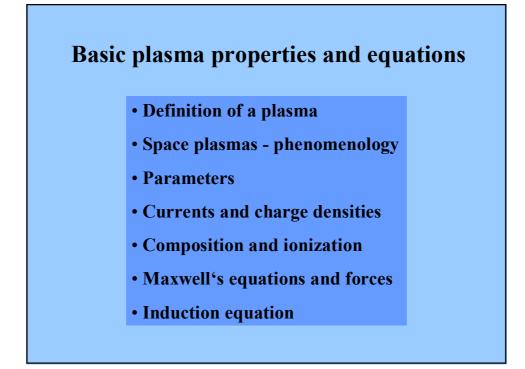
Space plasma physics

- Basic plasma properties and equations
- Space plasmas, examples and phenomenology
- Single particle motion and trapped particles
- Collisions and transport phenomena
- Elements of kinetic theory
- Fluid equations and magnetohydrodynamics
- Magnetohydrodynamic waves

Space plasma physics

- Boundaries, shocks and discontinuities
- Plasma waves in the fluid picture I
- Plasma waves in the fluid picture II
- Fundamentals of wave kinetic theory
- Concepts of plasma micro- and macroinstability
- Kinetic plasma microinstabilities
- Wave-particle interactions



Definition of a plasma

A plasma is a mixed gas or fluid of neutral and charged particles. Partially or fully ionized space plasmas have usually the same total number of positive (ions) and negative (electrons) charges and therefore behave quasineutral.

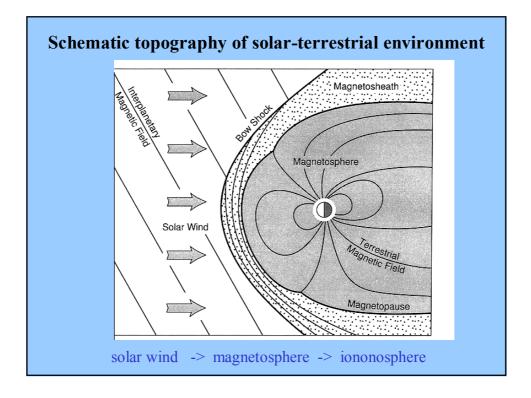
Space plasma particles are mostly free in the sense that their kinetic exceeds their potential energy, i.e. they are normally hot, T > 1000 K.

Space plasmas have typically *vast dimensions*, such that the free paths of thermal particles are larger than the typical spatial scales --> they are *collisionless*.

Different types plasmas

Plasmas differ by their chemical composition and the ionization degree of the ions or molecules (from different sources). Plasmas are mostly magnetized (internal and external magnetic fields).

- Solar interior and atmosphere
- Solar corona and wind (heliosphere)
- Planetary magnetospheres (plasma from solar wind)
- Planetary ionospheres (plasma from atmosphere)
- Coma and tail of a comet
- Dusty plasmas in planetary rings



Different plasma states

Plasmas differ by the charge, e_p mass, m_p temperature, T_p density, n_p bulk speed U_j and thermal speed, $V_j = (k_B T / m_j)^{1/2}$ of the particles (of species j) by which they are composed.

- Long-range (shielded) Coulomb potential
- Collective behaviour of particles
- Self-consistent electromagnetic fields
- Energy-dependent (often weak) collisions
- Reaction kinetics (ionization, recombination)
- Variable sources (pick-up)

Debye shielding

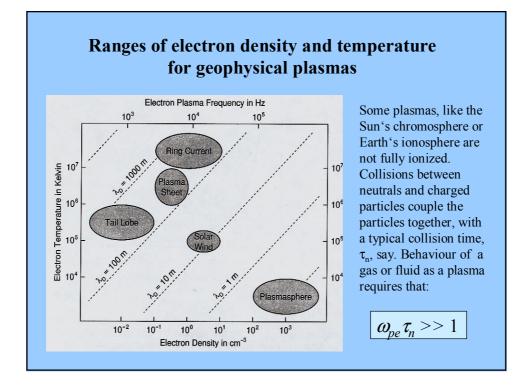
The mobility of free electrons leads to shielding of point charges (dressed particles) and their Coulomb potential.

