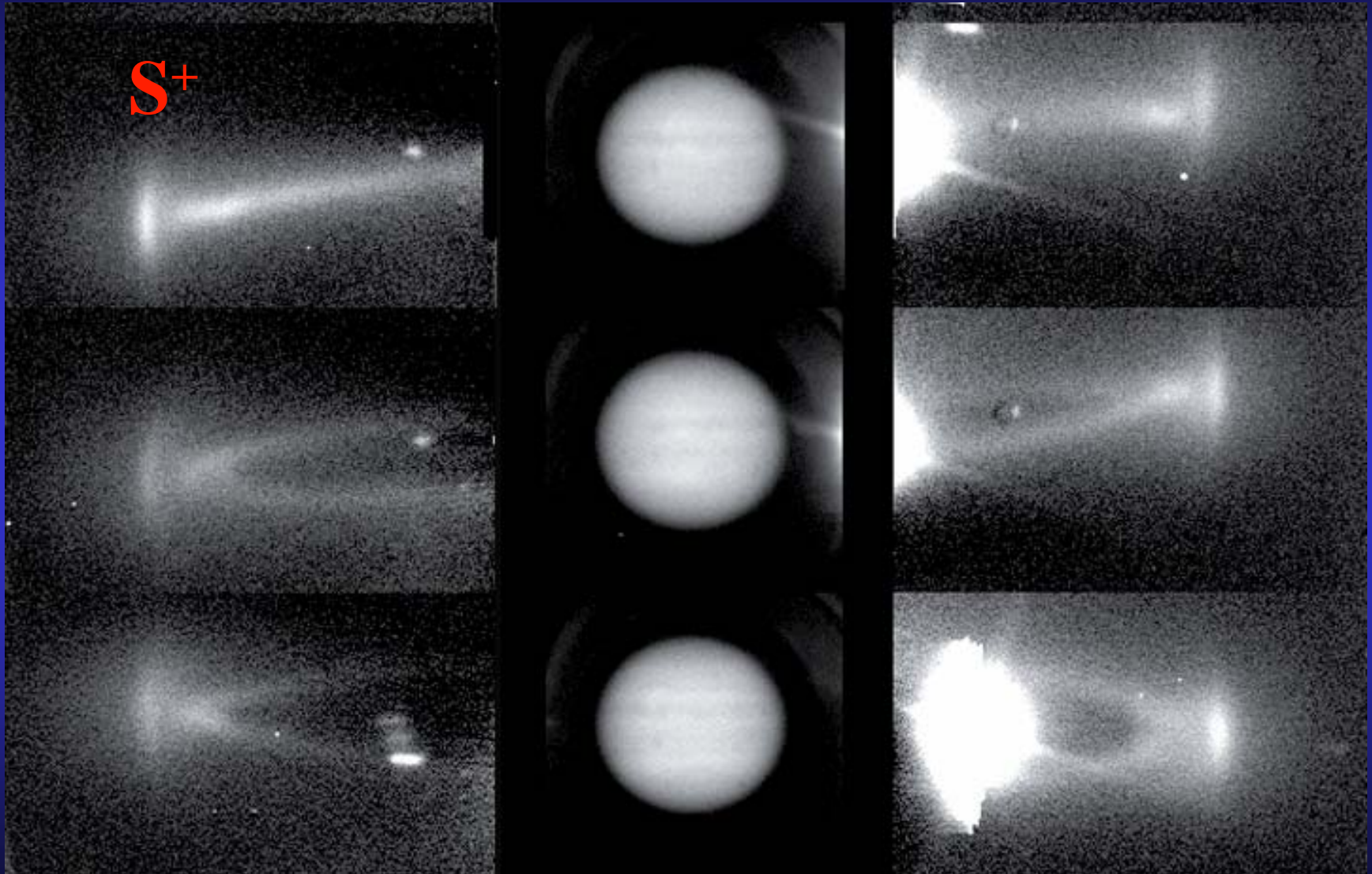
After quantities of lava are removed from below, the crust cracks and tilts, making tall, blocky mountains.



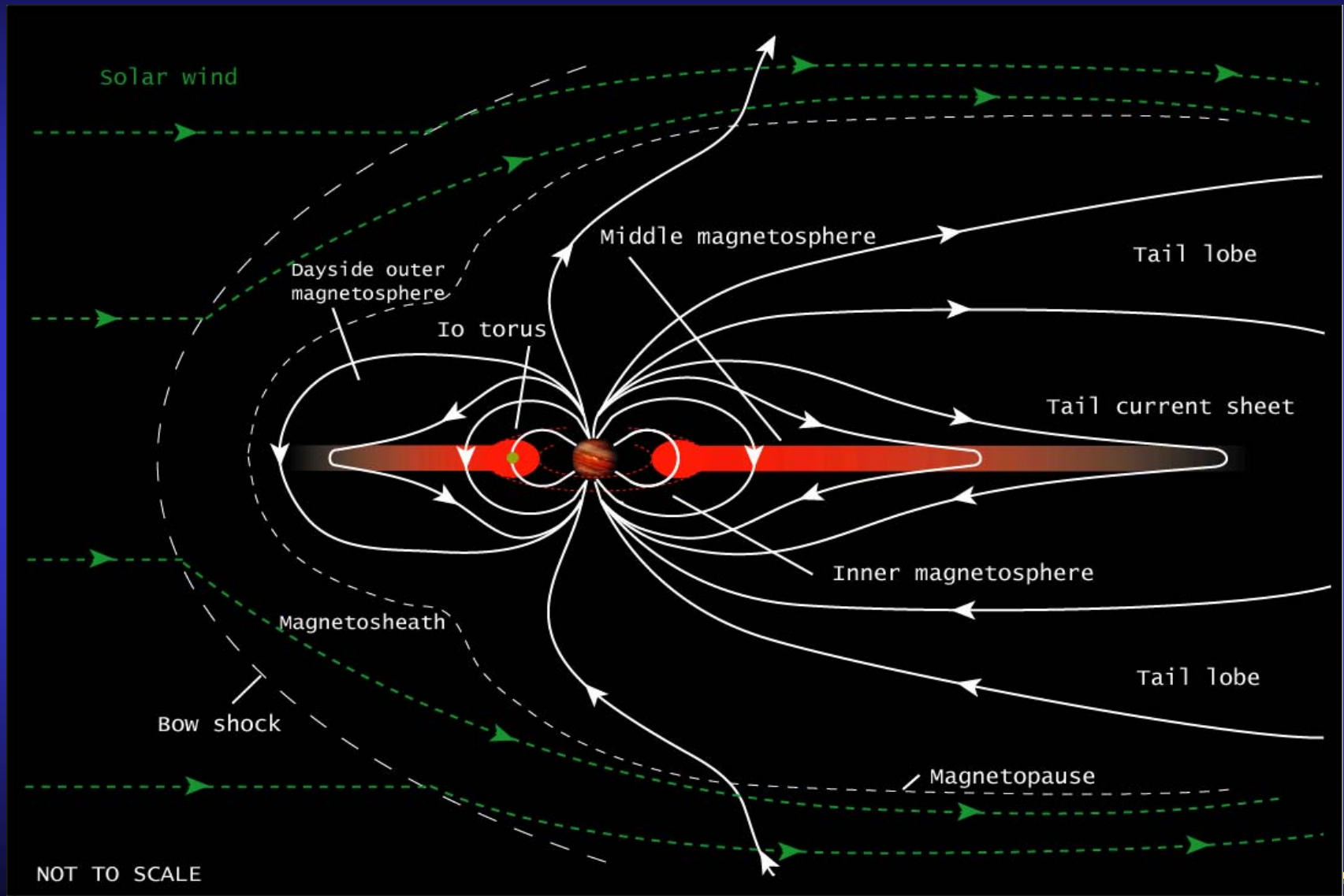
Io's volcanoes and geysers



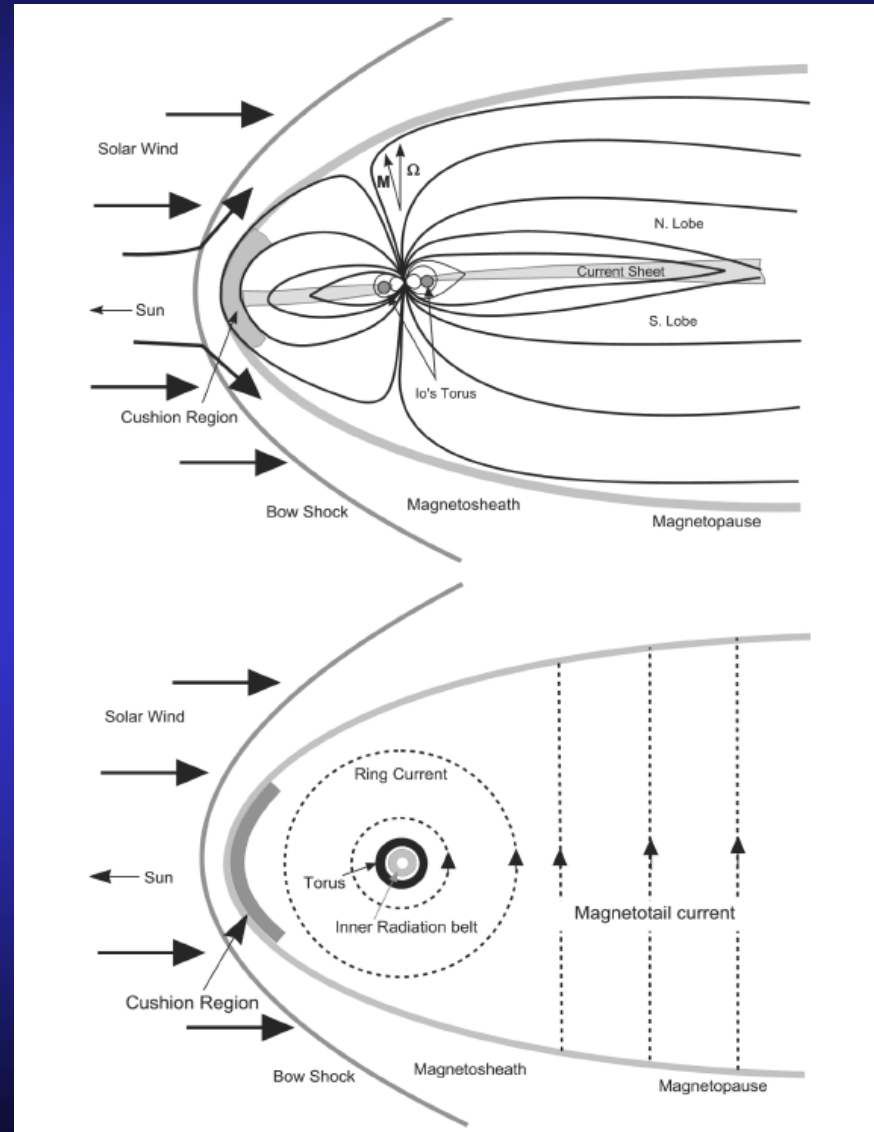
Io Plasma Torus (Schneider and Trauger)



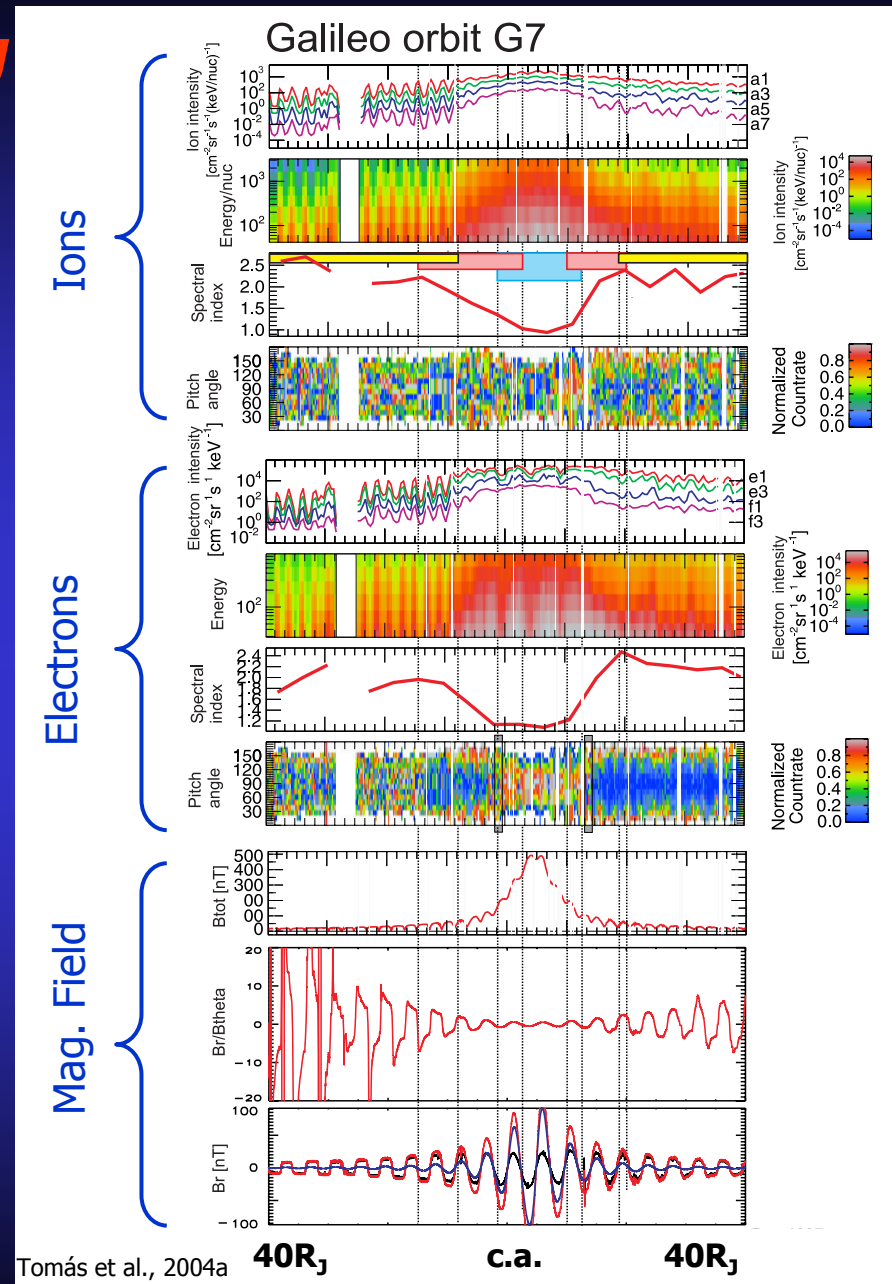
Jupiter's magnetosphere



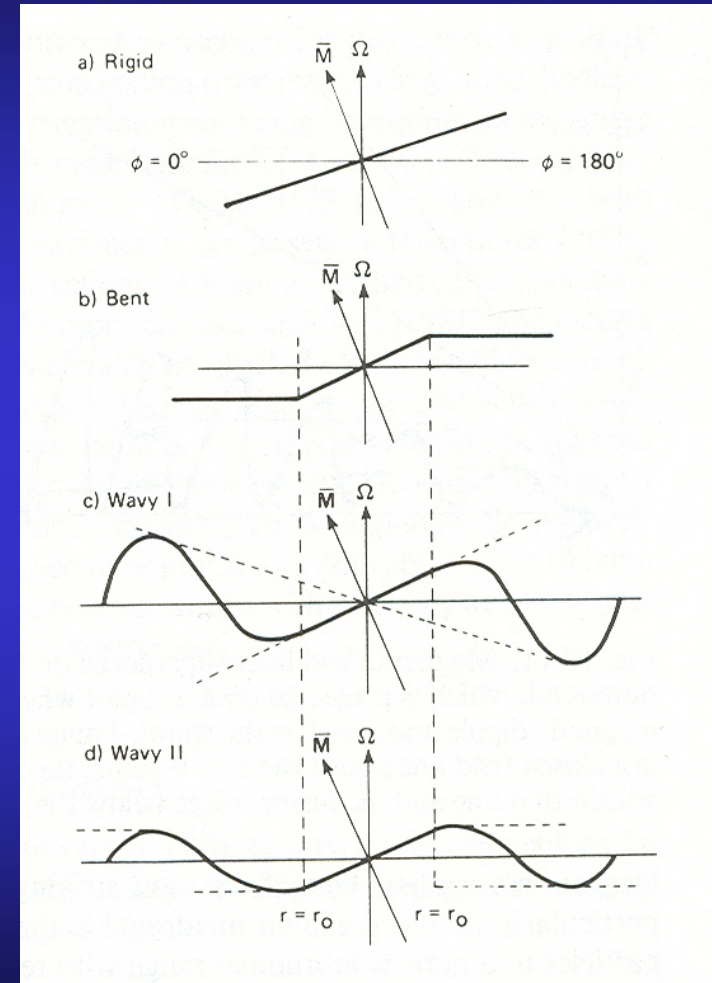
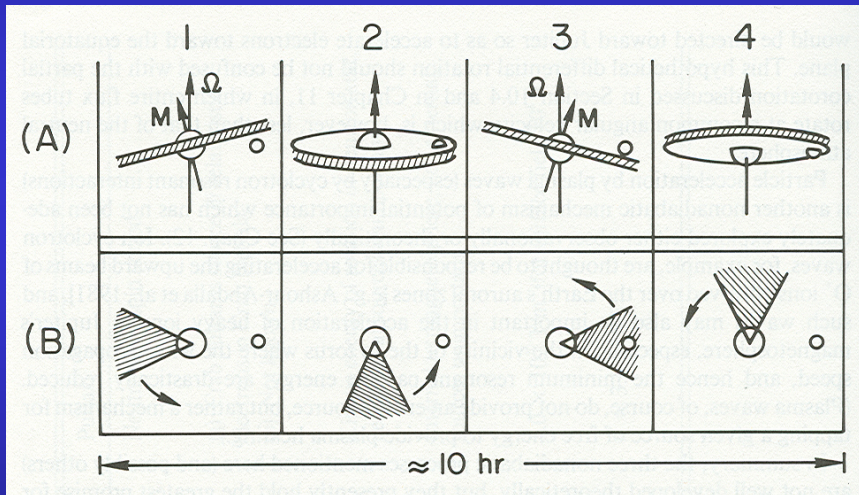
Regions in Jupiter's magnetosphere



Particles inside 40 R_J

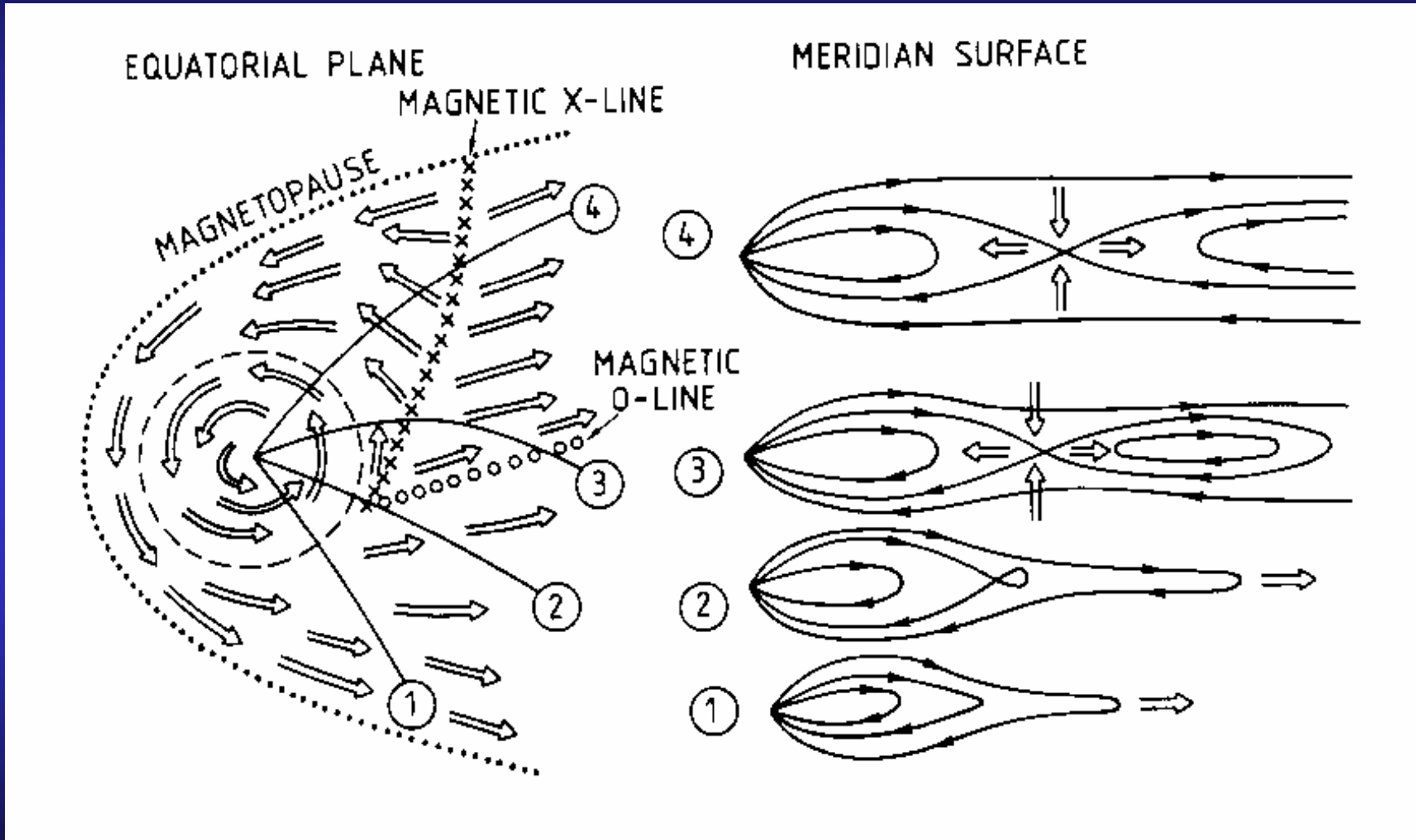


Periodic modulation of particle and field parameter



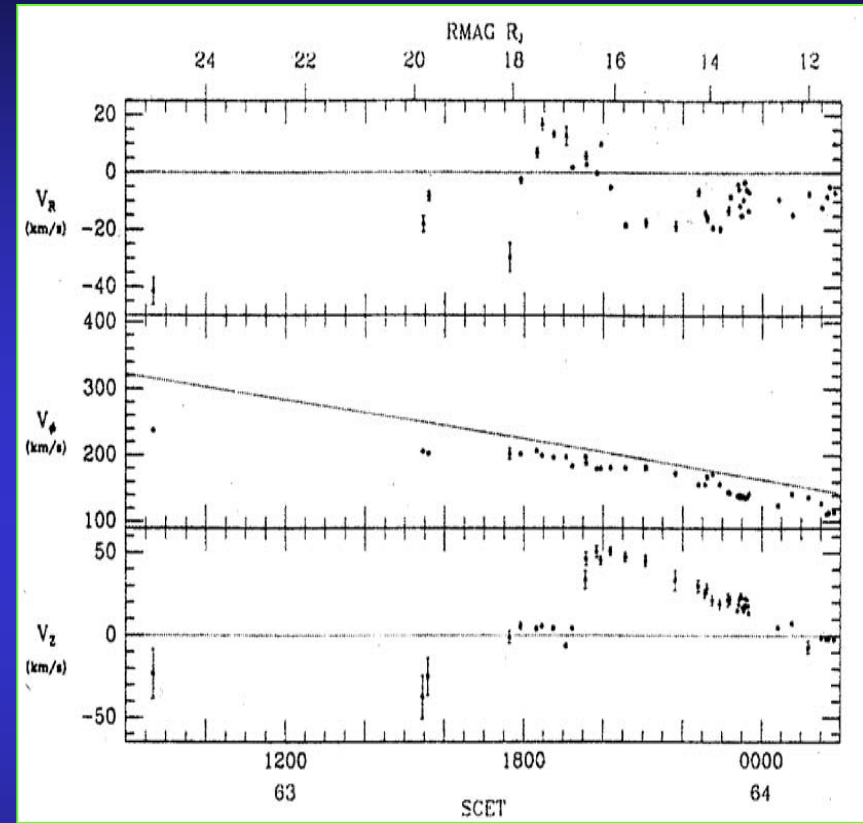
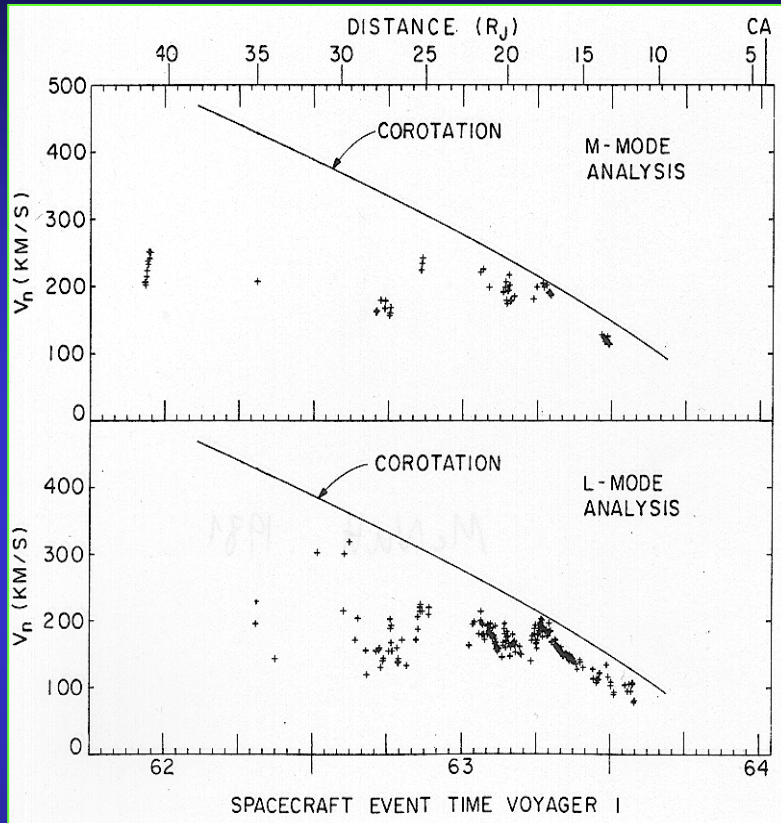
Jupiter

Structure and dynamics of the outer magnetosphere



Vasyliunas 1983

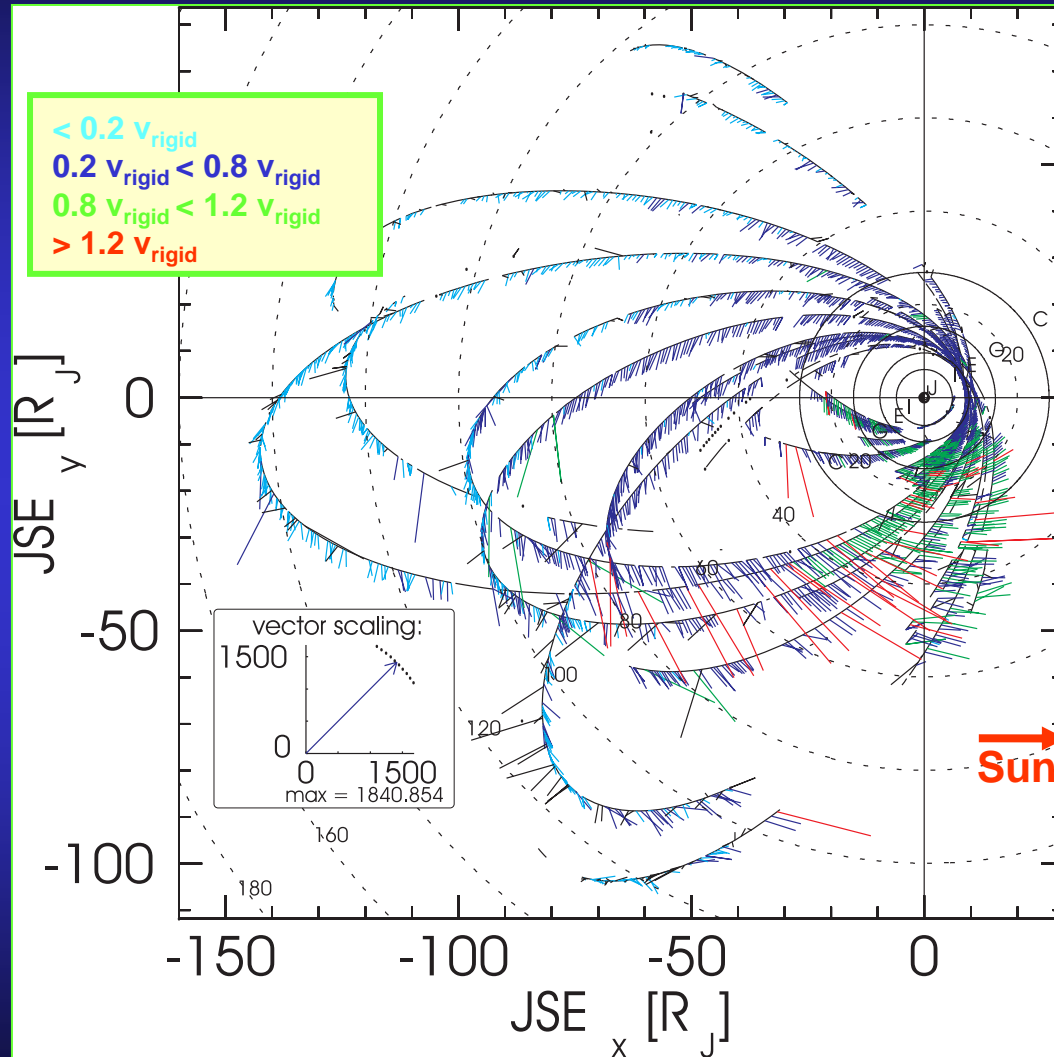
Flow measurements in Jupiter's magnetosphere



- **Voyager 1 PLS results**
 - McNutt et al., JGR, 86, 8319, 1981
 - Sands and McNutt, JGR, 93, 8502, 1988
- **Velocity lags rigid corotation trend to “constant” velocity outside 20 R_J**

Global Flow Pattern in Jupiter's equatorial plane

Galileo/EPD results



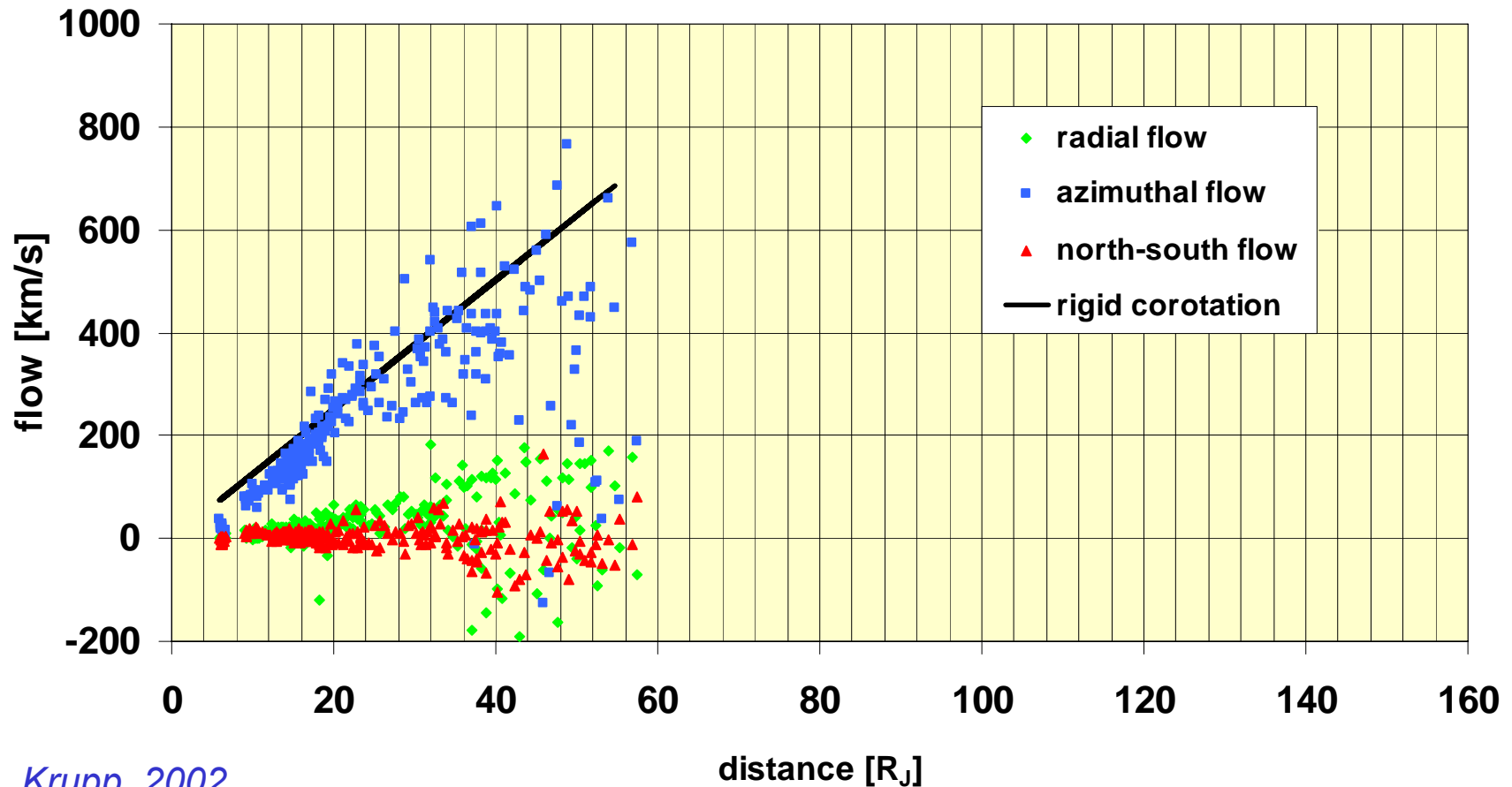
- flow is predominantly in corotation direction
- temporal stable in this averaged view
- flows in the deep magnetotail still in corotation direction, however substantially subrotational
- deviation from „normal“ state due to dynamic processes
- larger flows with radial outward components (100-200 km/s) at dawn compared to smaller flows with small radial inward components at dusk (50 km/s)

Krupp et al., 2001

Global Flow Pattern in Jupiter's equatorial plane

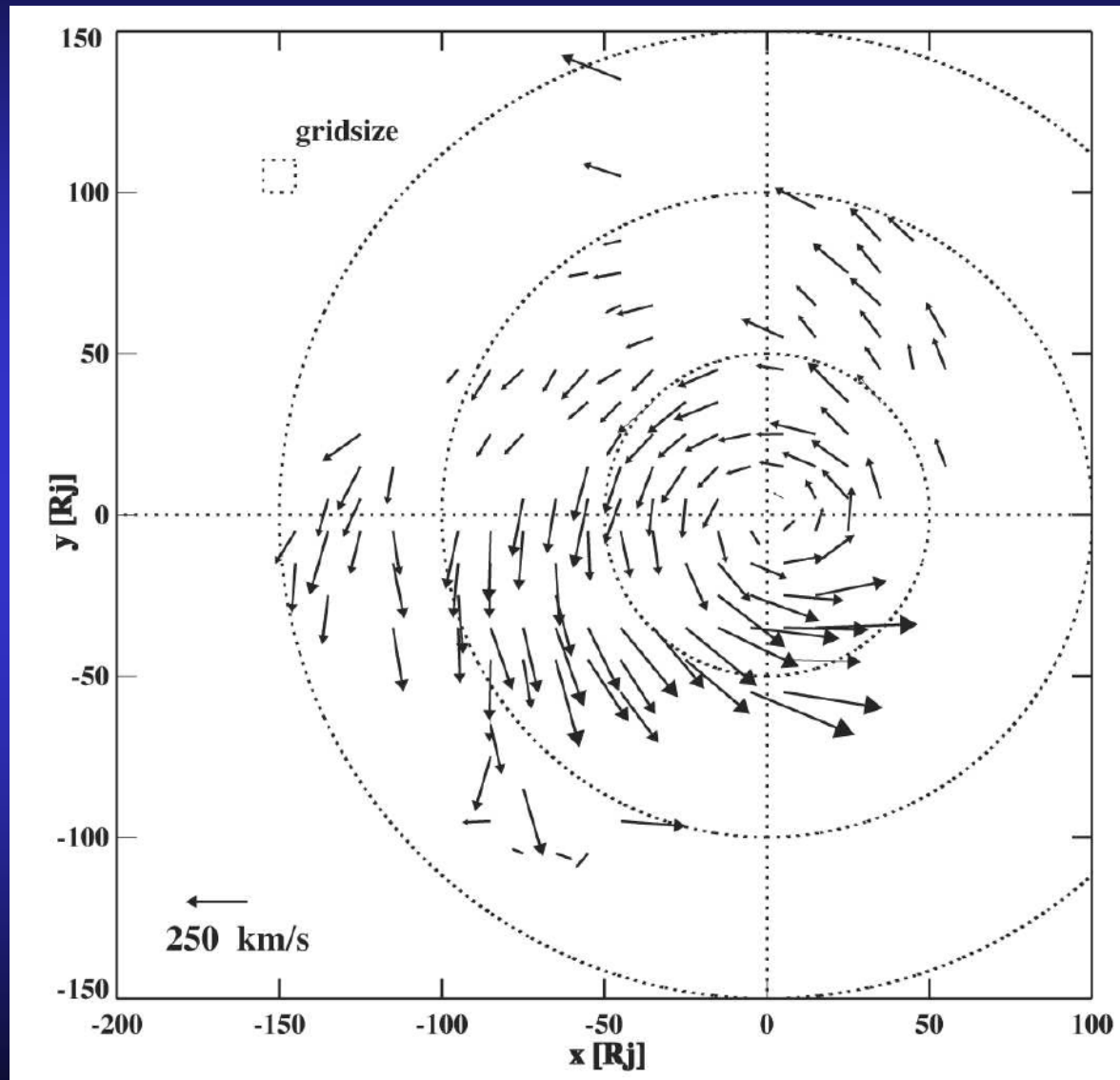
strong local time asymmetry between dawn and dusk

Flow LT 05:00-07:00

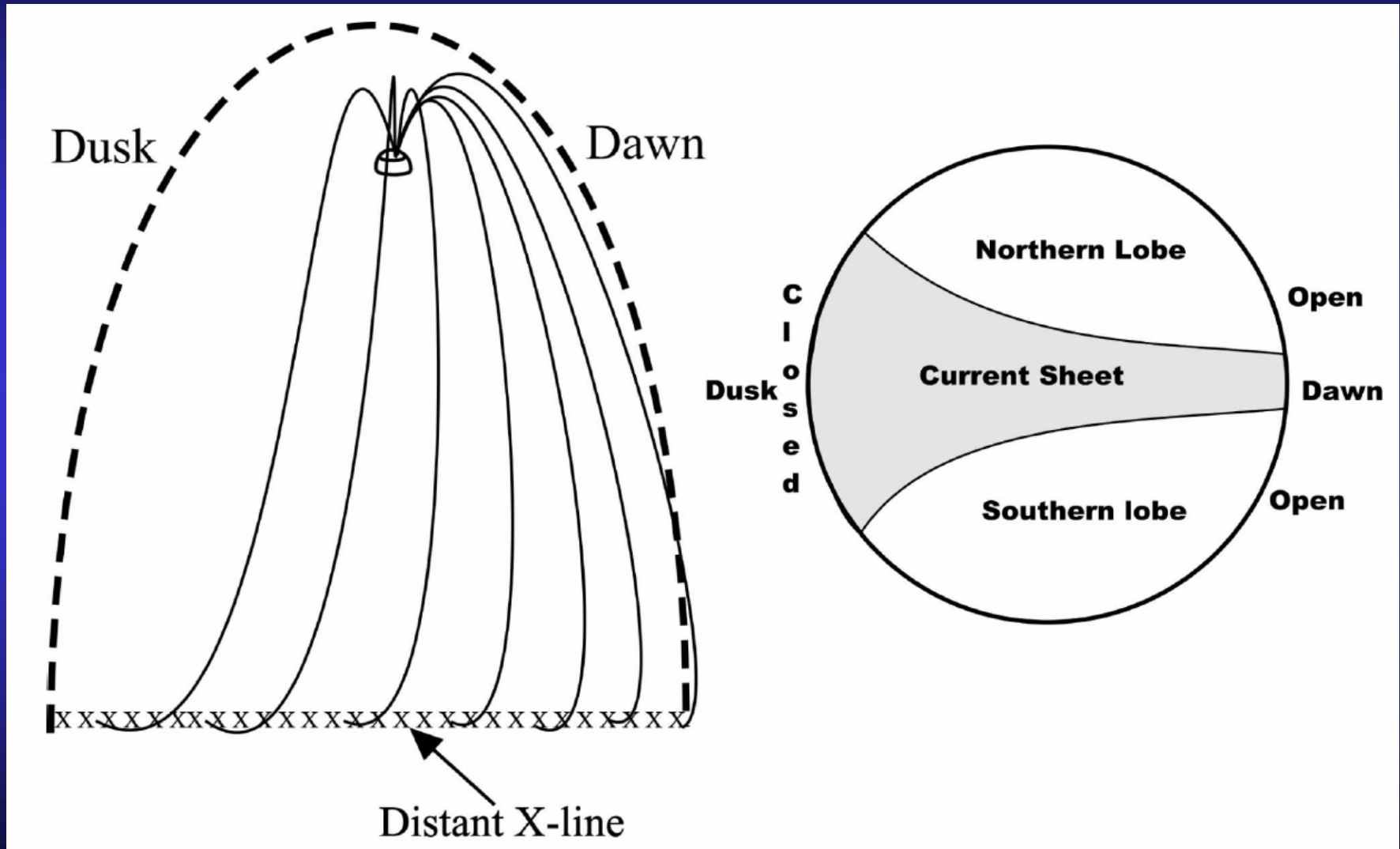


Krupp, 2002

Averaged flow pattern in the equatorial plane

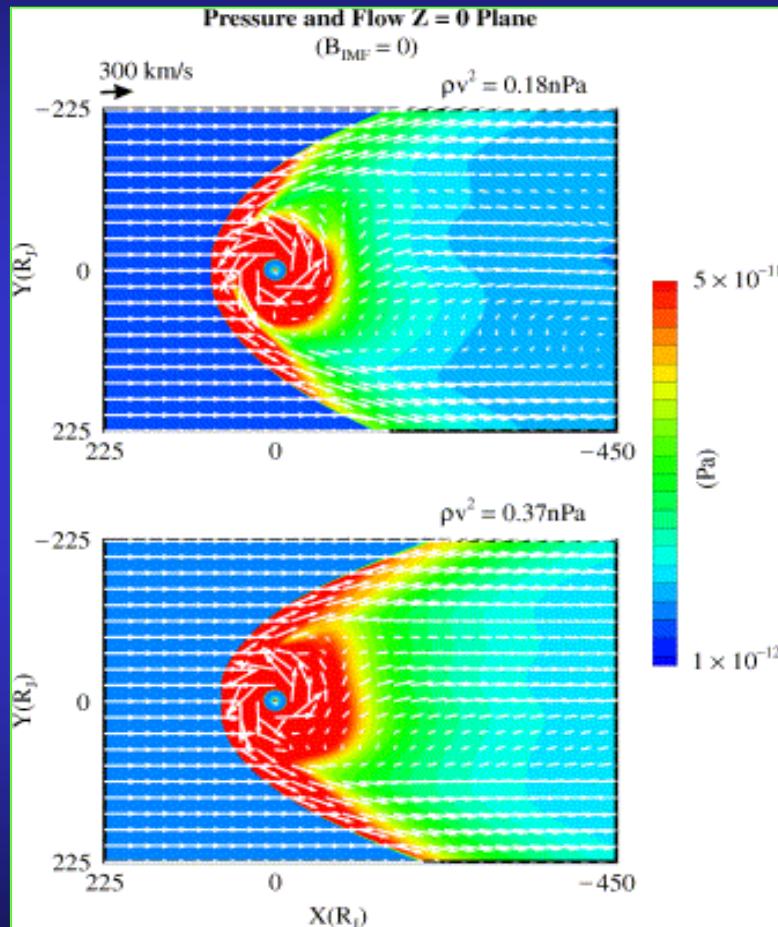


Configuration of magnetotail field lines and current sheet thickness

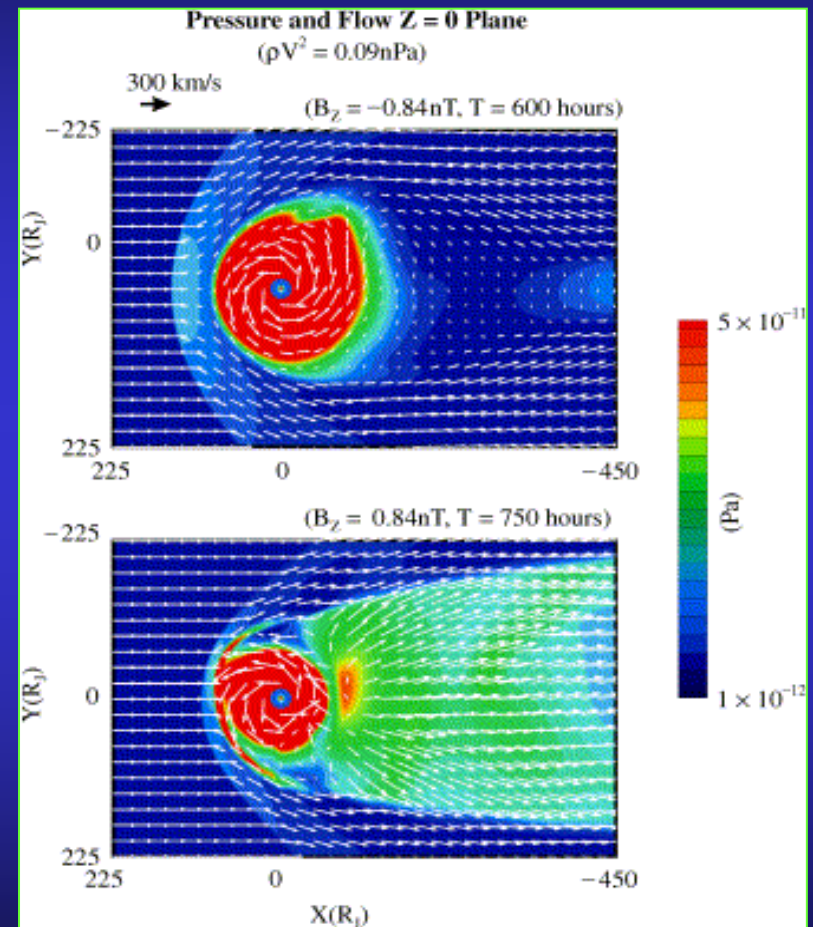


MHD simulations of the Jovian magnetosphere

IMF=0

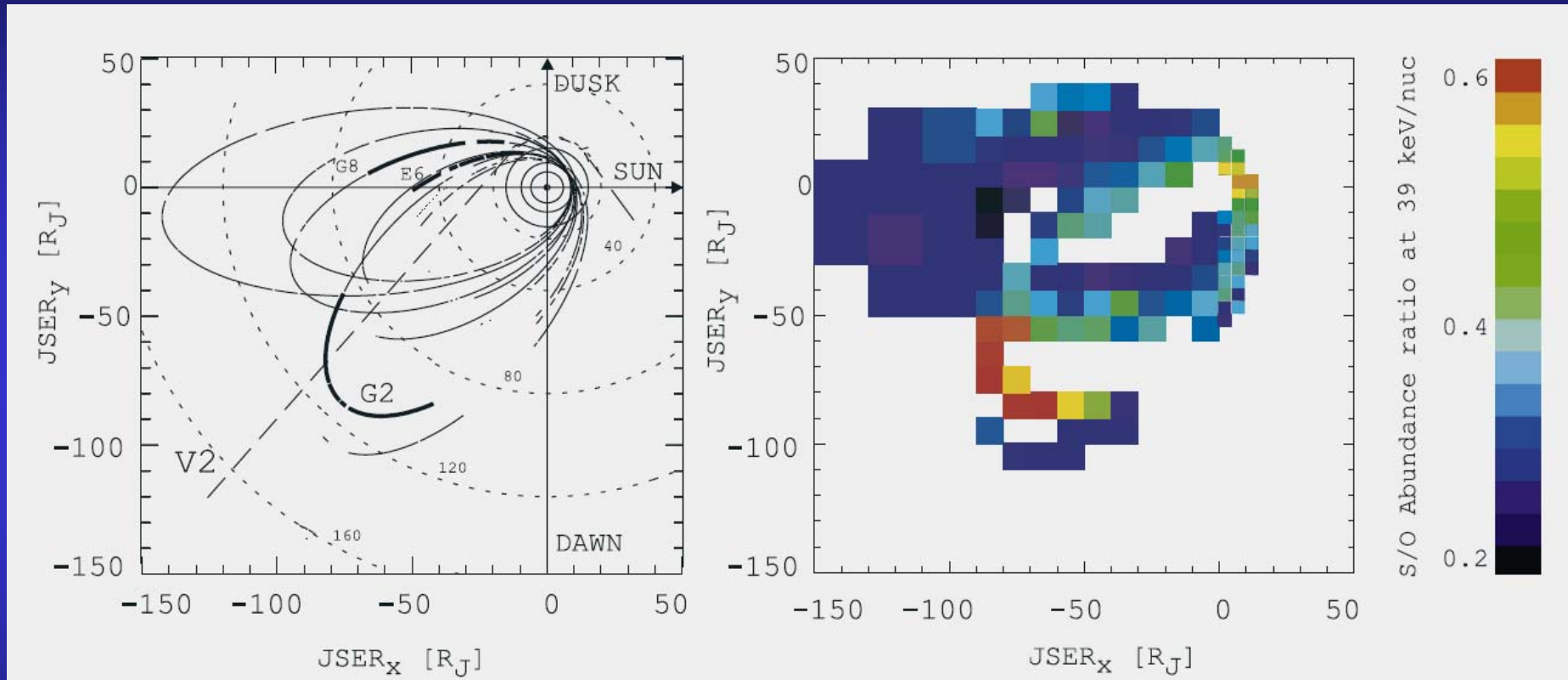


IMF=southward (top) and
northward (bottom)