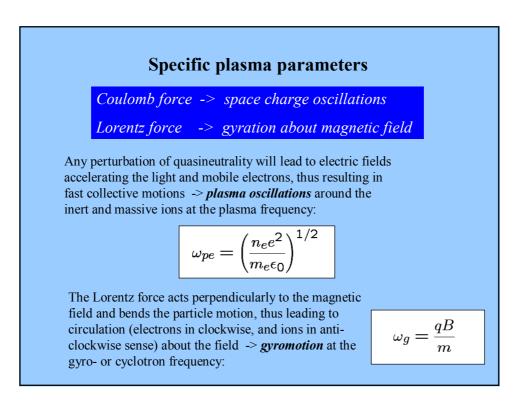
$$\phi_D = \frac{q}{4\pi\epsilon_0 r} exp\left(-\frac{r}{\lambda_D}\right)$$

The exponential function cuts off the electrostatic potential at distances larger than Debye length, λ_D , which for $n_e = n_i$ and $T_e = T_i$ is:

$$\lambda_D = \left(\frac{\epsilon_0 k_B T_e}{n_e e^2}\right)^{1/2}$$

The plasma is *quasineutral* on large scales, $L >> \lambda_D$, otherwise the shielding is ineffective, and one has microscopically a simple ionized gas. The plasma parameter (number of particles in the Debye sphere) must obey, $\Lambda = n_e \lambda_D^3 >> 1$, for *collective behaviour* to prevail.

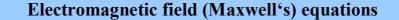




Theoretical descriptions of a plasma

Plasma dynamics is governed by the interaction of the charged particles with the self-generated (by their motions through their charge and current densities) electromagnetic fields. These internal fields feed back onto the particles and make plasma physics difficult.

- Single particle motion (under external fields)
- Magnetohydrodynamics (single fluid and Maxwell's equations)
- Multi-fluid approach (each species as a separate fluid)
- Kinetic theory (Vlasov-Boltzmann description in terms of particle velocity distribution functions and field spectra)



The motion of charged particles in space in strongly influenced by the self-generated electromagnetic fields, which evolve according to *Ampere's and Faraday's* (induction) laws:

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{j} + \epsilon_0 \mu_0 \frac{\partial \mathbf{E}}{\partial t}$$
$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

where ε_0 and μ_0 are the vacuum dielectric constant and free-space magnetic permeability, respectively. The charge density is ρ and the current density **j**. The electric field obeys *Gauss* law and the magnetic field is always free of divergence, i.e. we have:

$$\nabla \cdot \mathbf{E} = \rho/\epsilon_0 \qquad \qquad \nabla \cdot \mathbf{B} = 0$$

Electromagnetic forces and charge conservation

The motion of charged particles in space is determined by the electrostatic *Coulomb* force and magnetic *Lorentz* force:

$$\mathbf{F}_C = q\mathbf{E} \qquad \qquad \mathbf{F}_L = q(\mathbf{v} \times \mathbf{B})$$

where q is the charge and **v** the velocity of any charged particle. If we deal with electrons and various ionic species (index, s), the *charge and current densities* are obtained, respectively, by summation over all kinds of species as follows:

$$\rho = \sum_{s} q_{s} n_{s} \qquad \qquad \mathbf{j} = \sum_{s} q_{s} n_{s} \mathbf{v}_{s}$$

which together obey the *continuity equation*, because the number of charges is conserved, i.e. we have:

 $\frac{\partial \rho}{\partial t} + \nabla \cdot \mathbf{j} = \mathbf{0}$

Lorentz transformation of the electromagnetic fields

Let S be an inertial frame of reference and S' be another frame moving relative to S at constant velovity \mathbf{V} . Then the electromagnetic fields in both frames are connected to each other by the *Lorentz transformation*:

	$B'_x = B_x$
$E'_x = E_x$	$B'_y = \gamma \left(B_y + \frac{V}{c^2} E_z \right)$
$E'_y = \gamma(E_y - VB_z)$	
$E_z' = \gamma(E_z + VB_y)$	$B'_z = \gamma \left(B_z - \frac{v}{c^2} E_y \right)$

where $\gamma = (1-V^2/c^2)^{-1/2}$ is the *Lorentz factor* and c the speed of light. In the non-relativistic case, V << c, we have $\gamma = 1$, and thus **B'** \approx **B**. The magnetic field remains to lowest order unchanged in frame transformations.

However, the electric field obeys, $\mathbf{E}' \approx \mathbf{E} + \mathbf{V} \times \mathbf{B}$. A space plasma is usually a very good conductor, and thus we have, $\mathbf{E}' = \mathbf{0}$, and the result, $\mathbf{E} \approx -\mathbf{V} \times \mathbf{B}$, which is called the *convection electric field*.

Induction equation

In order to study the transport of plasma and magnetic field lines quantitatively, let us consider the fundamental induction equation, i.e. *Faraday's law* in combination with the simple phenomenological *Ohm's law*, relating the electric field in the plasma frame with its current:

$$\mathbf{j} = \sigma_0(\mathbf{E} + \mathbf{v} \times \mathbf{B})$$

Using *Ampere's law* for slow time variations, without the displacement current and the fact that the field is free of divergence ($\nabla \cdot \mathbf{B} = \mathbf{0}$), yields the induction equation (with conductivity σ_0):

$$\frac{\partial \mathbf{B}}{\partial t} = \nabla \times (\mathbf{v} \times \mathbf{B}) + \frac{1}{\mu_0 \sigma_0} \nabla^2 \mathbf{B}$$
Convection Diffusion