Walker, 2001

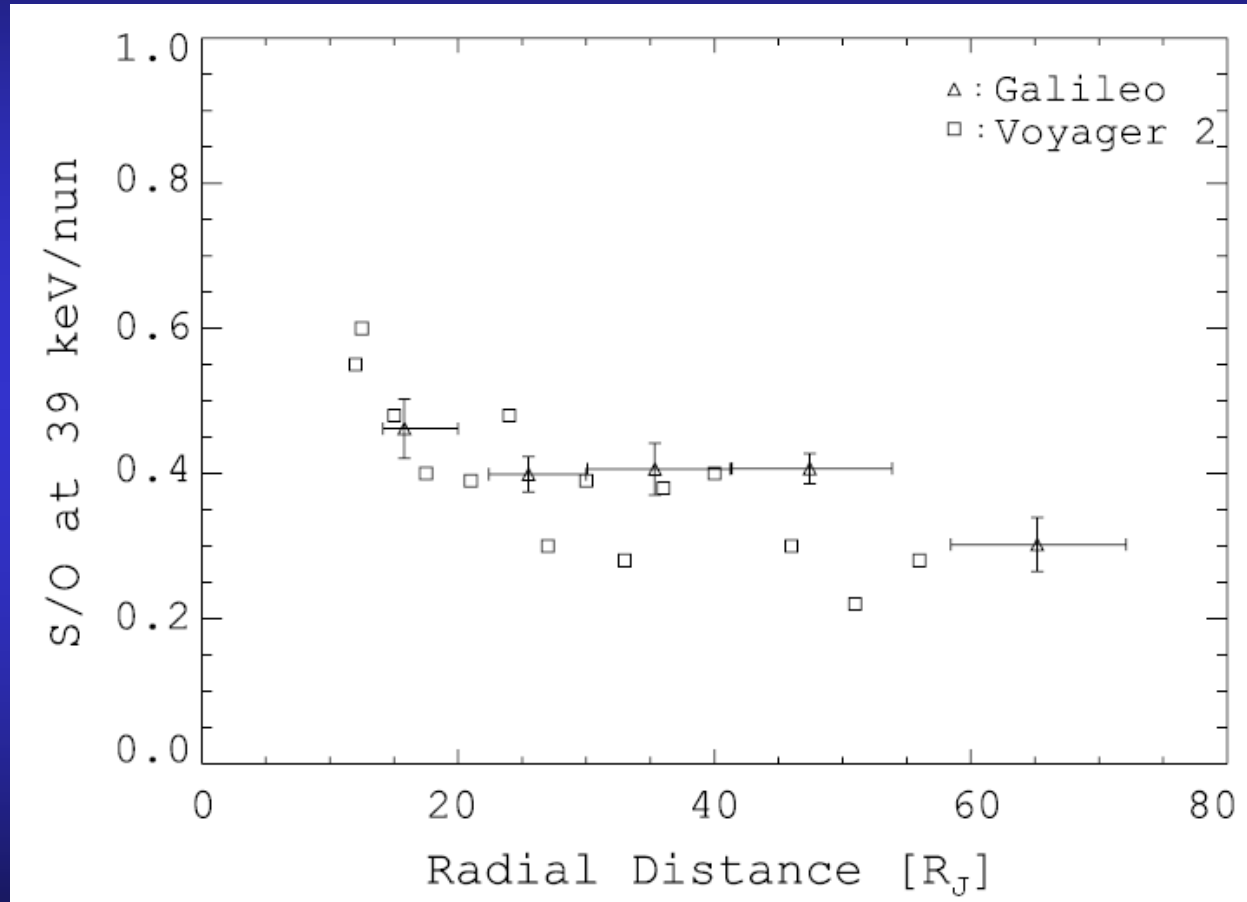
First global ion composition ratios of the Jovian magnetosphere



Radioti et al., 2005

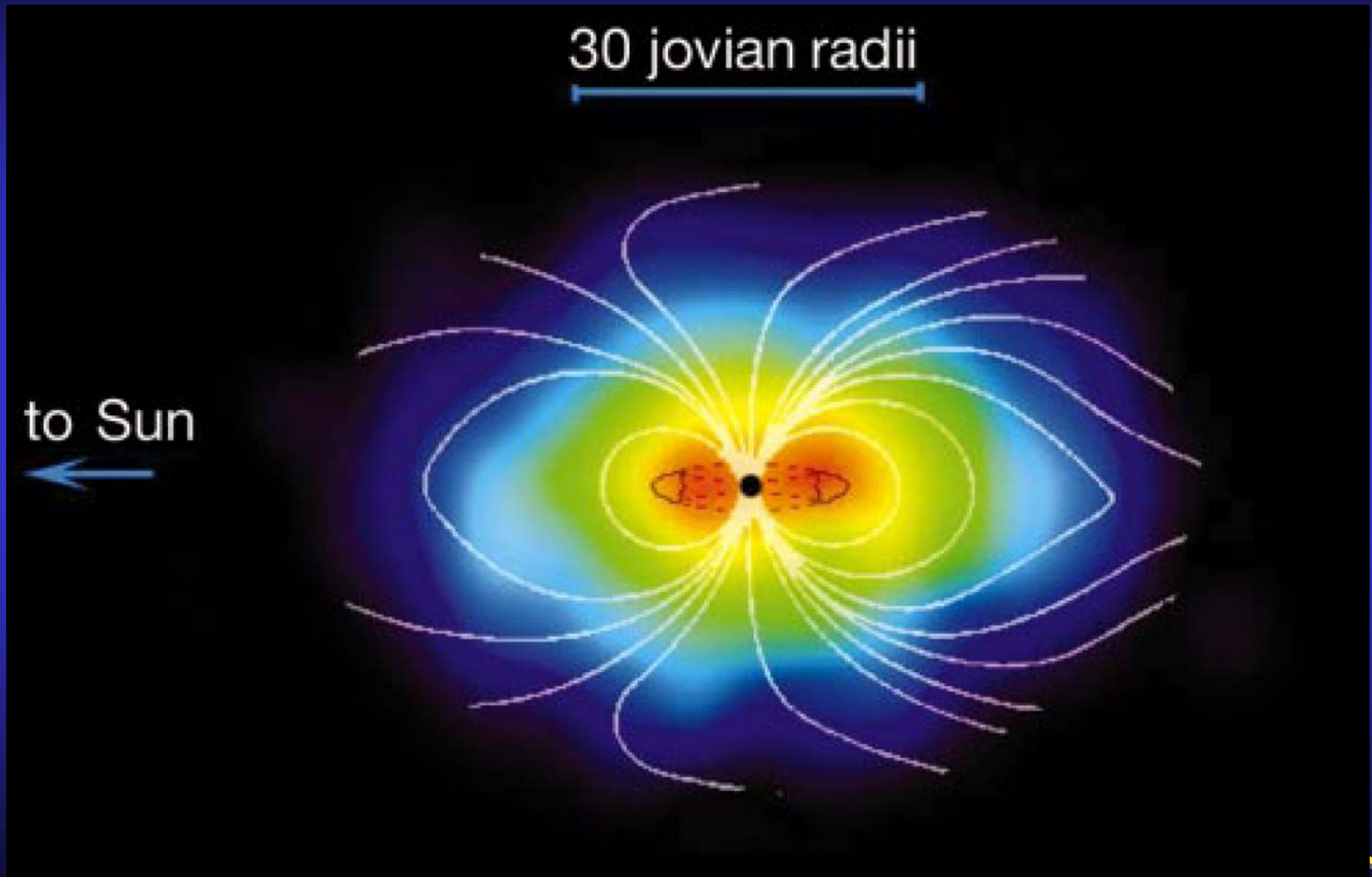
First global ion composition ratios of the Jovian magnetosphere

Galileo-Voyager 2 comparison

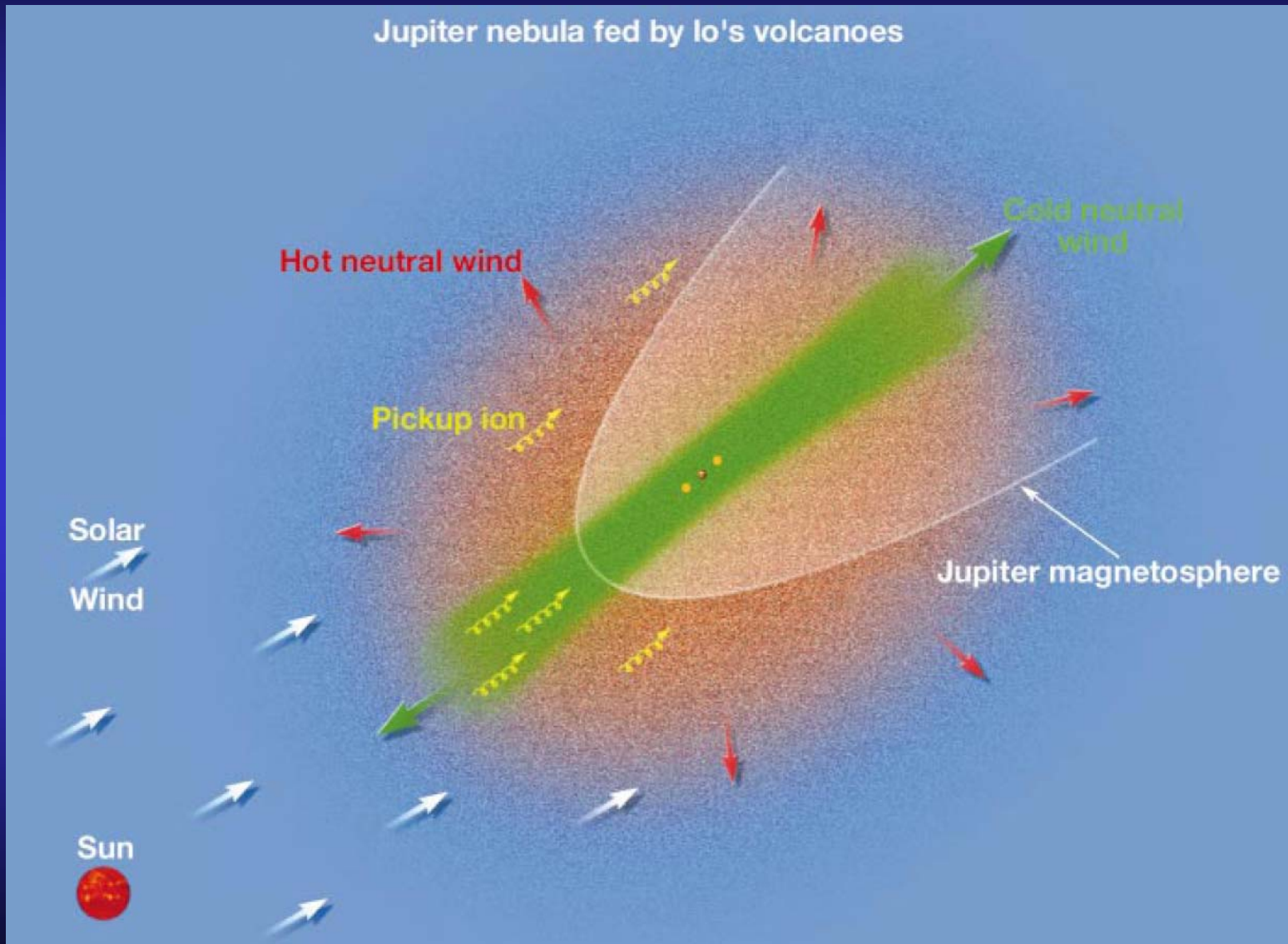


Radioti et al., 2005

Jupiter as a source of hot neutrals



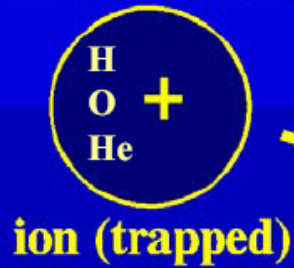
Jupiter as a source of hot neutrals



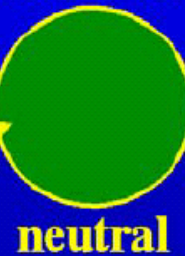
Energetic Neutral Atom (ENA) imaging

CHARGE EXCHANGE PROCESS

ENERGETIC



ENERGETIC



escape

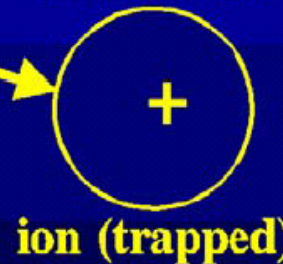


charge
exchange

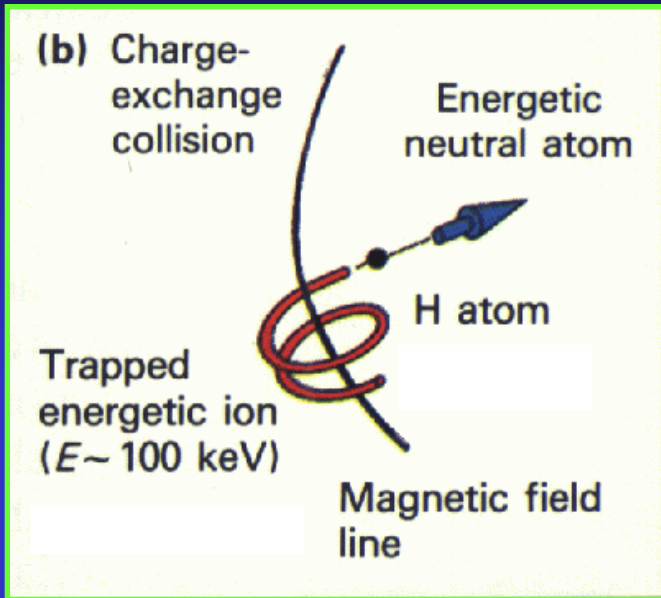
THERMAL



THERMAL



ENA principle



The co-existence of an energetic charged particle population (solar wind, magnetospheric plasma) and a planetary neutral gas leads to interaction, e.g., through charge-exchange:



Little exchange of momentum \rightarrow conserve velocity
 ENA are not influenced by E- and B-fields; they travel on straight ballistic path like a photon
 Directional detection of ENAs yields a global image of the interaction and allows to deduce properties of the source populations.

ENA production mechanism in space plasmas

Charge - exchange reaction with atmospheric / exospheric gases

Sputtering of planetary atmospheres

Backscattering from the planetary atmospheres (ENA albedo)

Sputtering from planetary surfaces

Ion neutralization / sputtering on dust particles

Recombination (CMI)

ENA principle

The directional ENA flux (J_{ena}) at a point in space represents an integral along the chosen line-of-sight of the product of the hot ion flux toward the observation point ($j_{ion}(\mathbf{r}, \mathbf{v}, t)$), the cold neutral density ($n_{neutral}(\mathbf{r}, t)$), and the charge exchange cross section. That is,

$$j_{ENA} \cong \int_0^{\infty} dr \times j_{Ion}(\vec{r}, \vec{v}, t) \times n_{Neutral}(\vec{r}) \times \sigma_{CE}(|\vec{v}|)$$

where

\mathbf{r} is the location along the line-of-sight at which the charge exchange interaction occurs,

\mathbf{v} is the ion vector velocity at the instant of the interaction

t time

Dynamics of the Jovian magnetosphere

radial transport

interchange motion

injections

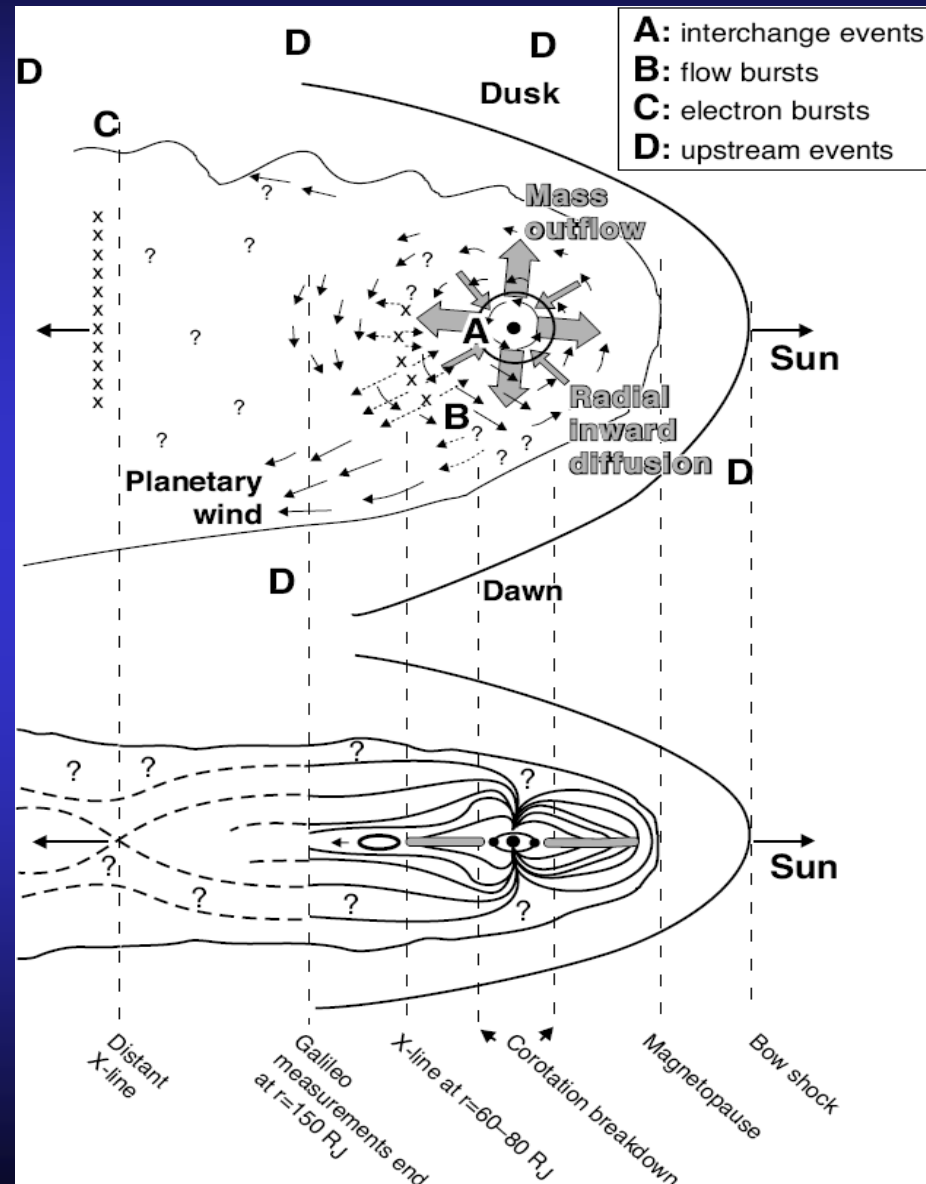
plasma sheet dynamics

particle bursts

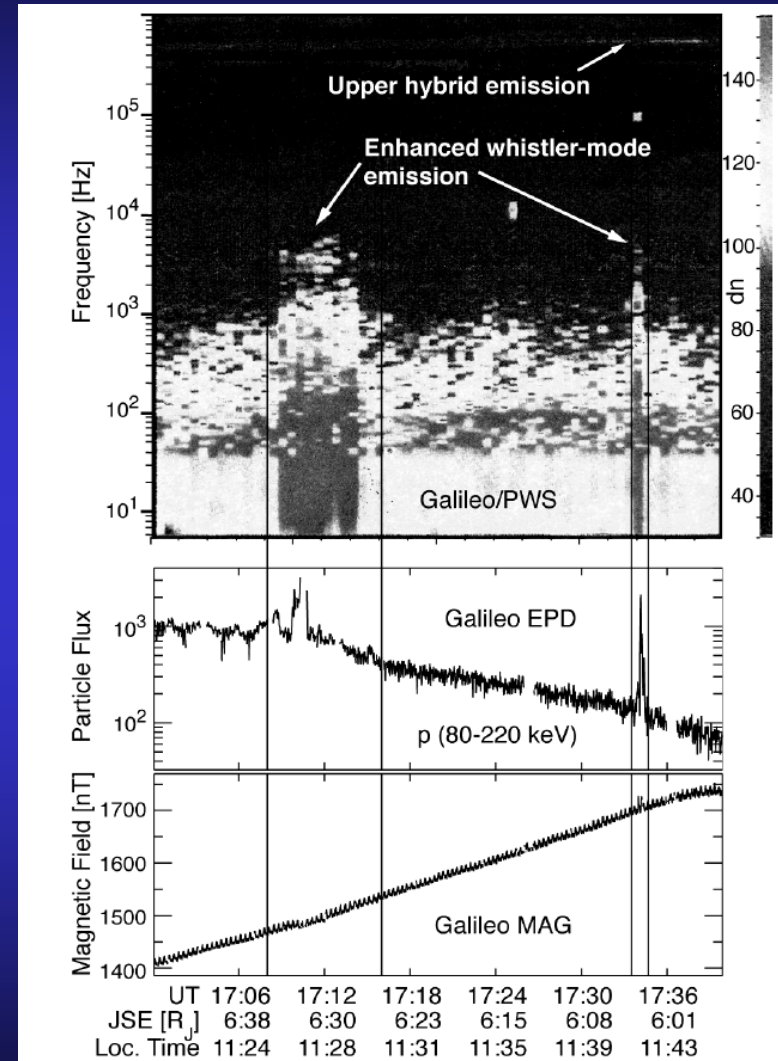
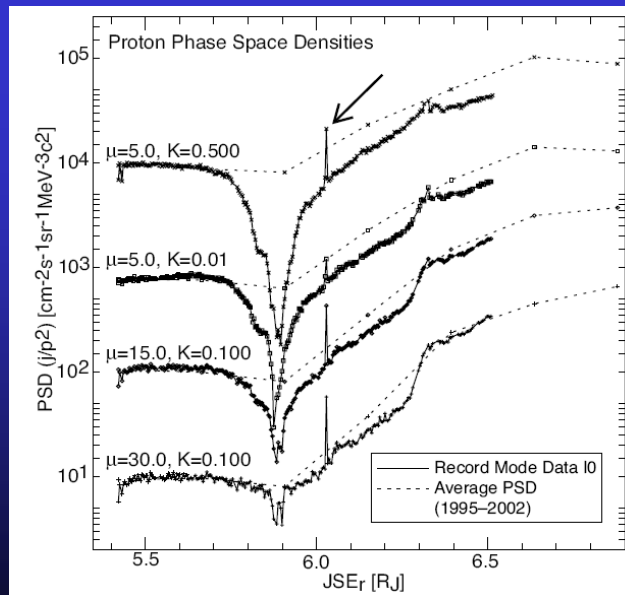
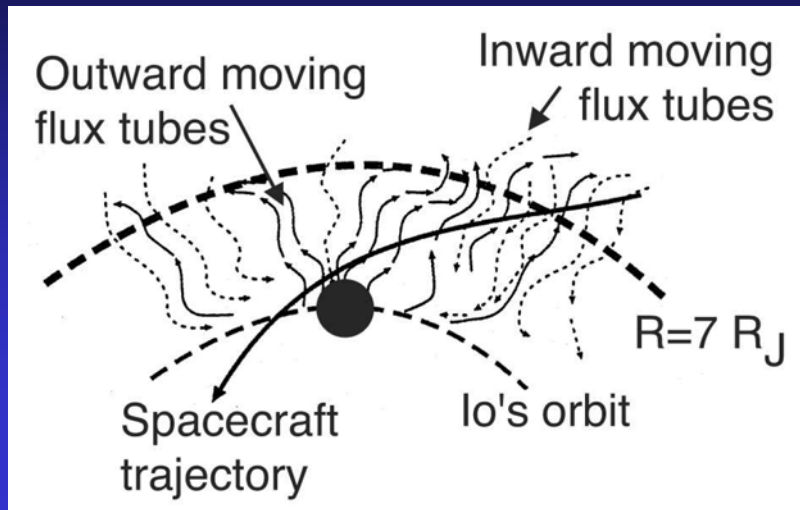
boundary phenomena

aurora

Jupiter - Particle motion in the magnetosphere

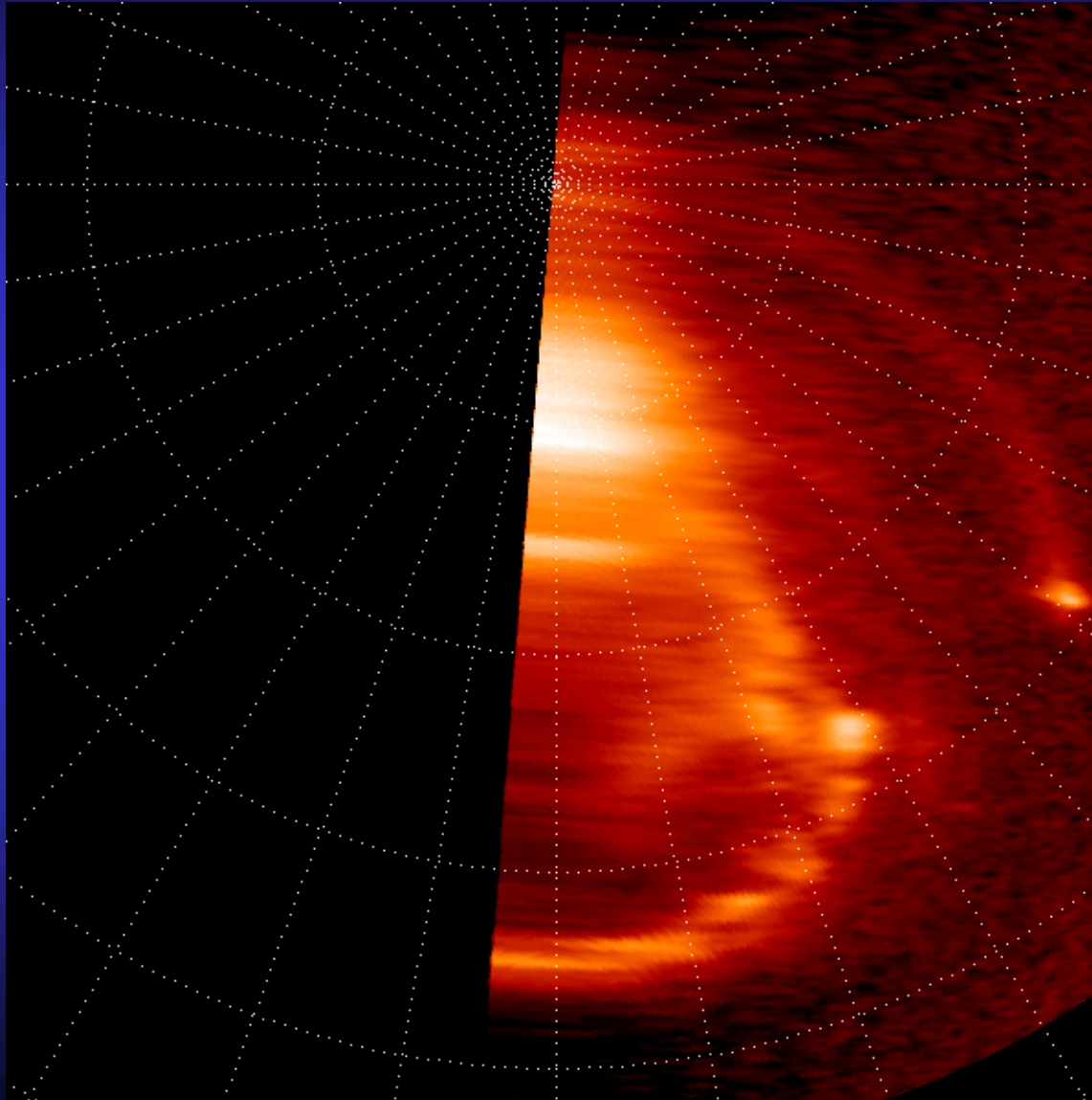


Interchange motion



Jupiter's Aurora - The Movie

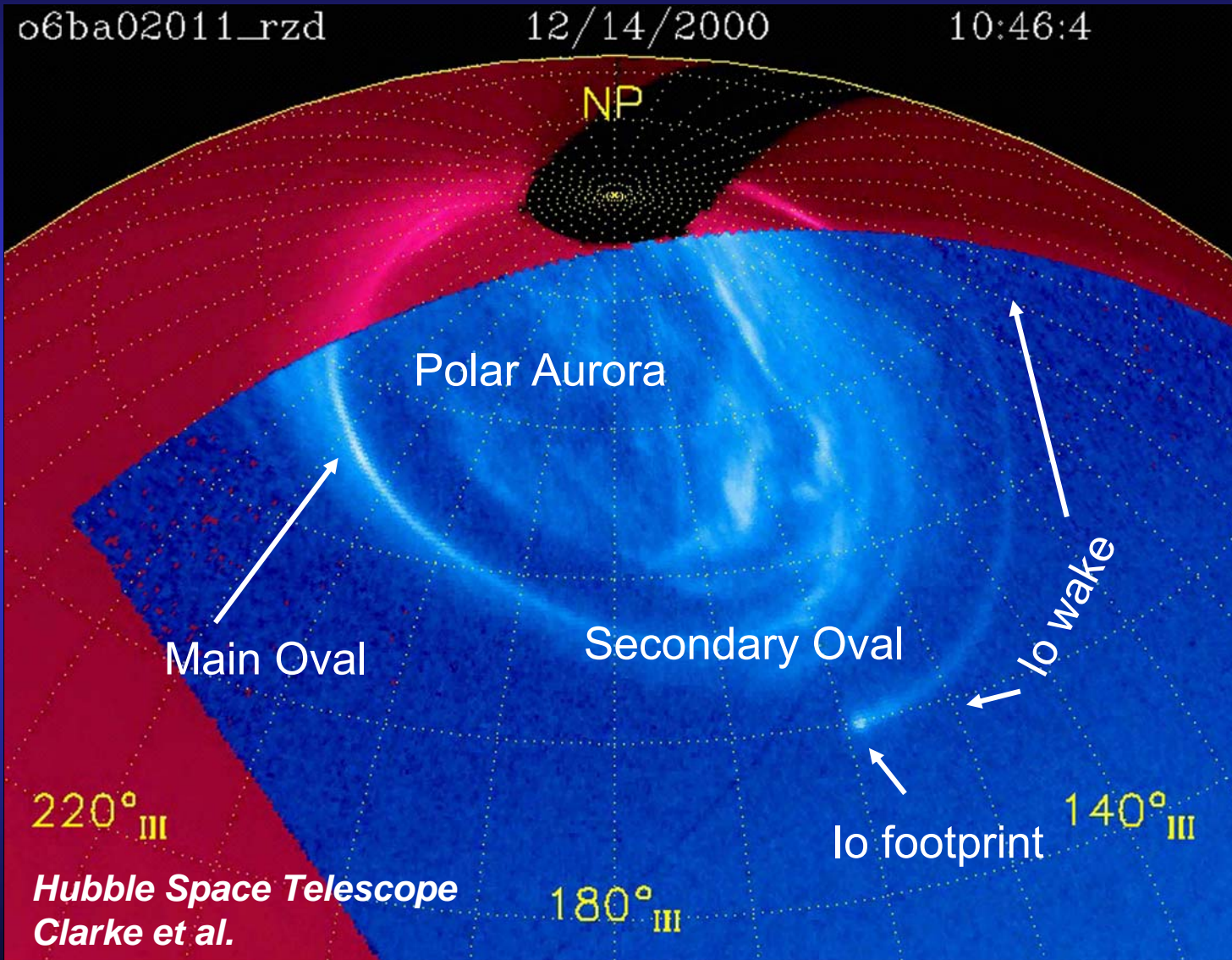
Fixed magnetic co-ordinates rotating with Jupiter



Clarke et al.
Grodent et al.
HST

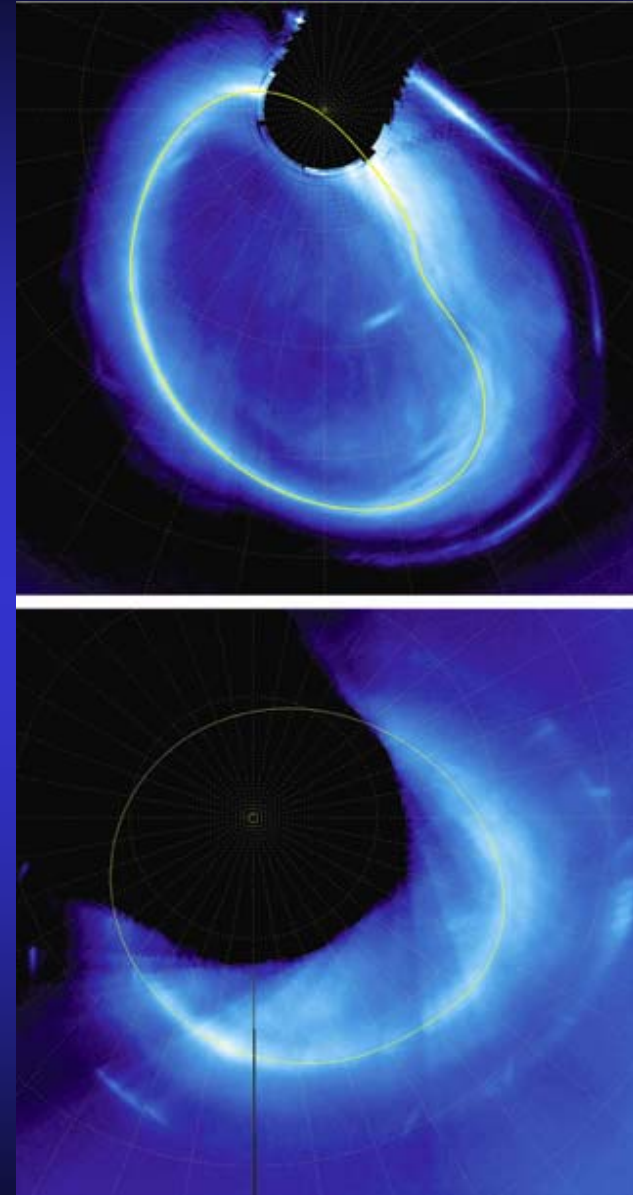
Jupiter

Different types of aurora



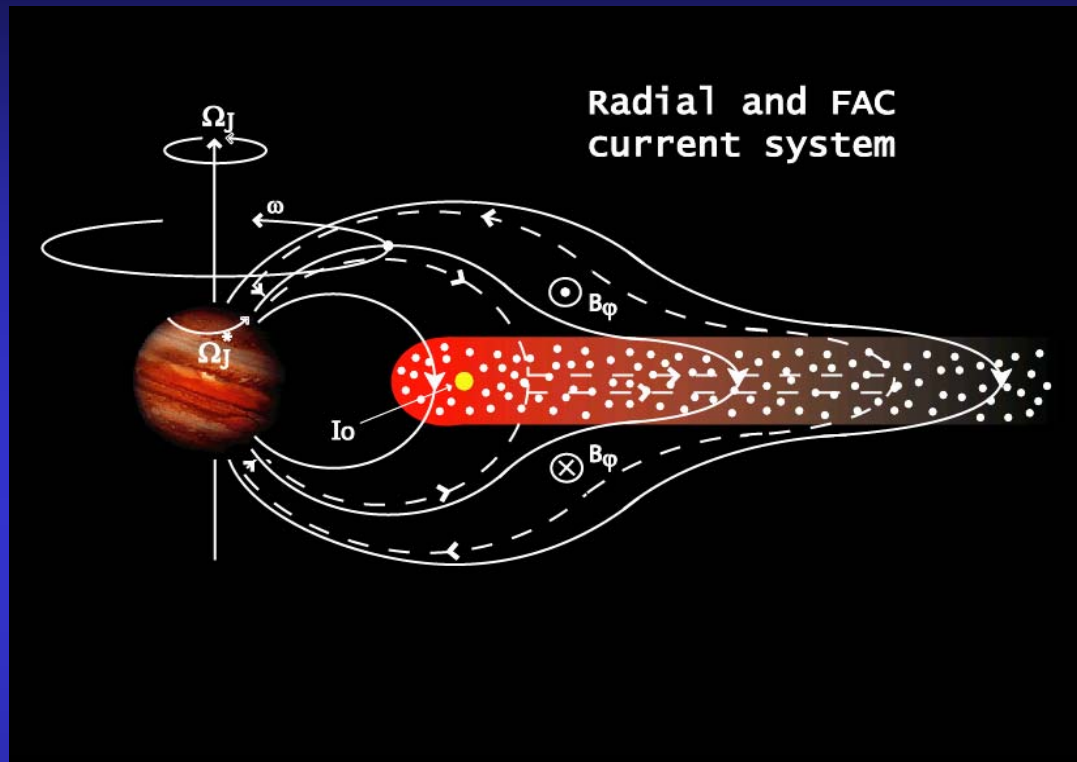
Jupiter`s main aurora

- Shape constant, fixed in magnetic co-ordinates
- Magnetic anomaly in north
- Steady intensity
- $\sim 1^\circ$ Narrow



Clarke et al., Grodent et al. HST

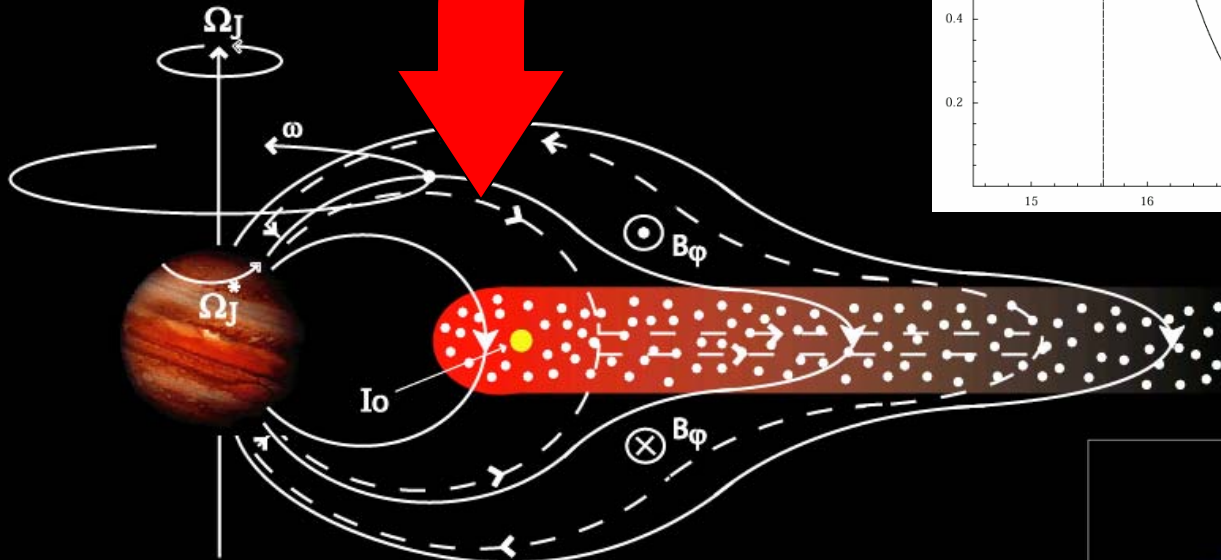
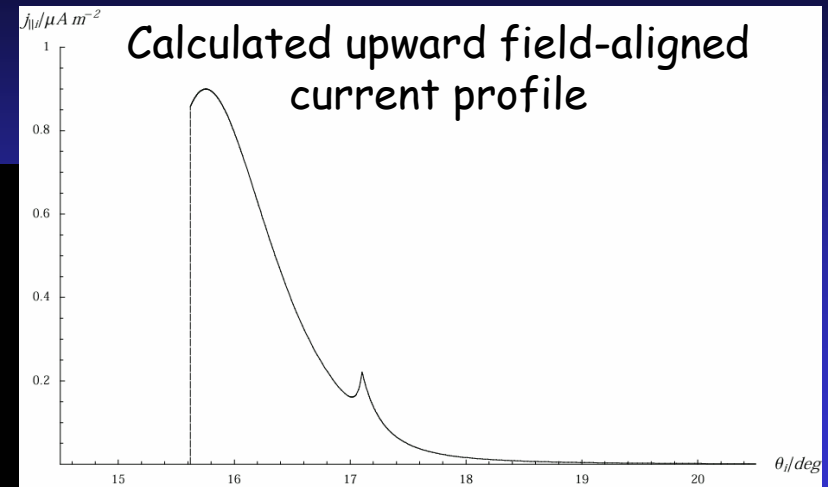
Large-scale current system in the Jovian magnetosphere



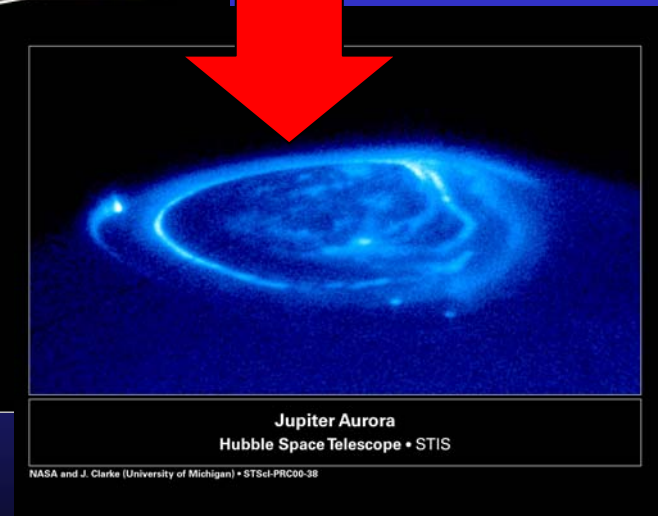
After Hill (1979)
and Vasyliunas (1983)

- Discovery of a local time asymmetry in the system of azimuthal currents which distend the field lines away from the planet (Bunce and Cowley, 2001a; Khurana, 2001)
- Investigations of field-aligned currents associated with magnetosphere-ionosphere coupling currents found to be $\sim 1 \mu\text{Am}^{-2}$ (Bunce and Cowley, 2001b; Khurana, 2001)

Origin of the Jovian main aurora

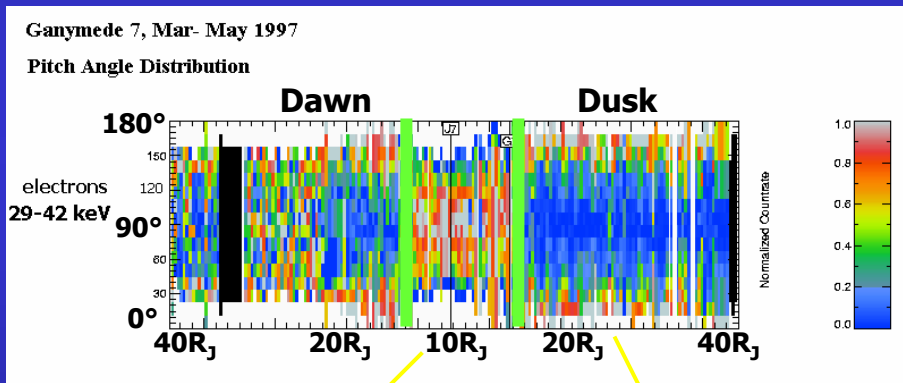


- Bunce and Cowley (2001b), Cowley and Bunce (2001), Hill (2001) and Southwood and Kivelson (2001) suggest the main auroral oval is due to the breakdown of corotation of the equatorial plasma
- Modulation of the oval in anti-correlation with solar wind dynamic pressure (C&B, 2001, 2003a&b; S&K, 2001)



Particle measurements at equator and correlation with secondary oval

➤ Most prominent and well defined boundary → **change in the electron pitch angle distributions located between 10 and 17 R_J**



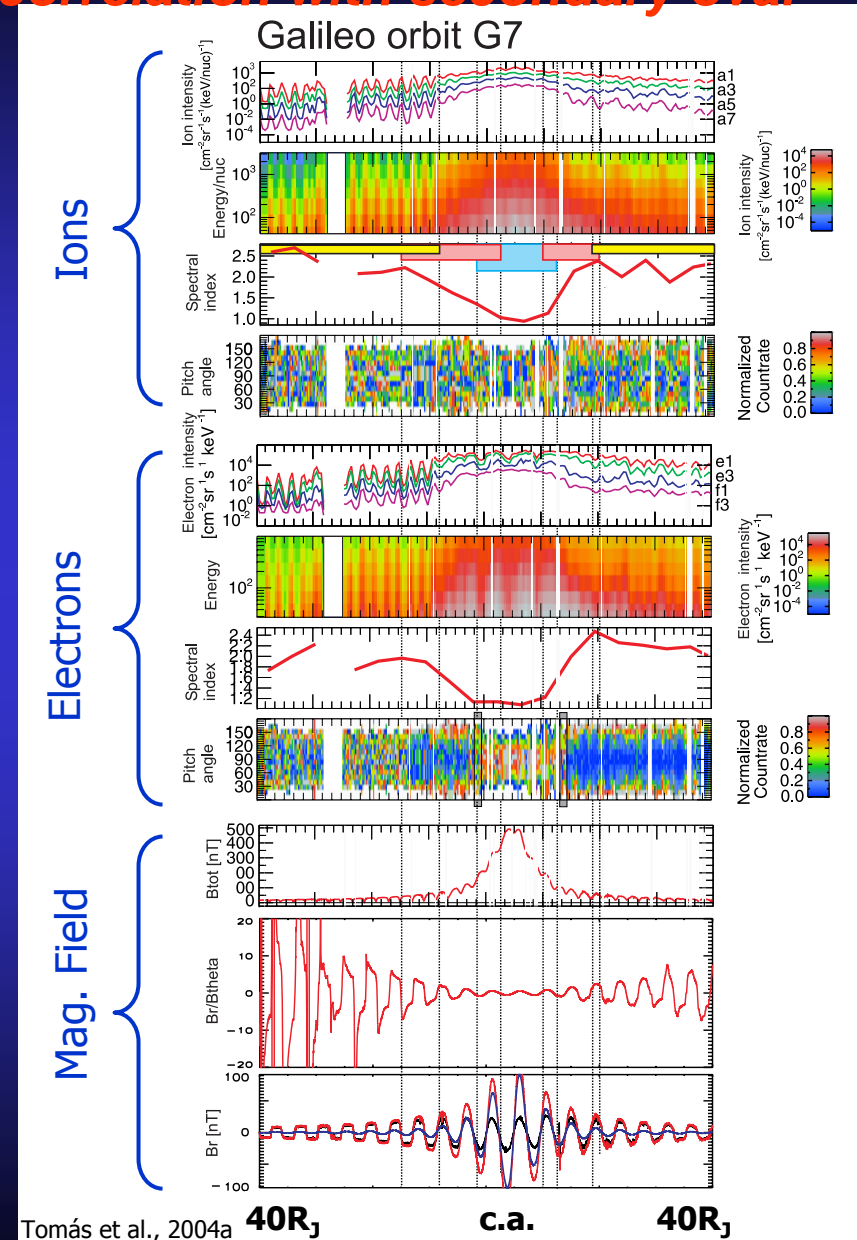
Inner Region

Outer Region

Pancake distribution with electrons maximum at 90°

Field aligned bi-directional electrons

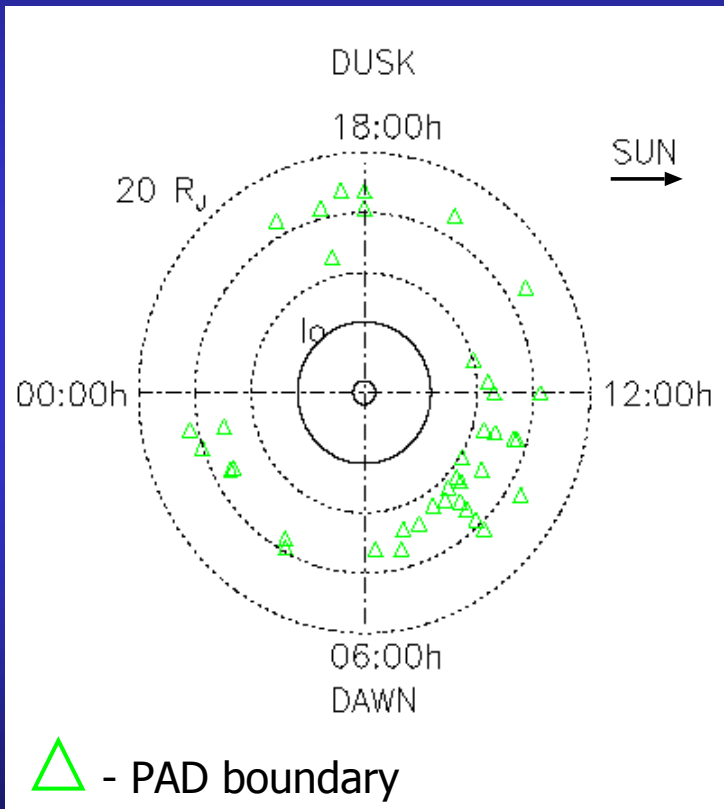
Tomas, 2004, 2005



Tomás et al., 2004a

Galileo observations

- Local time dependence of the PAD boundary in the equatorial plane

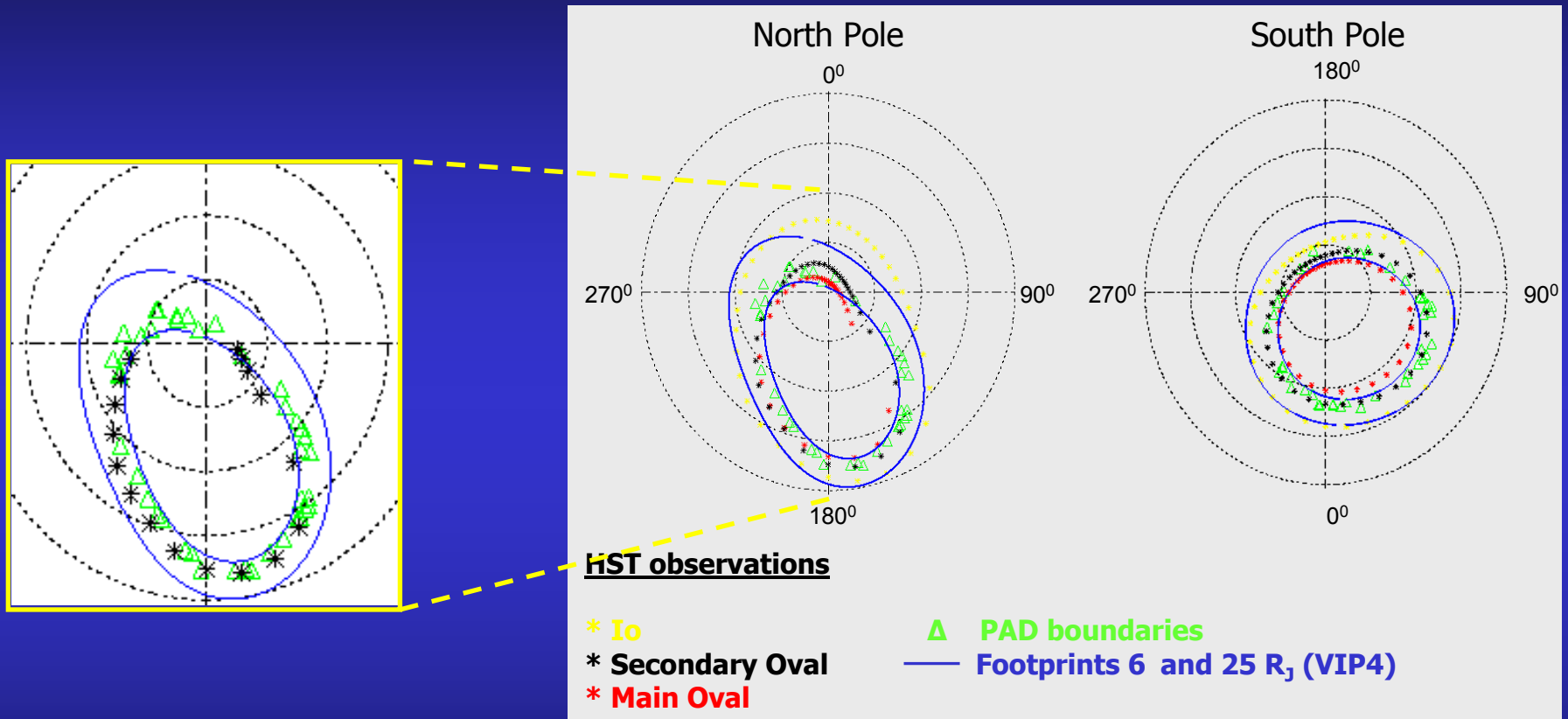


- Coverage of the Jovian magnetosphere in most of the local time sectors.

- No strong local time asymmetry between dawn and dusk.

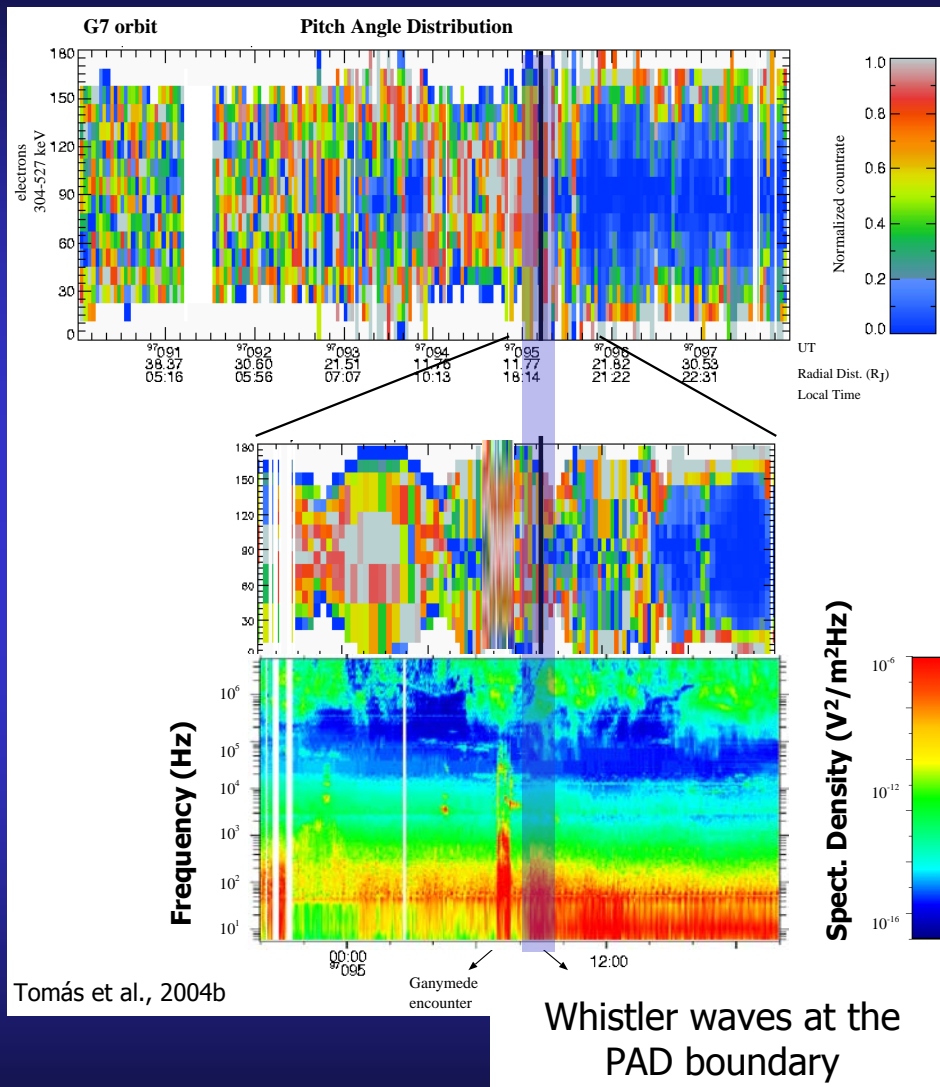
Tracing the magnetic field lines

- Comparing the footprints of the PAD boundary (VIP4 model) with the HST observations



- Good conjugation between the PAD boundary and the secondary oval

Wave-particle interaction



- Pitch angle diffusion coefficient

$$D_{\alpha\alpha} = \frac{2\pi f_c}{\gamma} \left(\frac{B'}{B} \right)^2 \cdot \epsilon$$

- Strong diffusion limit

$$D_{sd} = \left(\frac{v}{4R_J} \right) \frac{1}{L^4}$$

Considering:

$$L - [10, 17] R_J \quad B - [350, 50] \text{ nT}$$

$$f_c - [10^4, 10^3] \text{ Hz} \quad E' - [1.0, 0.1] \text{ mV/m}$$

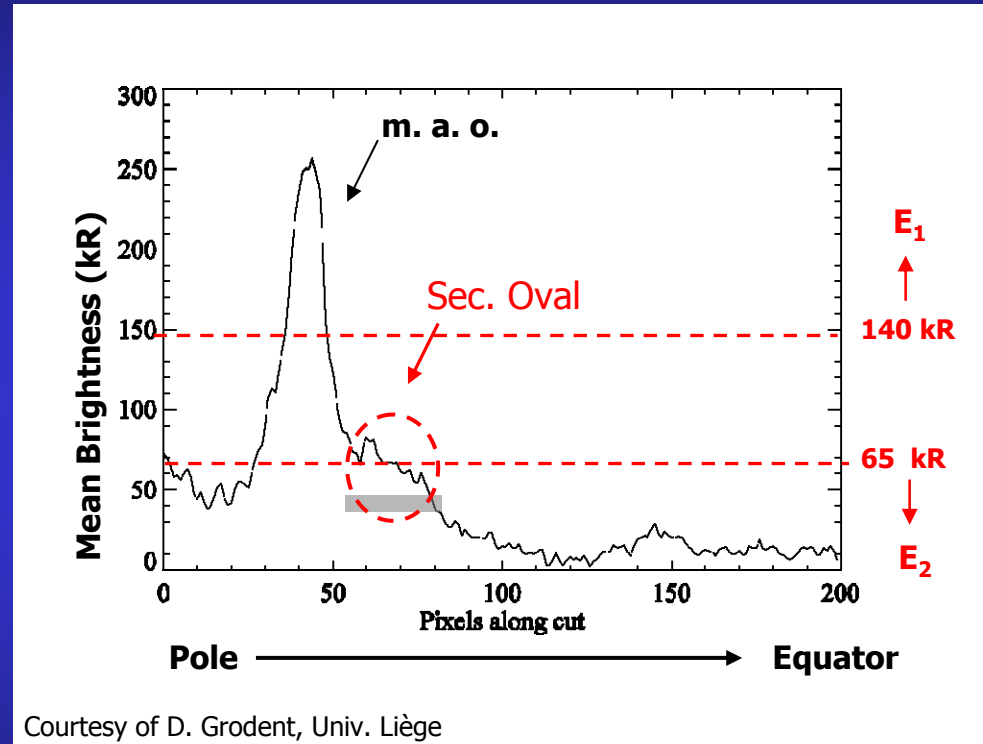
$D_{\alpha\alpha} \sim 2 D_{sd} \rightarrow$ The conditions for strong pitch angle diffusion are satisfied.

Precipitation energy flux

- Considering:
- The precipitation energy flux given by :

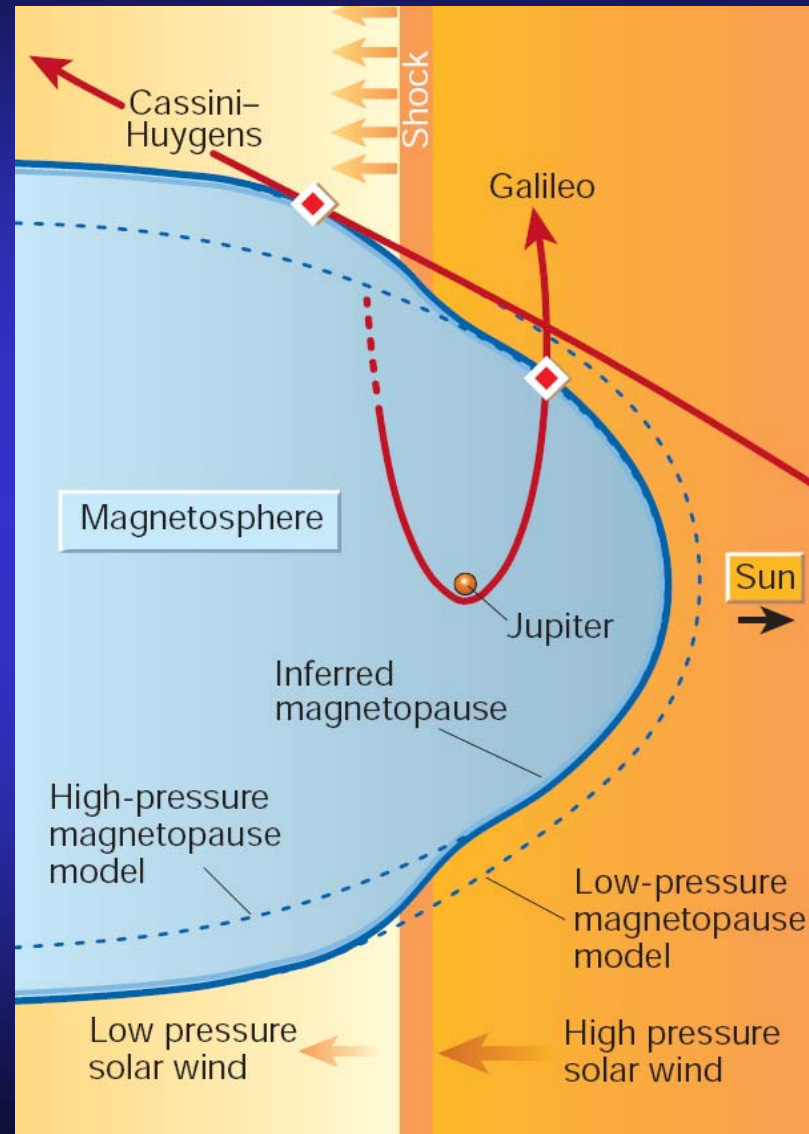
$$\varepsilon = \int_{E_{\min}}^{E_{\max}} \mathbf{E} \cdot \mathbf{j}(E, \gamma) \cdot dE$$

- Measured electron's spectra at the PAD boundary.
- Strong pitch-angle scattering.
- Electron's energy : $E_1 \in [55, 304]$ keV.
 $E_2 \in [55, 188]$ keV.



Sufficient to directly produce the observed auroral emissions of the secondary oval without the need of a field aligned potential drop.

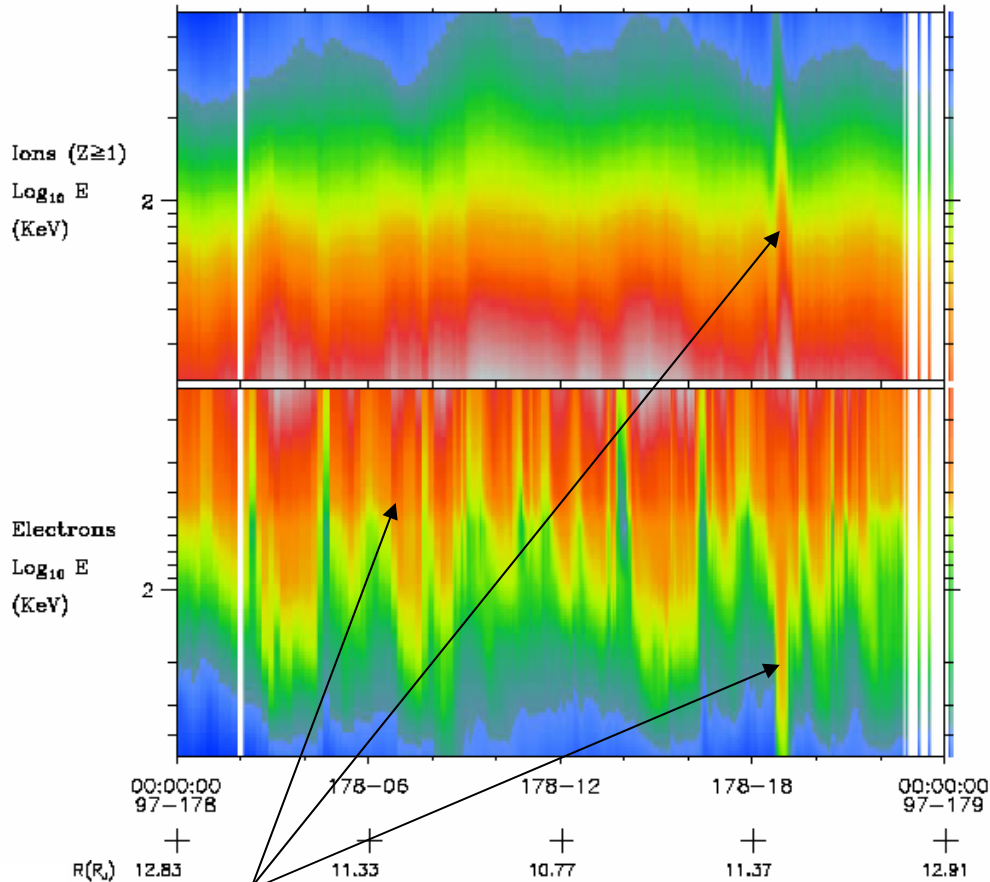
Cassini – Galileo Rendezvous at Jupiter



Dynamics in Jupiter's magnetosphere

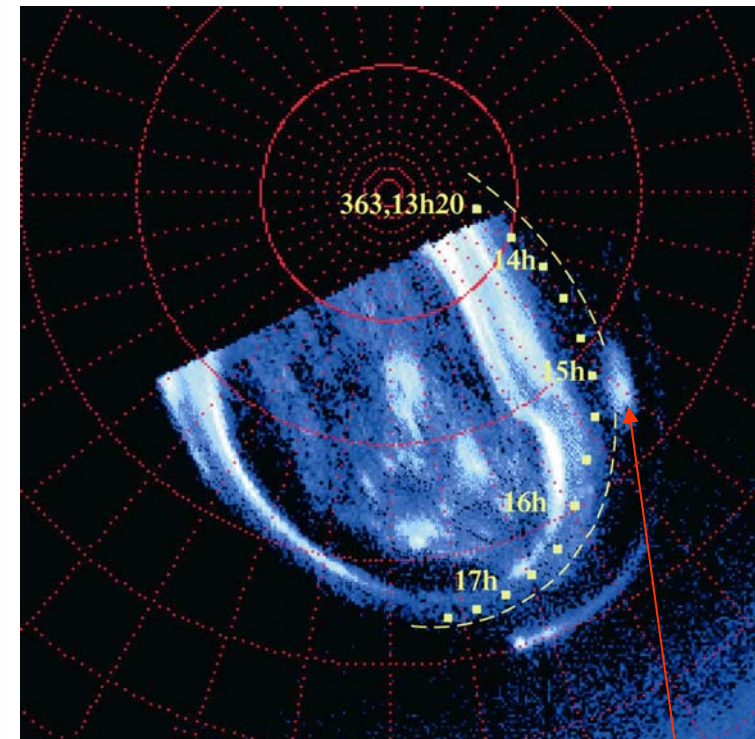
Energetic Particle Injections & correlation to auroral emissions

24 hour Galileo Energetic Particle Spectrogram



Extreme “storm-time” dynamics observed in the vicinity of Europa’s orbit

HST Image of Jupiter’s UV aurora

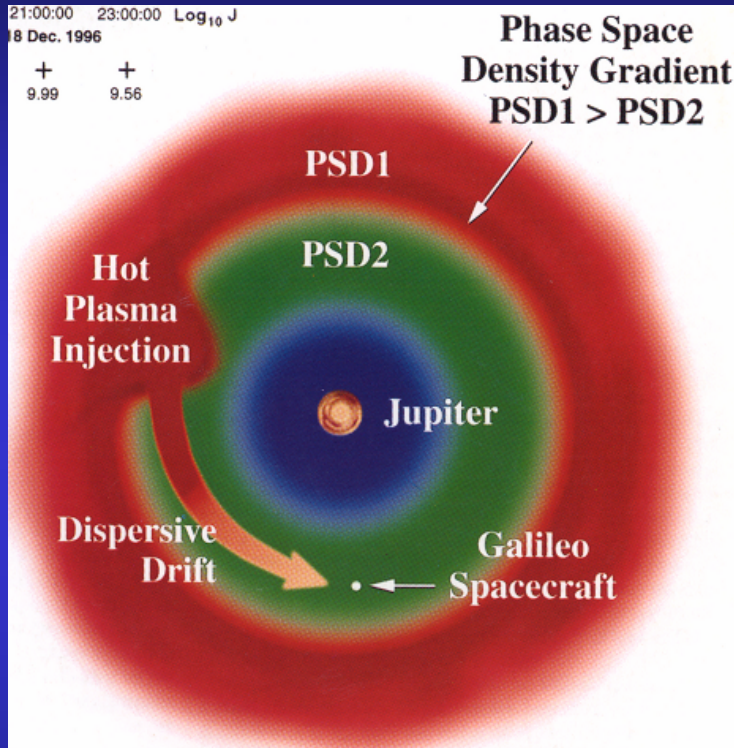


Mauk et al., 1997; 1999, 2000

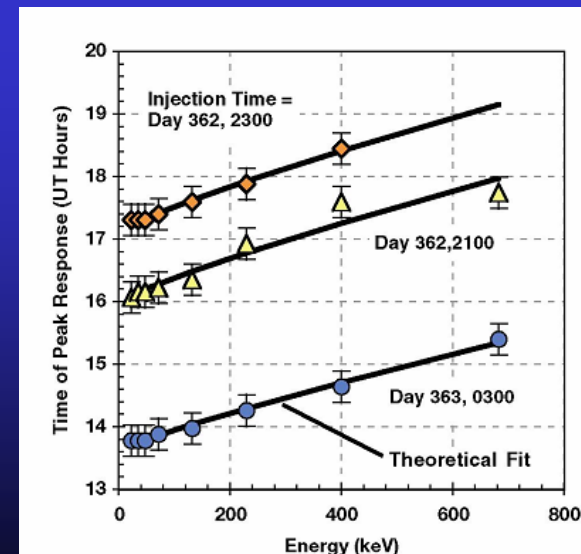
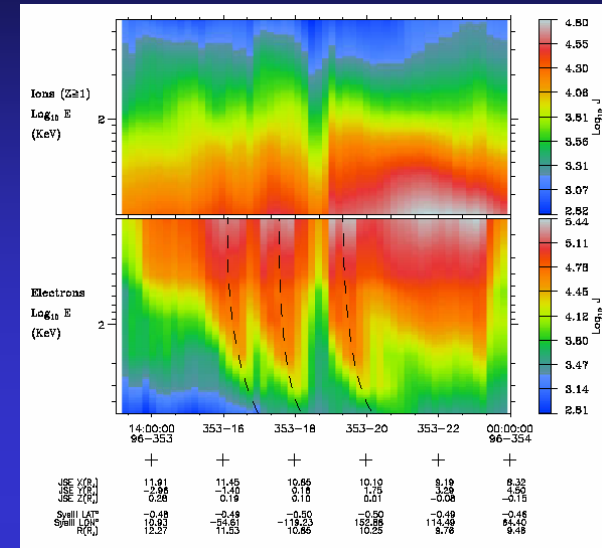
Auroral manifestation of near-Europa storm dynamics

Dynamics in Jupiter's magnetosphere

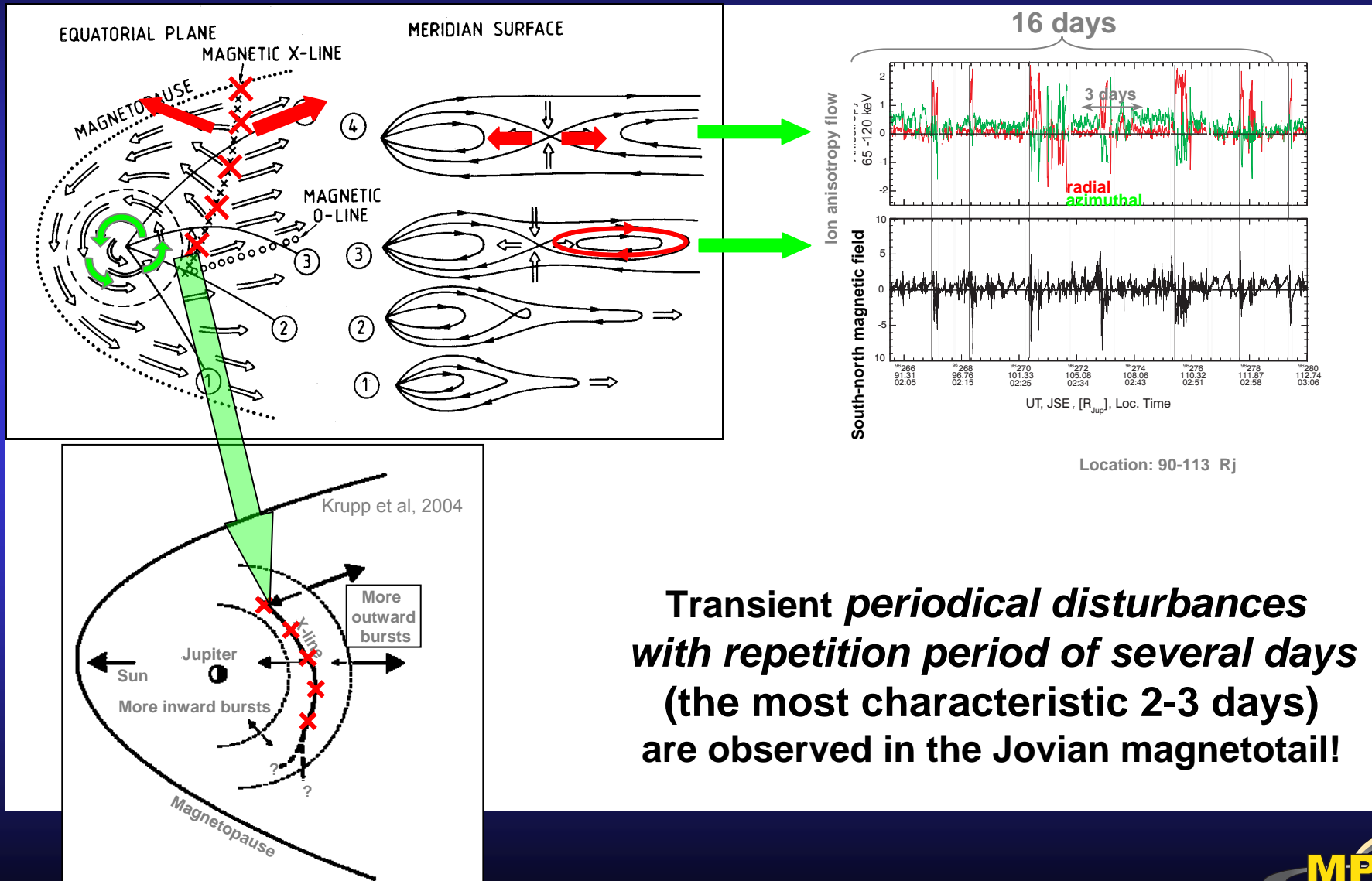
Particle injections



The behaviors of Jupiter magnetosphere injections were understood by invoking sudden radial injections over confined regions in azimuth followed by slow, dispersive, azimuthal drifts.

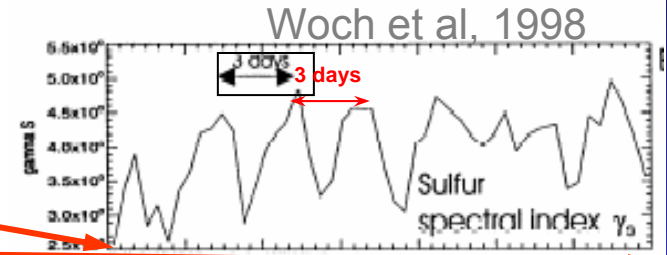
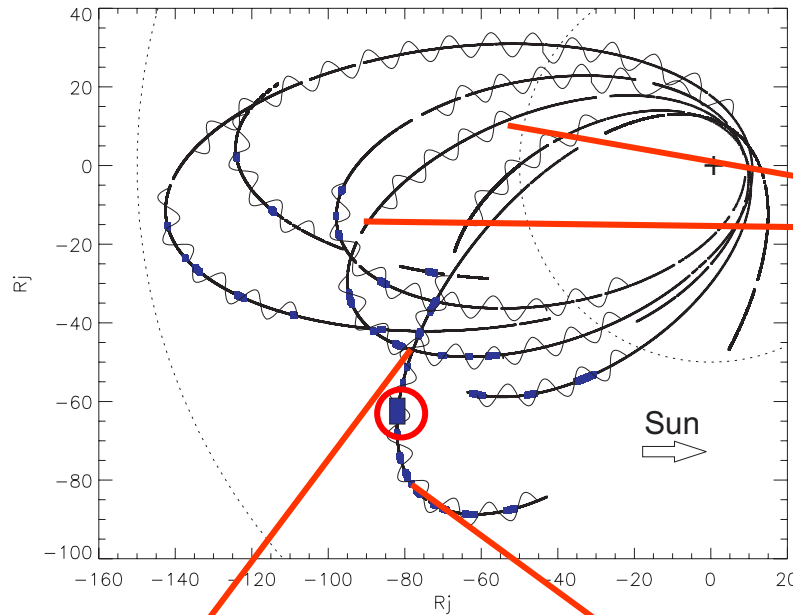


Dynamics of the Jovian magnetotail

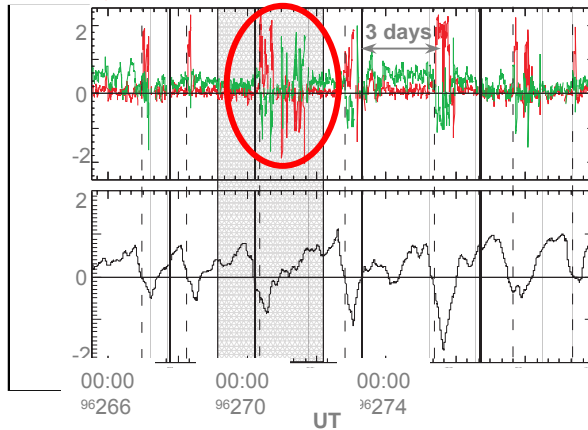


Transient *periodical disturbances* with repetition period of several days (the most characteristic 2-3 days) are observed in the Jovian magnetotail!

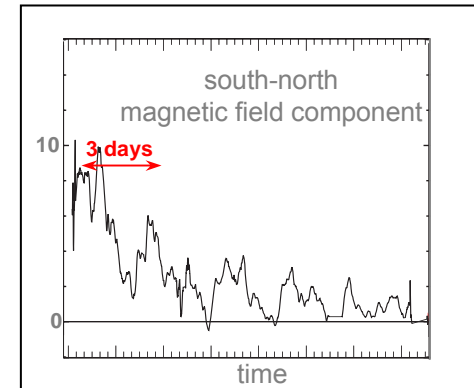
Global nature of several days periodicities



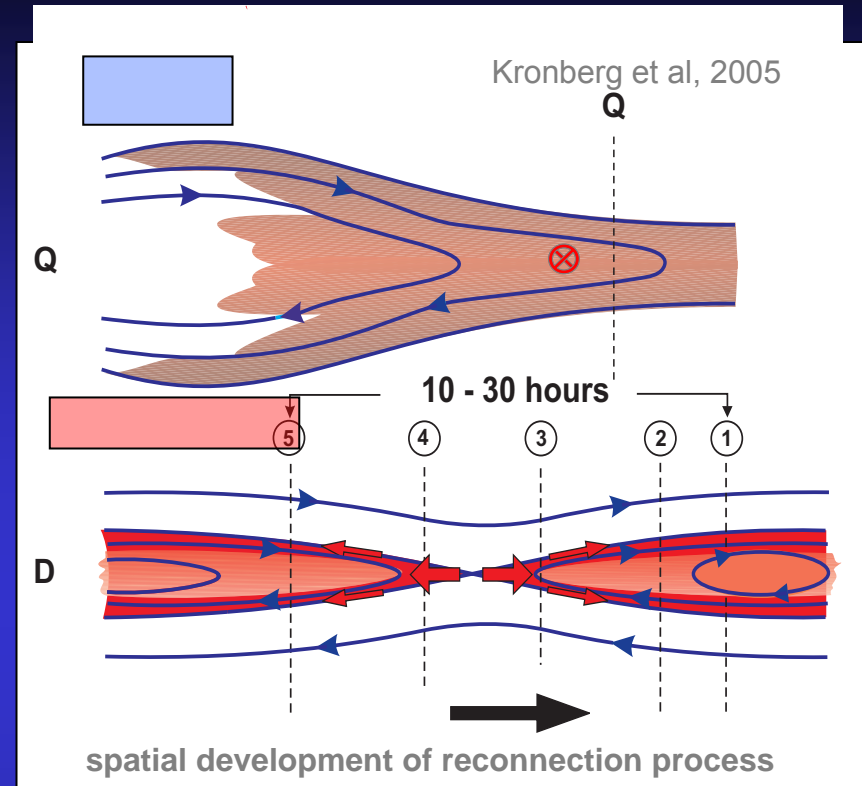
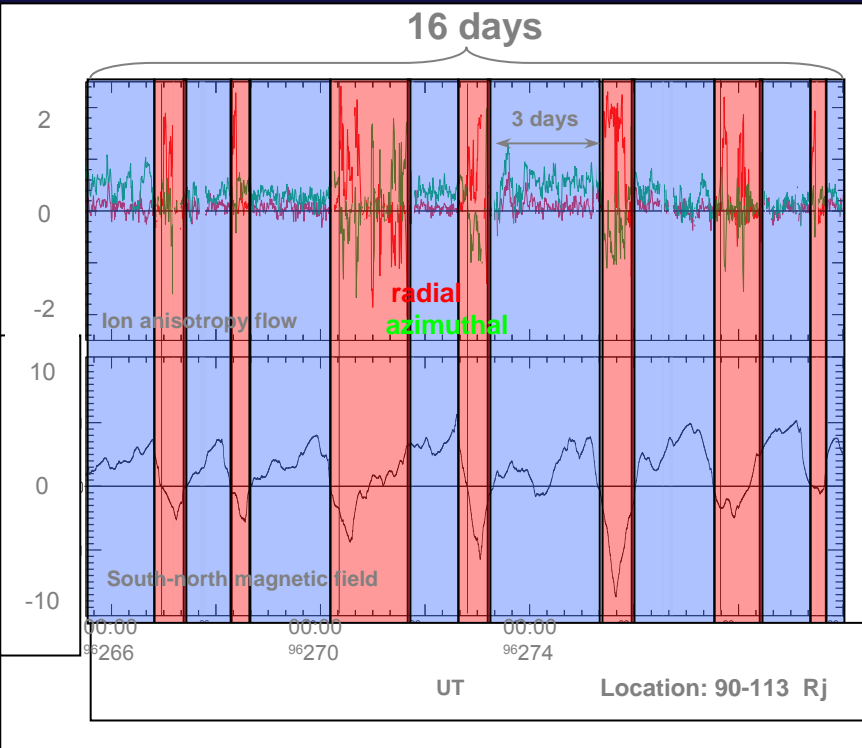
energy spectra
several days periodicities



Location: 90-113 Rj



Interpretation of observations



Quiet state

corotational plasma flow
+
stretching of the magnetotail

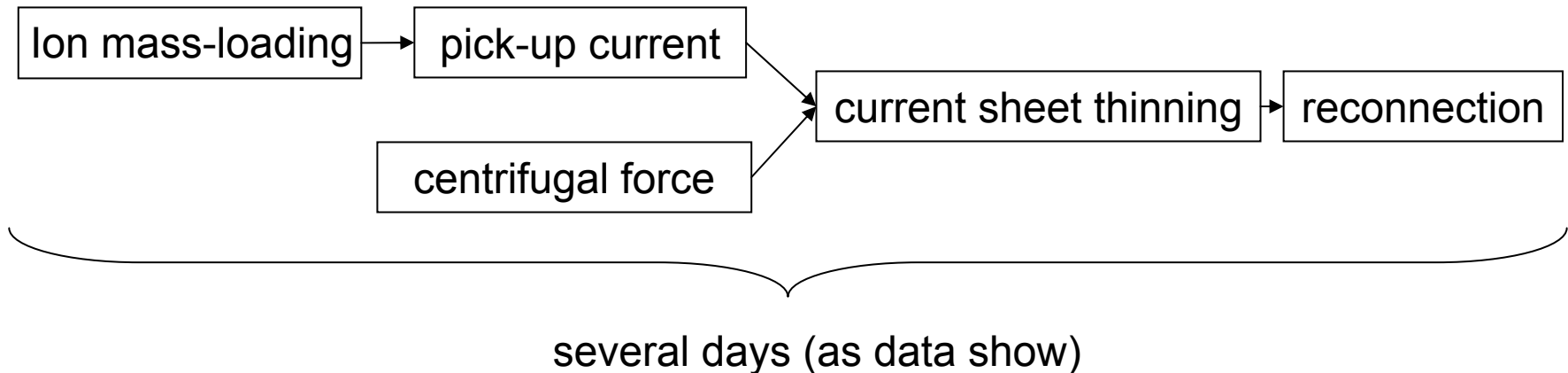
mass-loading

Disturbed state

radial inward and outward flow bursts
+
thin plasma sheet
+
reconnection

mass-release

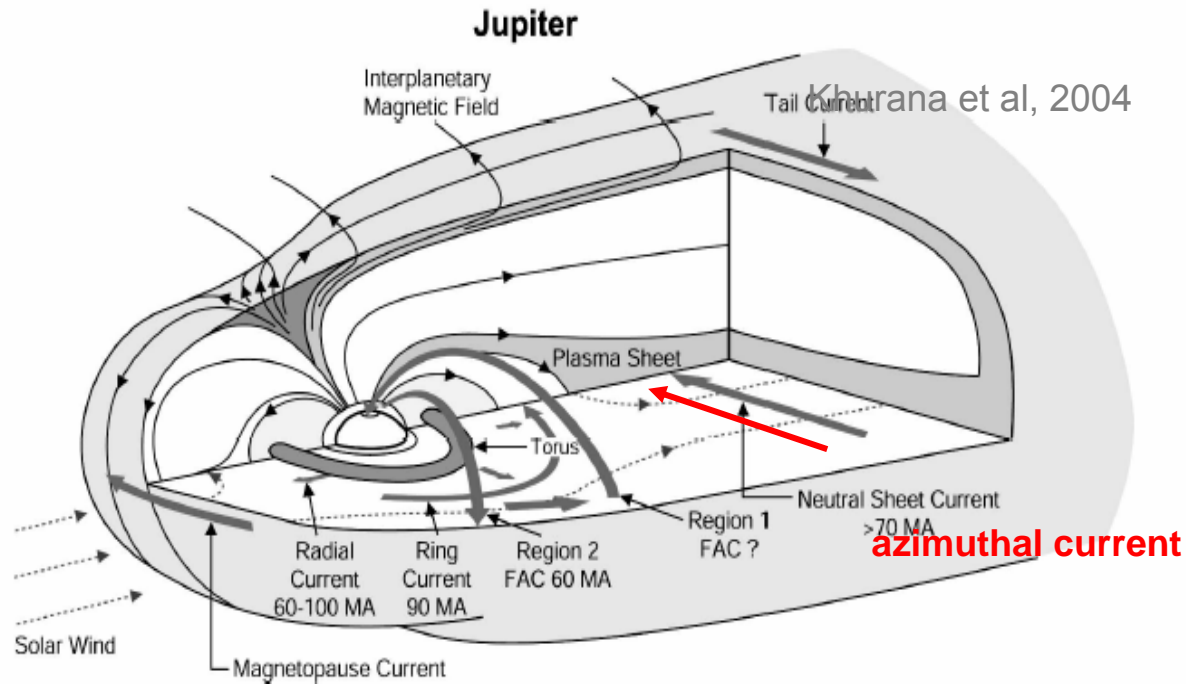
Internally driven magnetotail Theory



Local stress balance in the middle and outer magnetosphere is contained in the momentum equation for the plasma

$$\left[\underbrace{\rho \omega^2 r}_{\text{centrifugal force density}} + \underbrace{\nabla P}_{\text{pressure gradient}} = \underbrace{\vec{j} \times \vec{B}}_{\text{magnetic force density}} \right]$$

Current system in the Jovian magnetosphere



The currents at the equatorial plane of the magnetotail are

$$\left[\vec{j}_r + \vec{j}_\phi = -\dot{\rho} r B_\theta \omega \vec{e}_r - \frac{\rho \omega^2 r}{B_\theta} \vec{e}_\phi \right]$$

Time estimations

Ampere's law:

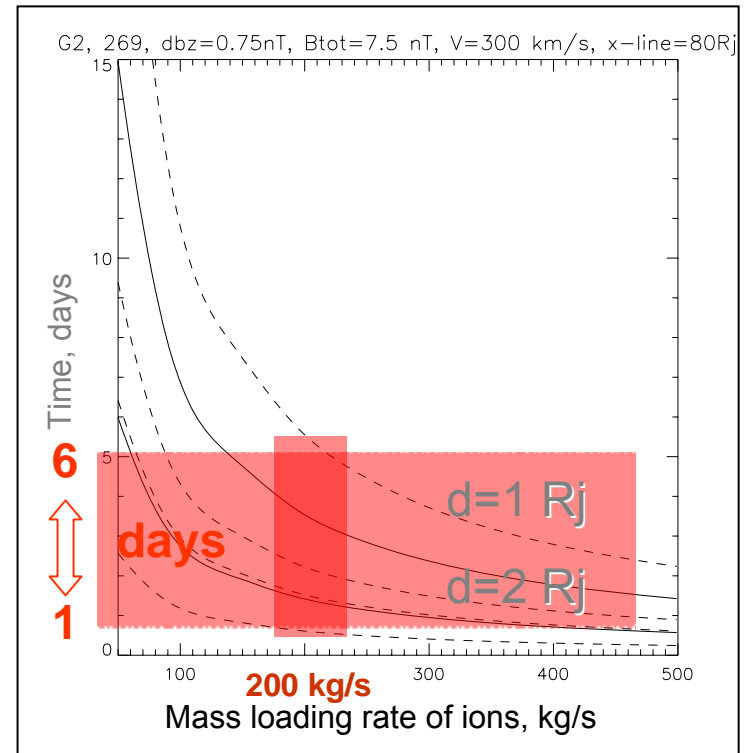
$$(\nabla \times \vec{B})_{\varphi} = \mu_0 j_{\varphi} \approx -\frac{B_r}{d}$$



$$\frac{\partial B_{\theta}}{\partial t} = \frac{\partial \rho}{\partial t} \frac{\mu_0 \omega^2 r d}{B_r}$$



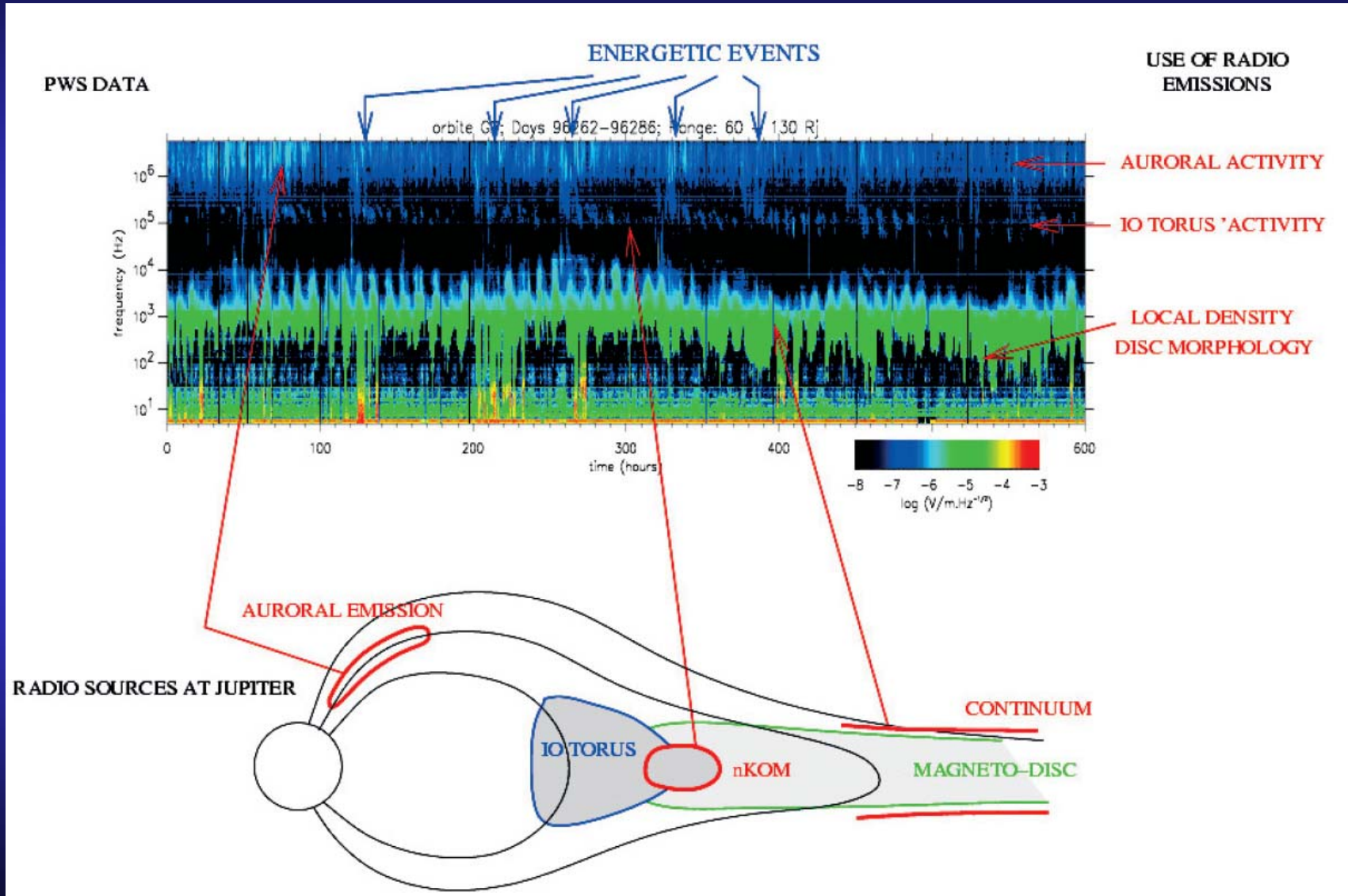
$$\Delta t = \frac{\Delta B_{\theta} B_r}{\dot{\rho} \mu_0 \omega^2 r d}$$



Input parameters:

$\Delta B_{\theta} \approx 0.1 B_r$	0.75 nT
$\omega = V / R$	$3 \cdot 10^5 (m/s) / R$
Distance to x-line	80 Rj
The most probable mass loading rate	200 kg/s

Radio emissions at Jupiter from various regions



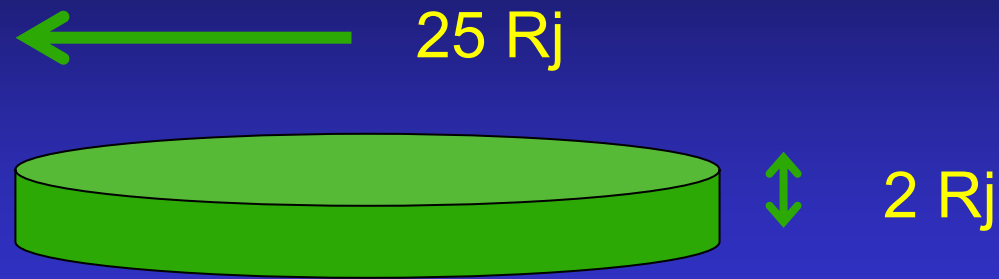
Jupiter

Aurora and tail disruptive events (Grodent et al., 2004)

	In Situ* Russell et al., Woch et al., Krupp et al.	Auroral Spots
Distance	70-120 R_j	>100 R_j
Local Time	postmidnight	premidnight
Size	~25 R_j	5-50 R_j
Duration	Mins-hours	5 min-1hour
Recurrence	4 hours-3days	1-2 days

Jupiter

Tail disruption events - numbers



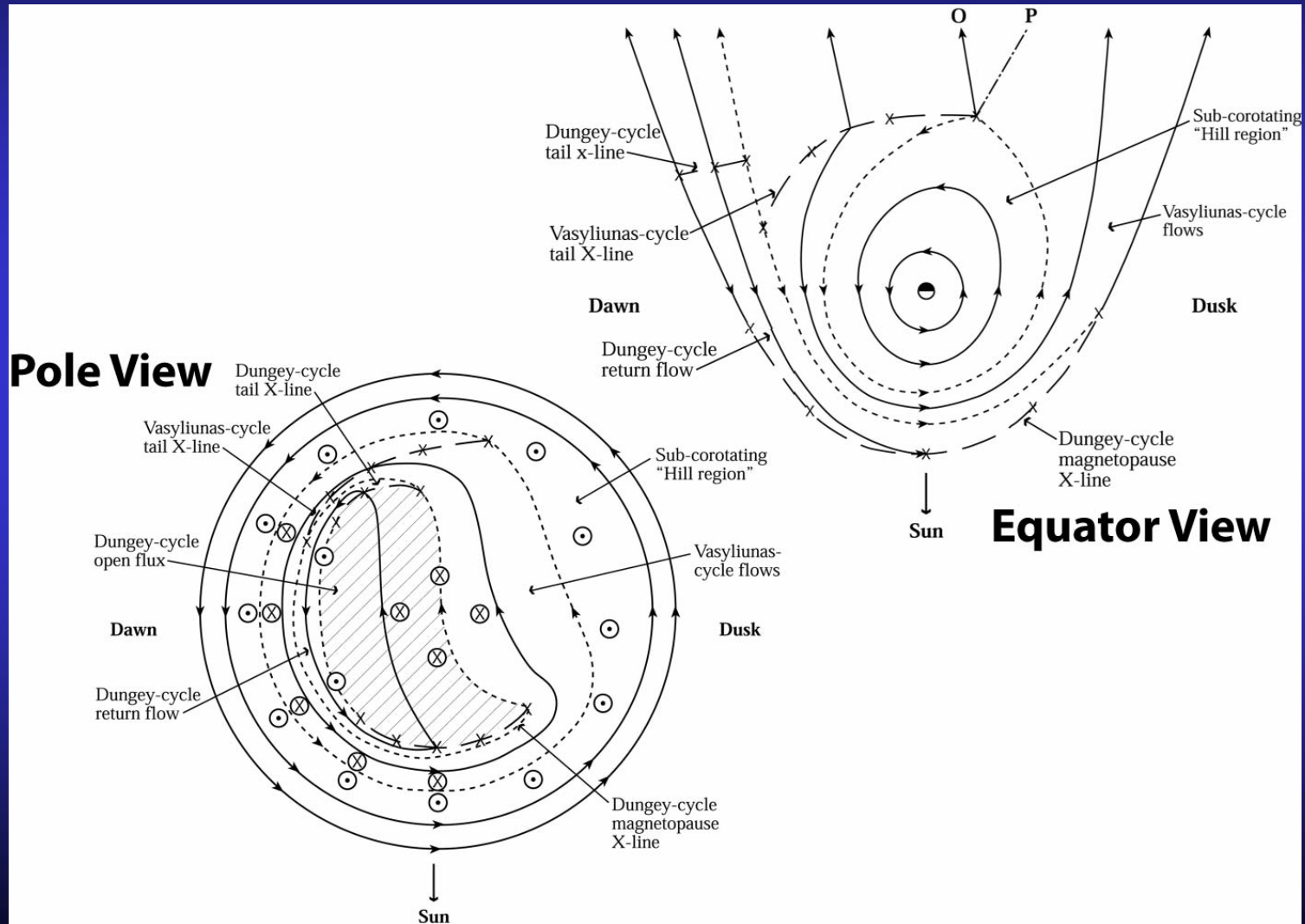
$$\sim 8000 R_j \times 0.01 \text{ ions/cc}$$

$$= 500 \text{ tons per plasmoid}$$

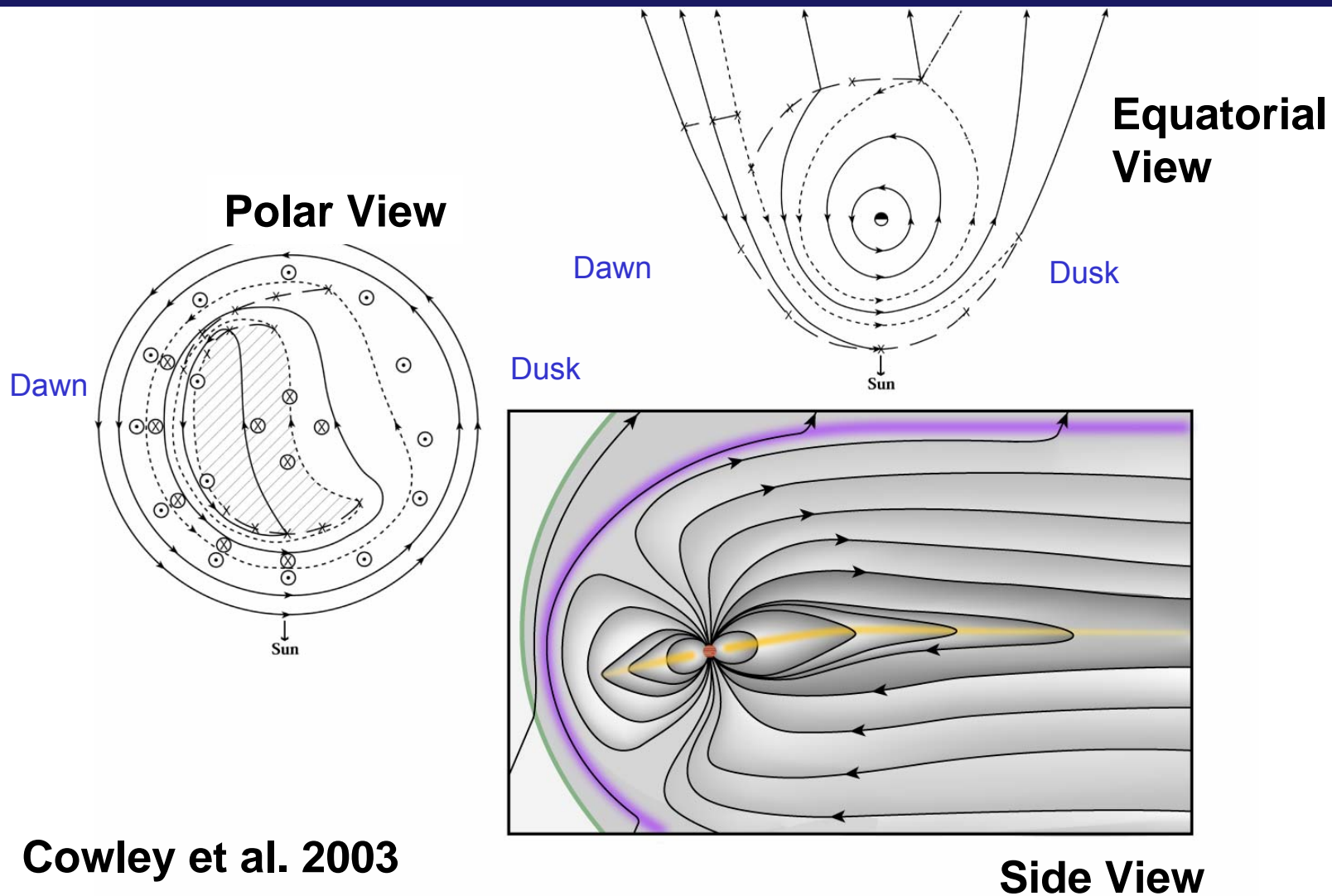
$$1 \text{ per day} = 0.006 \text{ ton/s}$$

$$1 \text{ per hour} = 0.15 \text{ ton/s}$$

Dynamics in the Jovian magnetosphere

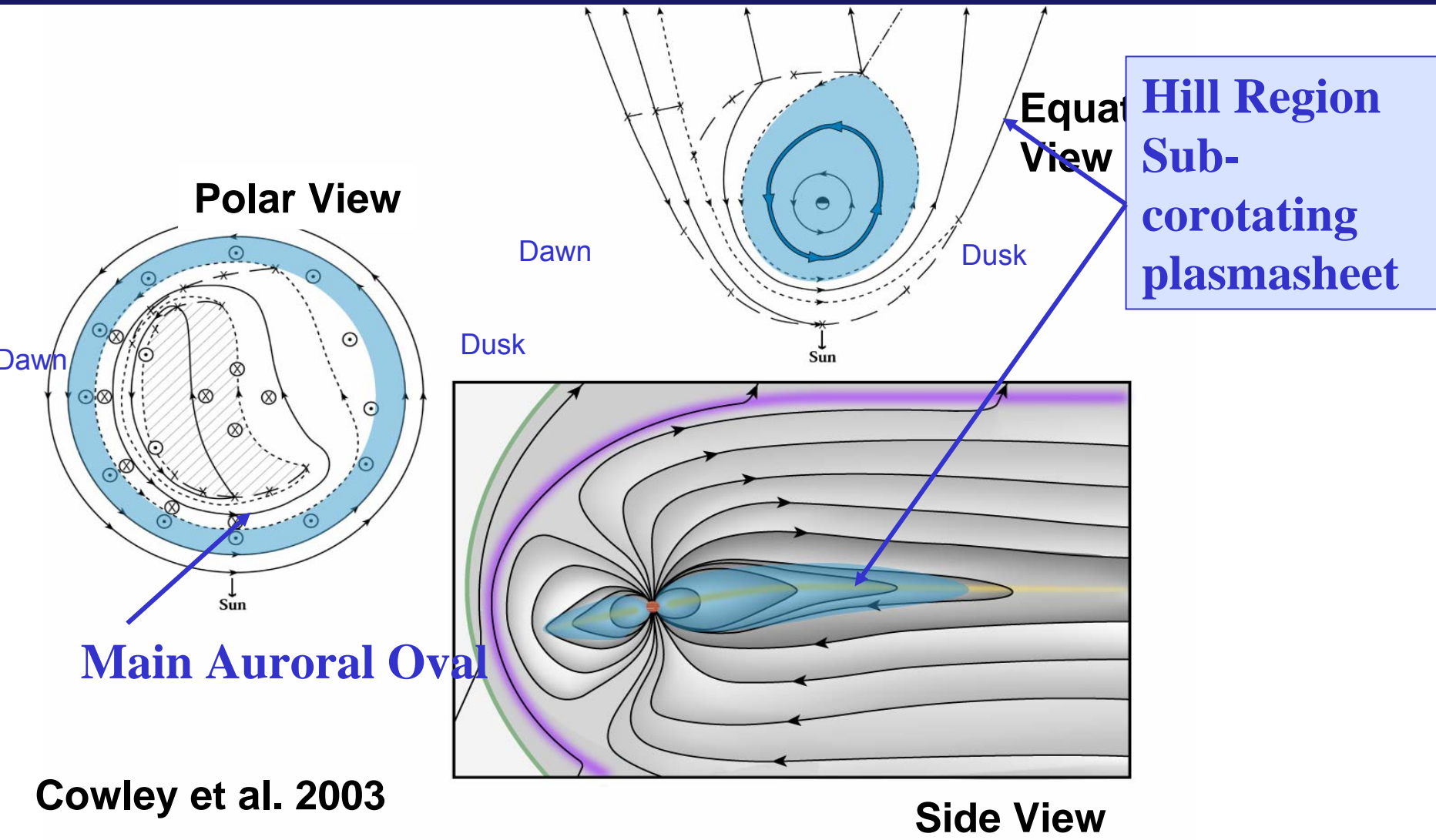


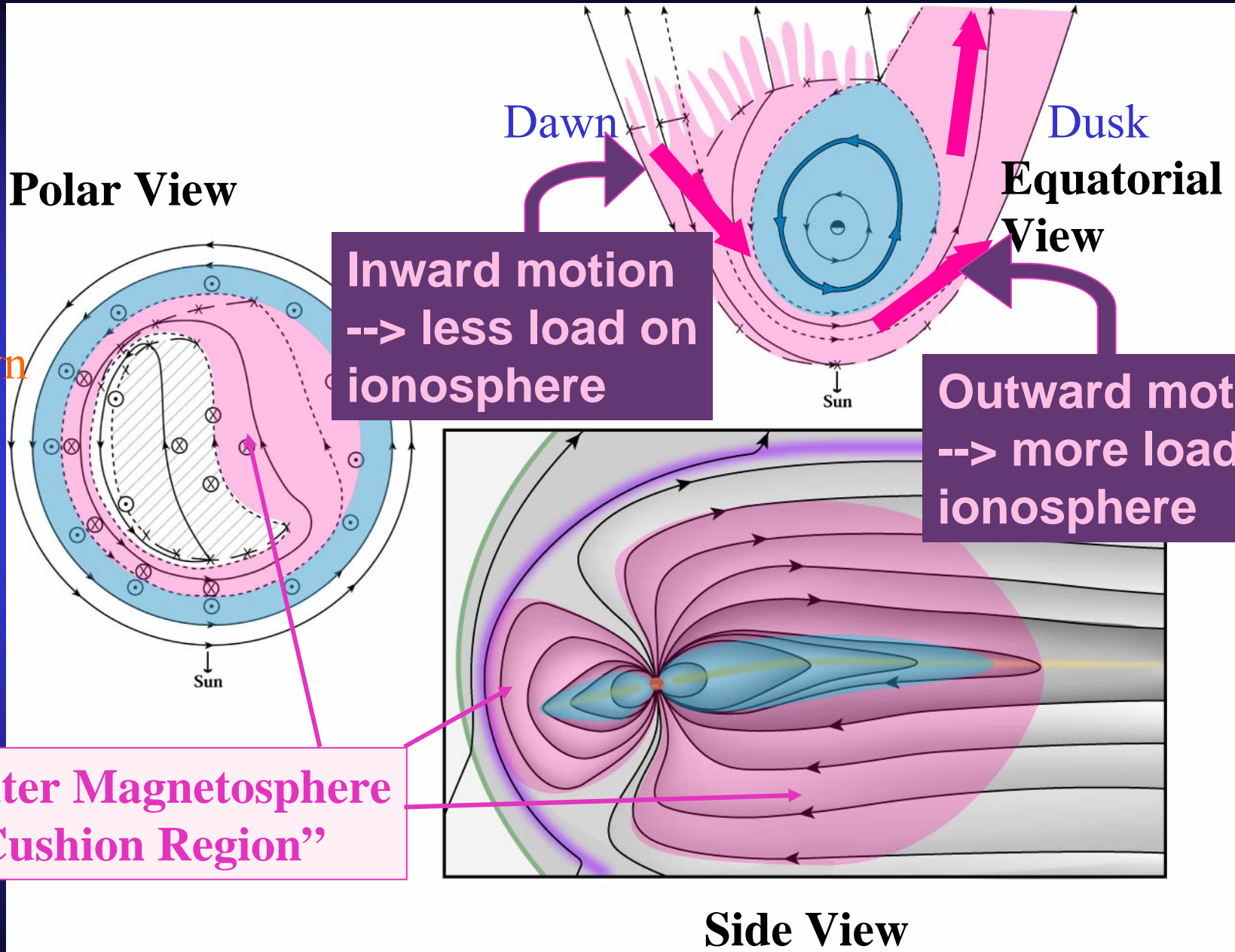
Configuration of the Jovian magnetosphere



Dynamics in the Jovian magnetosphere

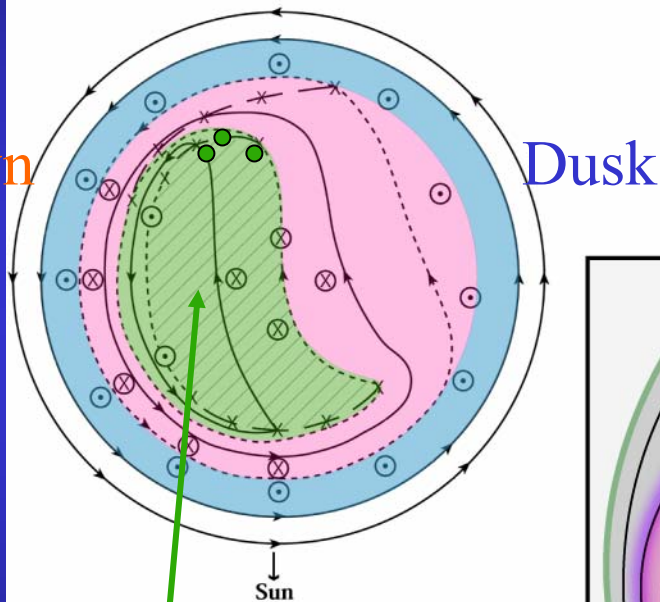
Jupiter aurora





???

Polar View



Dawn

Dusk

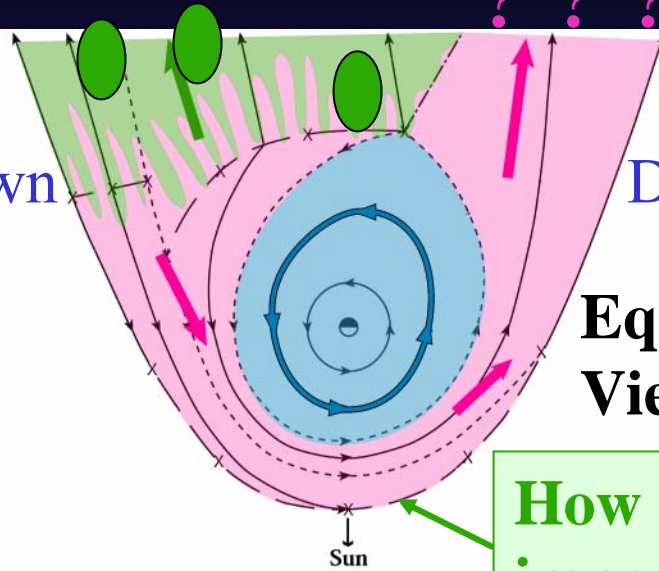
Sun

How Much of Polar Flux is Open?

Dawn

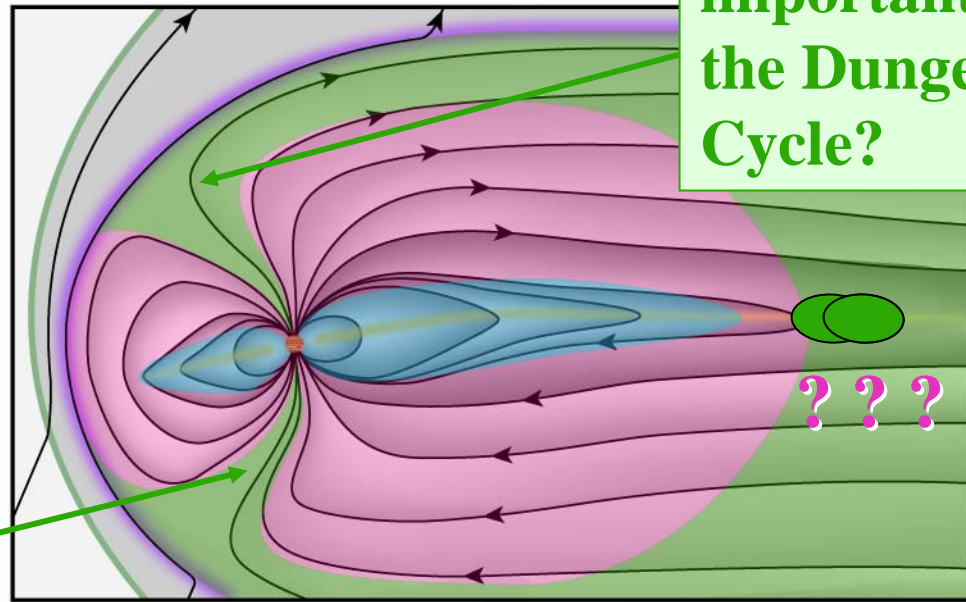
Dusk

Equatorial View



Sun

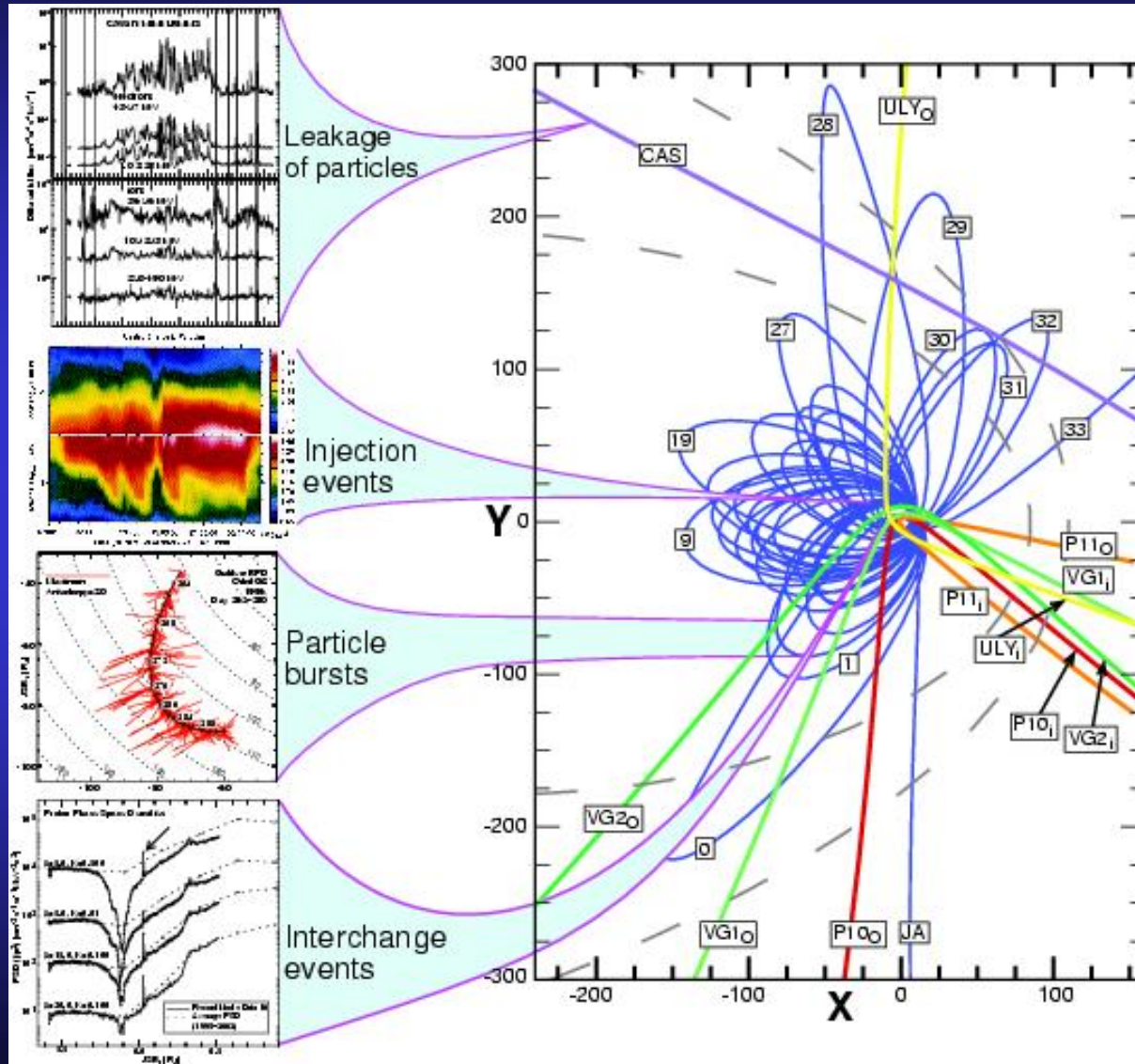
How important is the Dungey Cycle?



???

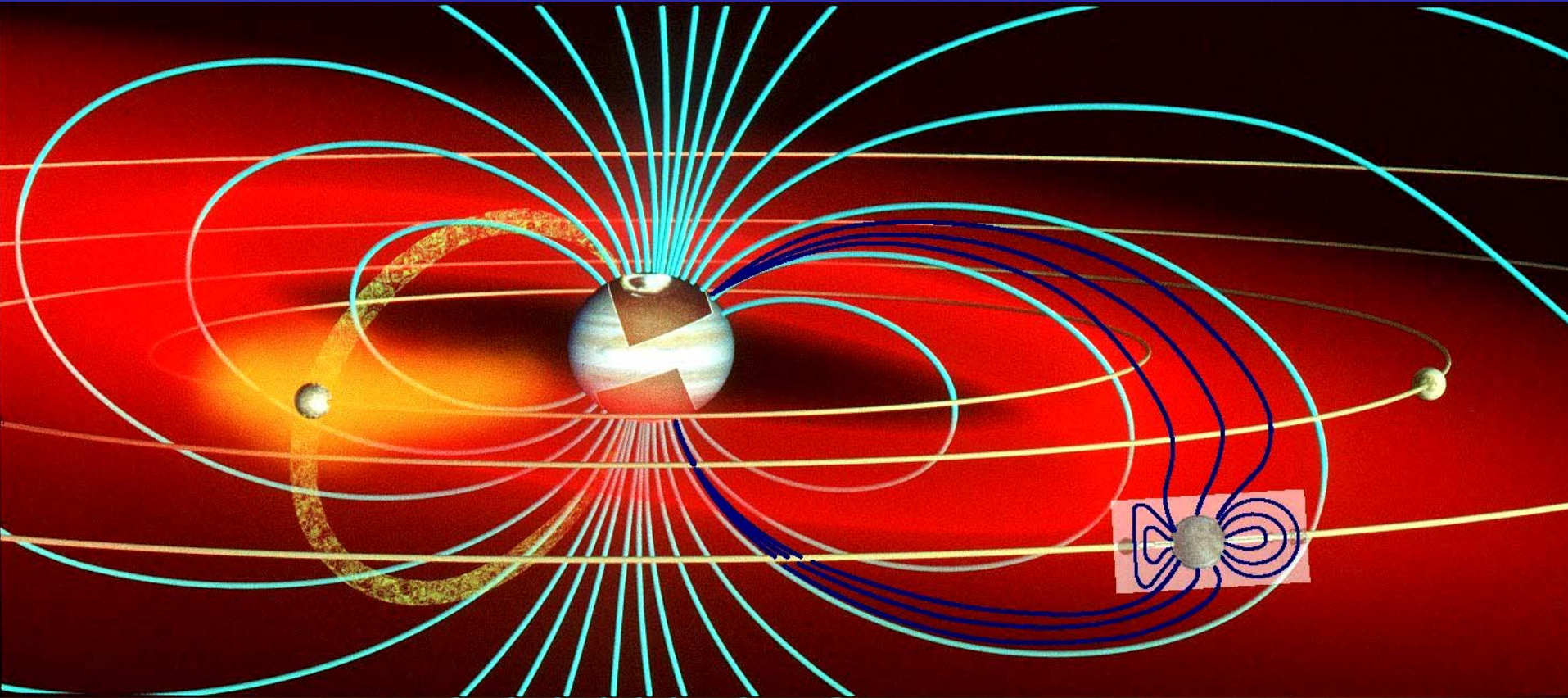
Side View

Dynamics in the Jovian magnetosphere



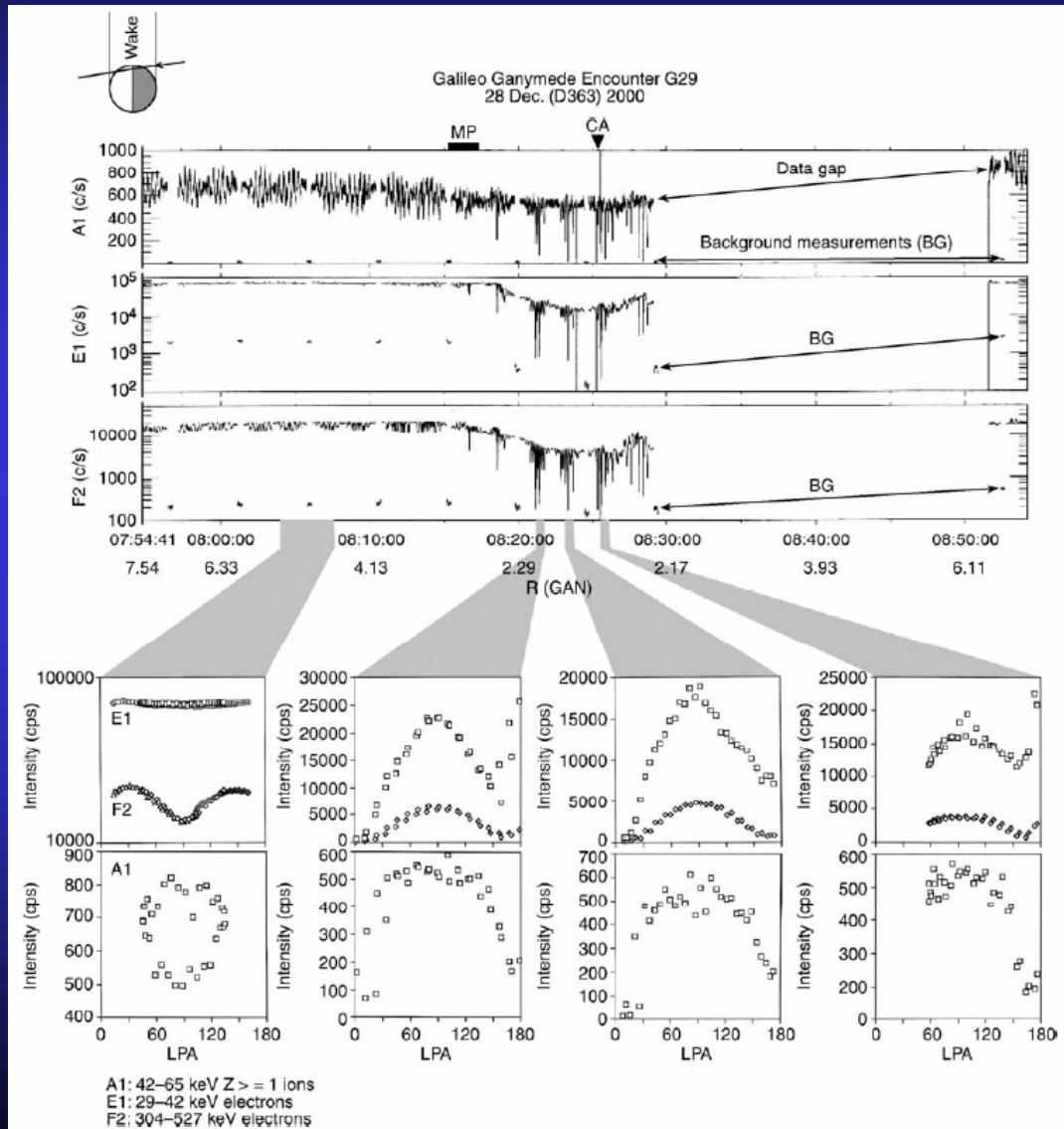
Ganymede magnetosphere

A magnetosphere within a magnetosphere



Ganymede:

Electron beams in Ganymede's magnetosphere



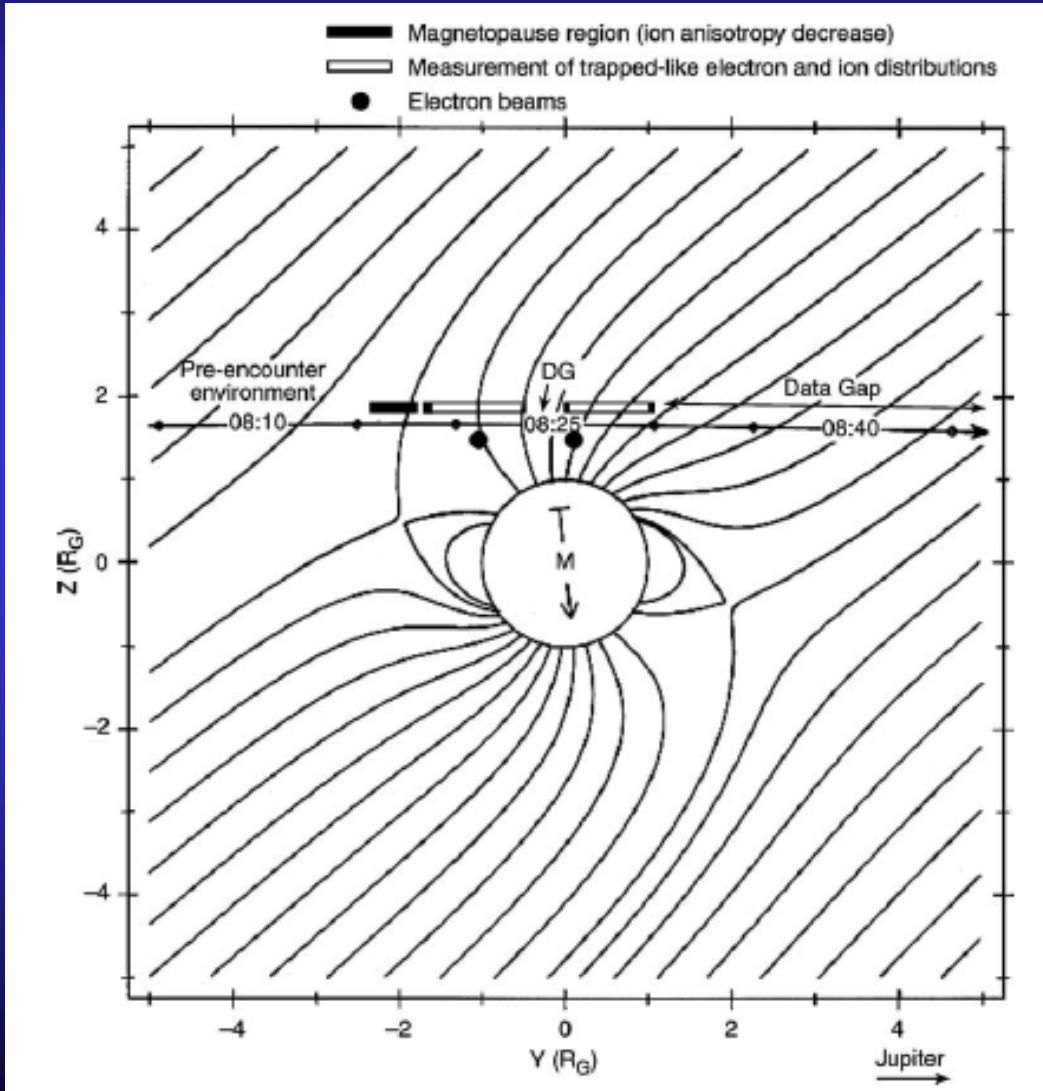
Williams, JGR, 2004

EPD results from Galileo's orbit 29

- Ganymede's magnetosphere more complex
- Electron beams may be formed by the entry and subsequent quasi-chaotic drift of ambient Jovian electrons

Ganymede:

Electron beams in Ganymede's magnetosphere



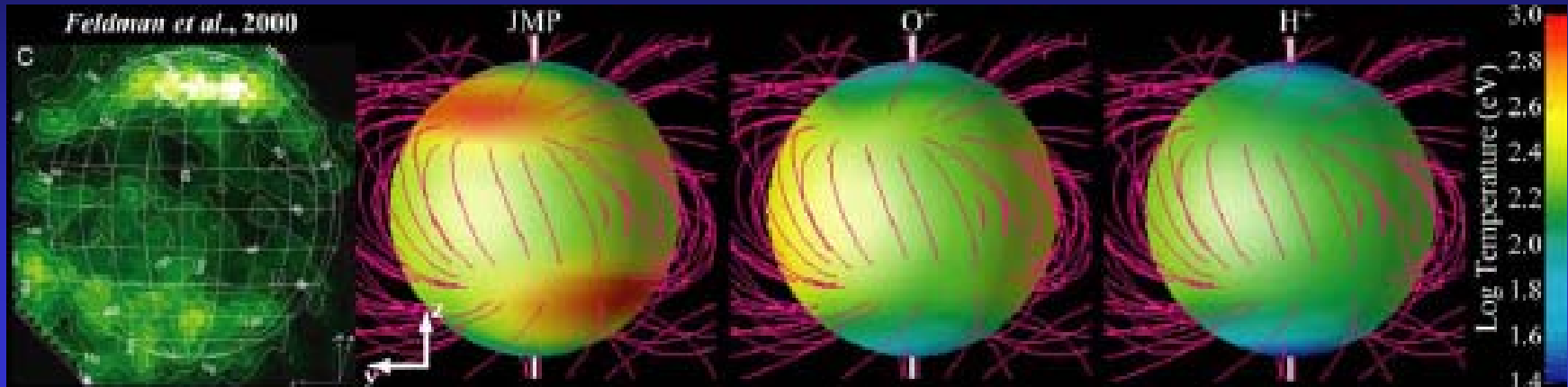
Williams, JGR, 2004

EPD results from Galileo's orbit 29

- **Ganymede's magnetosphere more complex**
- **Electron beams may be formed by the entry and subsequent quasi-chaotic drift of ambient Jovian electrons**

Ganymede:

Multi-Fluid simulations in Ganymede's magnetosphere



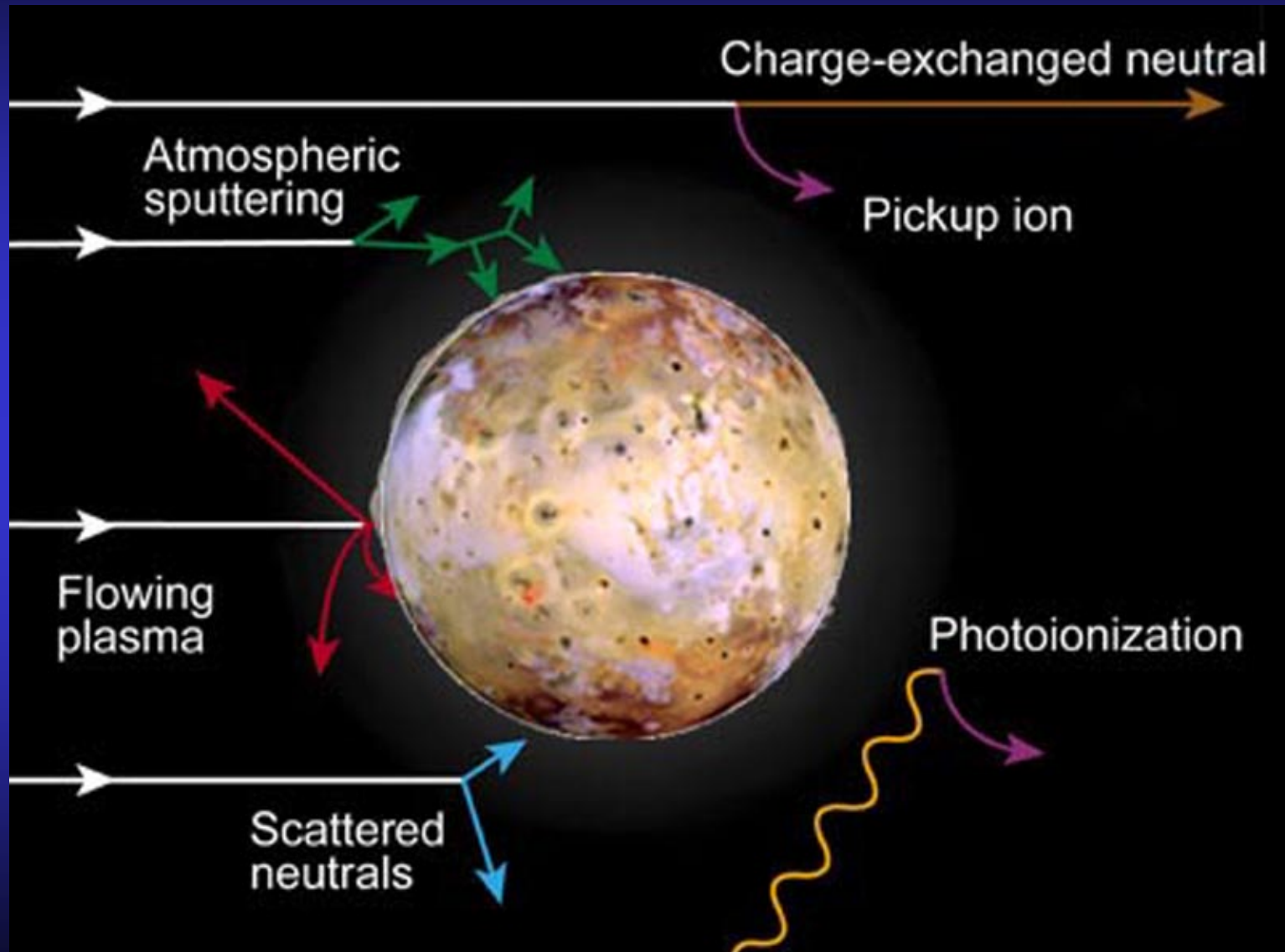
Paty and Winglee, GRL, 2004:

Simulation results compared to Galileo magnetometer measurements and Hubble observations of Ganymede's UV aurora

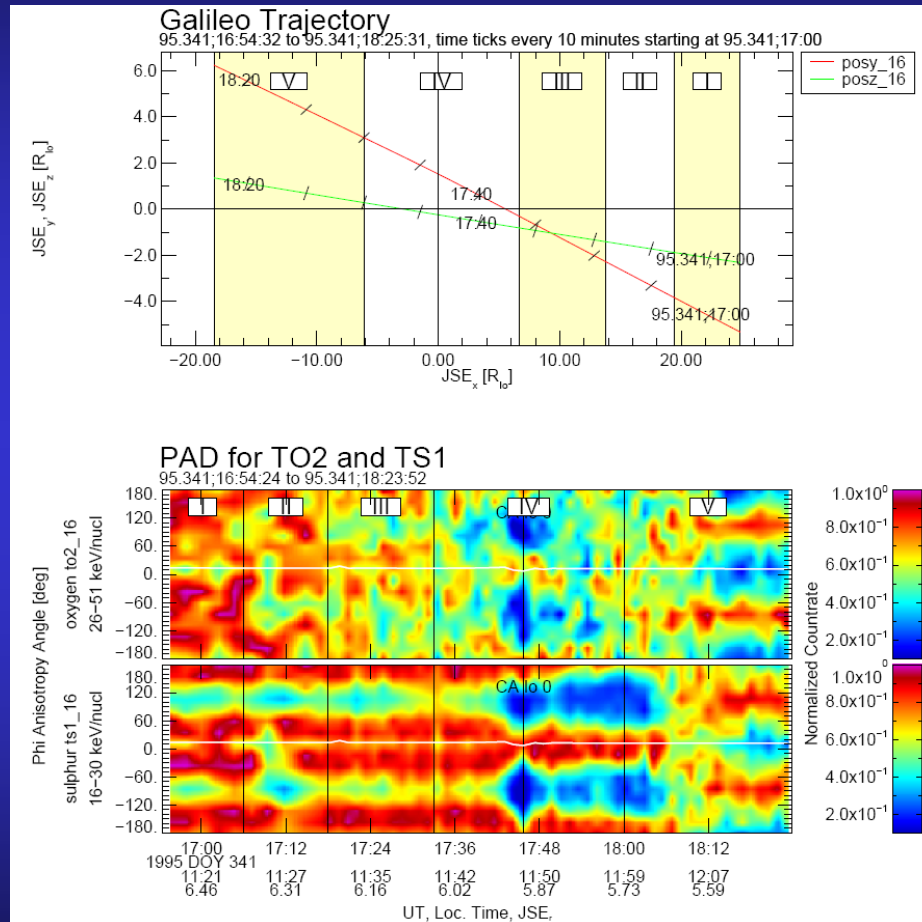
→ *good agreement of precipitation in the cusp*

→ *ionospheric outflow rates determined (10^{26} ions/s)*

plasma-moon interactions



Interaction between magnetospheric plasma and Io-Torus



Particle Observations:

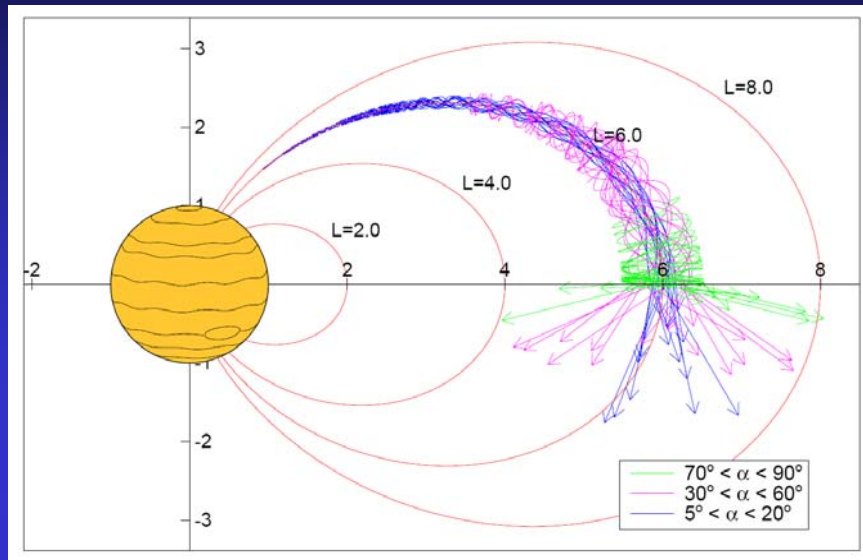
- *bounce loss cone* (0° and 180° PA) for protons, oxygen and sulphur
- additional loss cone at 90° PA for sulphur

Possible loss mechanisms:

- *bounce loss cone*: scattering processes near Jupiter
 - depletion at 0° (and 180°) pitch angle
- scattering processes in Io-torus region
 - depletion at 90° pitch angle

Lagg et al., 1998

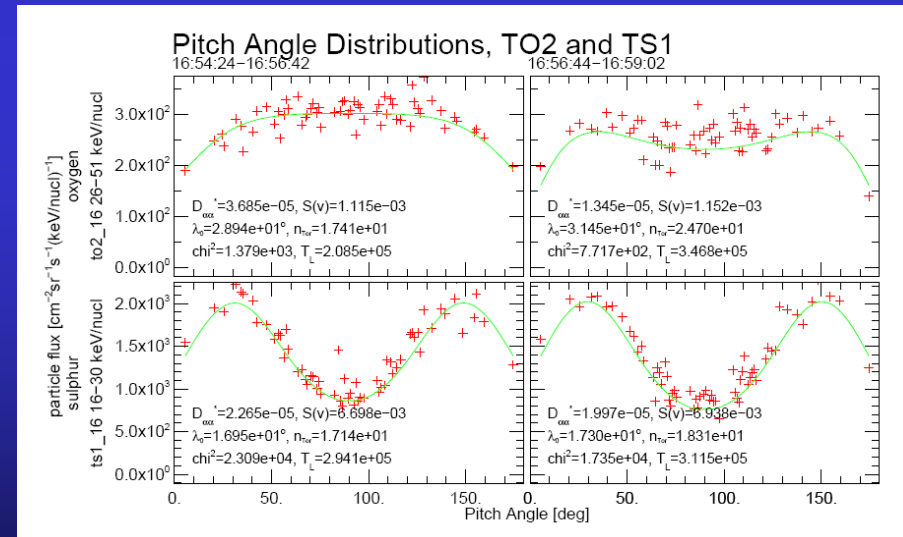
Interaction between magnetospheric plasma and Io-Torus



Possible loss mechanisms for 90 deg PA:

- bounce resonant waves
- satellite sweeping
- shell splitting
- particle-particle interactions in Io-torus

Lagg et al., 1998



particle-particle interaction in the Io-Torus

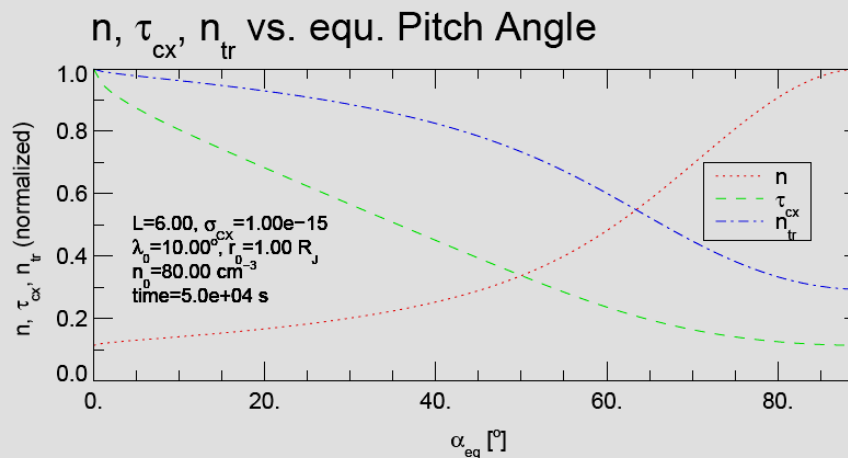
- Coulomb scattering → small cross section
- charge exchange ion-ion → not observable with EPD
- charge exchange ion-neutral:

estimating average neutral number density n and lifetime τ_{cx} [Ip, 1981]:

$$\bar{n}(\lambda_m) = \int_{\lambda=0}^{\lambda_m} \frac{n_{Torus}(\lambda)}{v_{\parallel}(\lambda)} ds \bigg/ \int_{\lambda=0}^{\lambda_m} \frac{1}{v_{\parallel}(\lambda)} ds, \quad \tau_{cx} = \frac{1}{\bar{n}\sigma_{cx}v}$$

assume Gaussian distribution for neutral torus density:

$$n_{Torus}(r, \lambda) = n_0 \exp\left(-\left(\frac{\lambda}{\lambda_0}\right)^2\right) \exp\left(-\left(\frac{r - R_{Torus}}{r_0}\right)^2\right) \approx n_0 \exp\left(-\left(\frac{\lambda}{\lambda_0}\right)^2\right)$$



Lagg et al., 1998

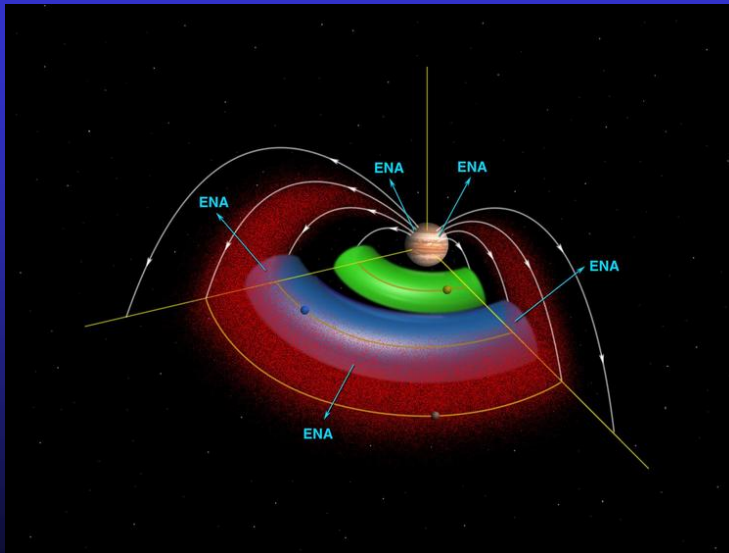
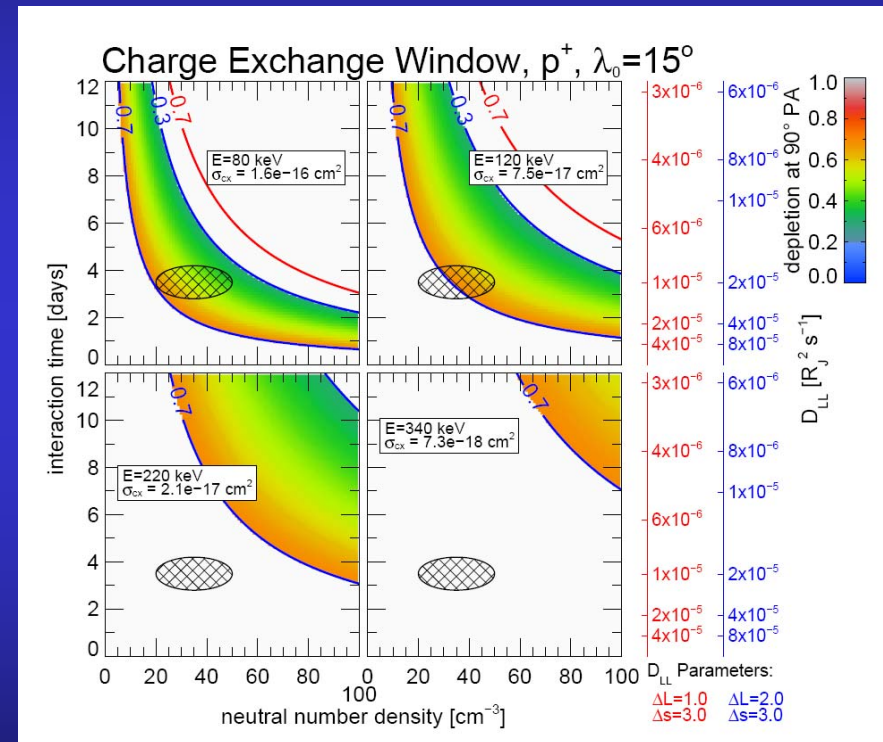
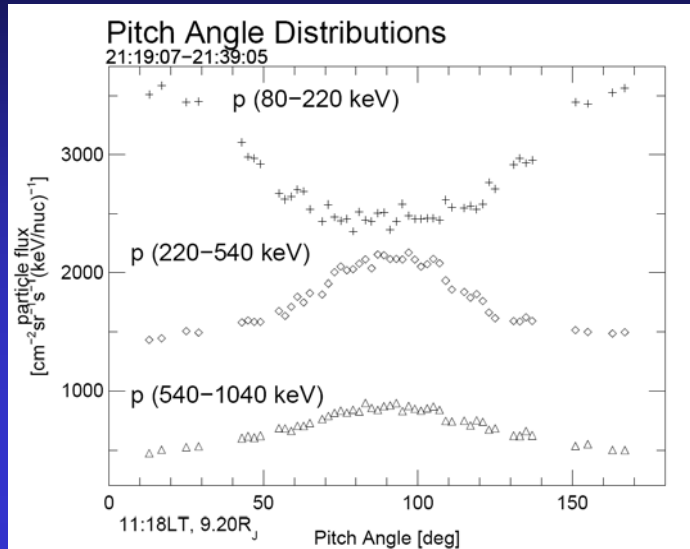
neutral density in the Io-Torus from energetic particle measurements

channel	energy [keV/nucl]	reaction	σ_{cx} [cm ²]	$D_{\alpha\alpha}$ [cm ² s ⁻¹]	T_L [s]	λ_0 [°]	n_0 [cm ⁻³]
sulphur							
TS1	16 - 30	$S^+ + X$	$2.36 \cdot 10^{-15}$	$2.1 \cdot 10^{-5}$	$3.0 \cdot 10^5$	17	18
TS2	30 - 62		$2.02 \cdot 10^{-15}$	$4.4 \cdot 10^{-5}$	$1.9 \cdot 10^5$	23	25
TS3	62 - 310		$9.00 \cdot 10^{-16}$	$4.9 \cdot 10^{-5}$	$1.4 \cdot 10^5$	23	34
oxygen							
TO1	12 - 26	$O^+ + X$	$1.51 \cdot 10^{-15}$	$6.9 \cdot 10^{-5}$	$2.3 \cdot 10^5$	31	11
TO2	26 - 51		$1.09 \cdot 10^{-15}$	$2.8 \cdot 10^{-5}$	$2.3 \cdot 10^5$	30	23

modell/observation of	density OI [cm ⁻³]	density SI [cm ⁻³]
<i>Brown</i> [1981]	30	
<i>Smith and Strobel</i> [1985]	30	6
<i>Skinner and Durrance</i> [1986]	$>29 \pm 16$	$>6 \pm 3$
this work		≈ 25

Lagg et al., 1998

Europa torus from charged and neutral particle measurements



Lagg et al., 2001